

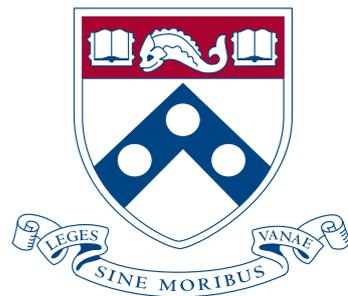
# ITK v4 Registration Refactoring

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Feb 2, 2011

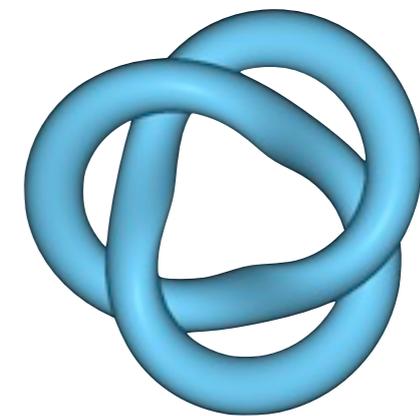
Brian Avants, Nick Tustison, Gang Song, Michael Stauffer, Shreyas Seshamani, James C. Gee

Penn Image Computing and Sciences Laboratory  
University of Pennsylvania, Philadelphia, PA.



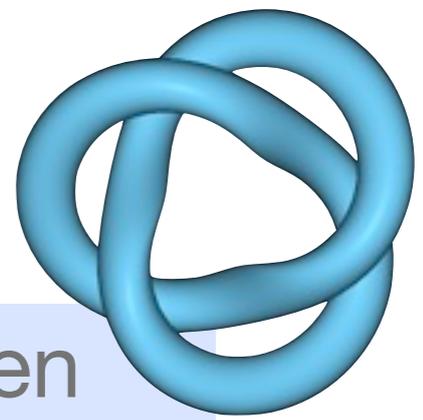
# What moves ITK registration forward

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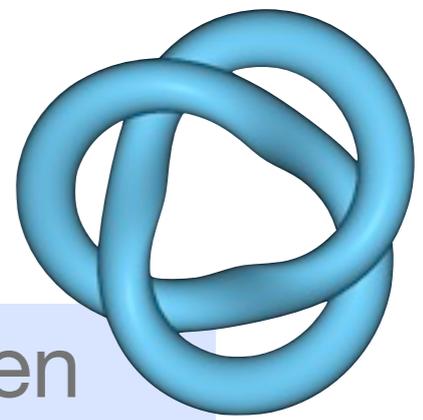
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- **Hans Johnson:** why does Mattes MI fail in ITK v4 when the same code worked in ITK320? BSplines?

# What moves ITK registration forward

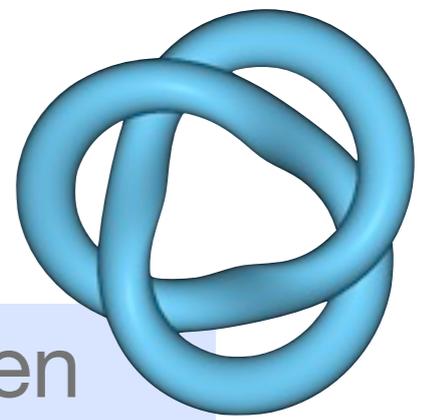
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# What moves ITK registration forward

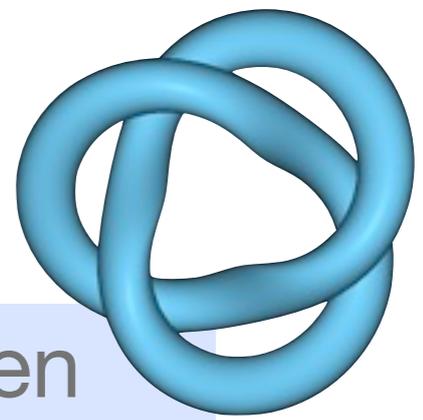
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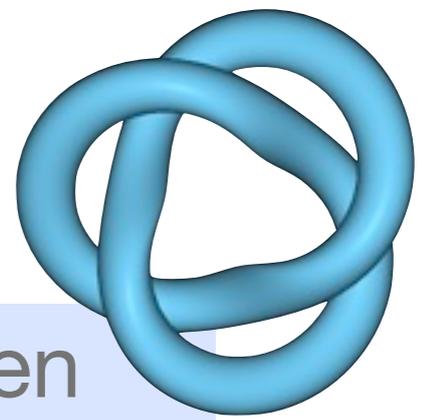
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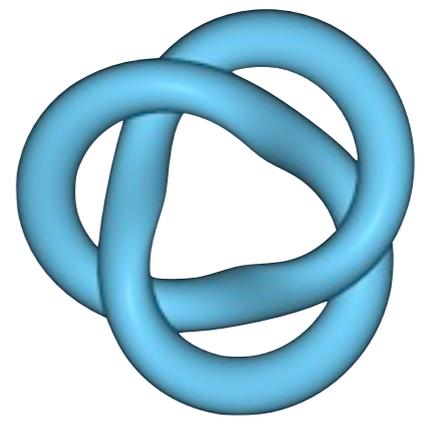
# What moves ITK registration forward

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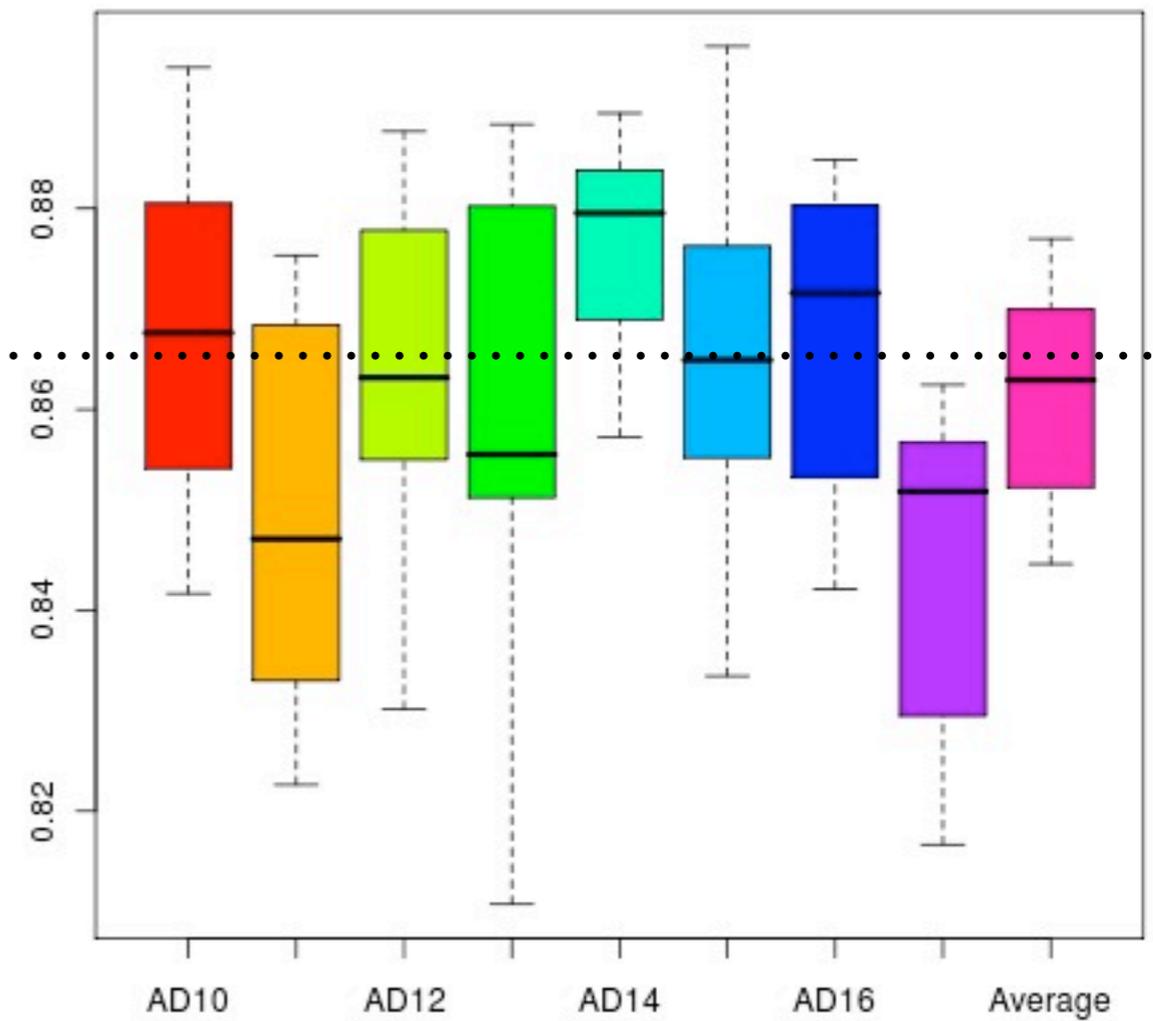
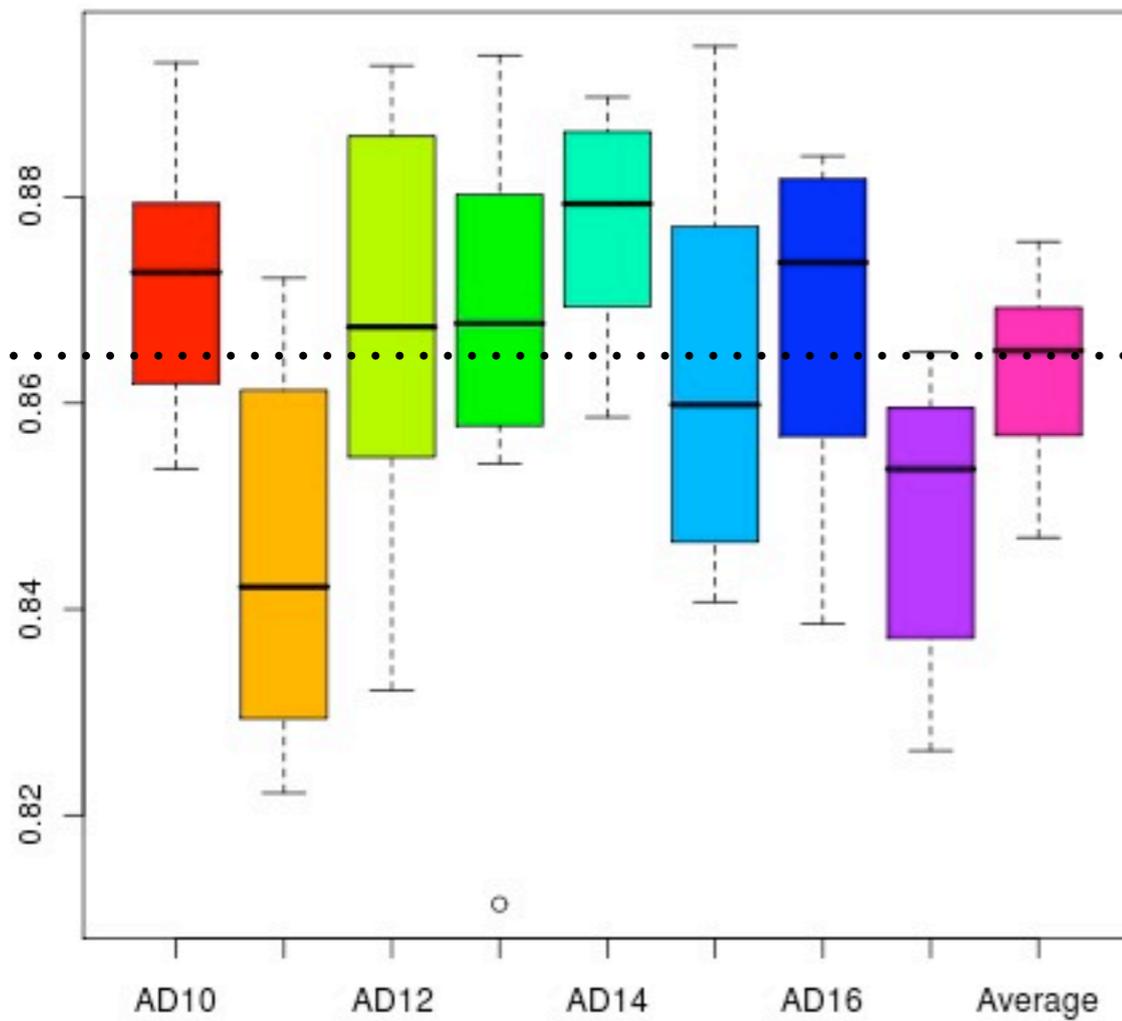


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- **Slicer:** big projects that we want to support. Kilian asks “why is resampling taking longer than registration?”
- **New theory:** interesting ideas we should be able to easily implement. E.g. LDDMM, longitudinal mapping, multivariate problems ...

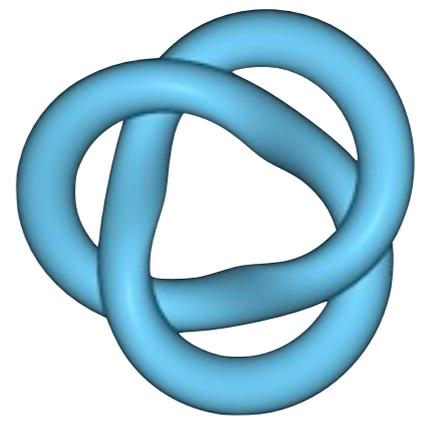
# ITK Mattes MI vs FSL correlation ratio



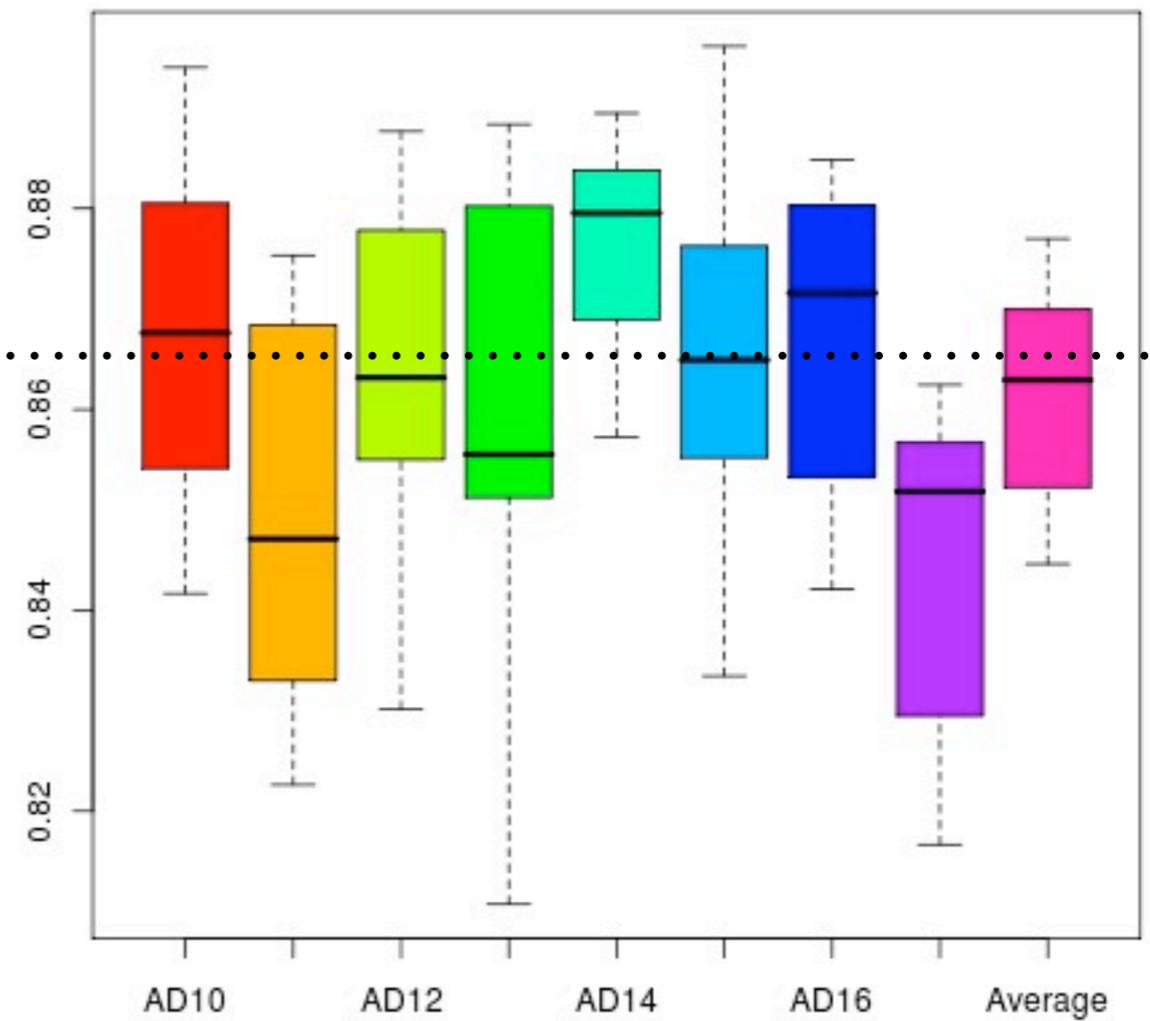
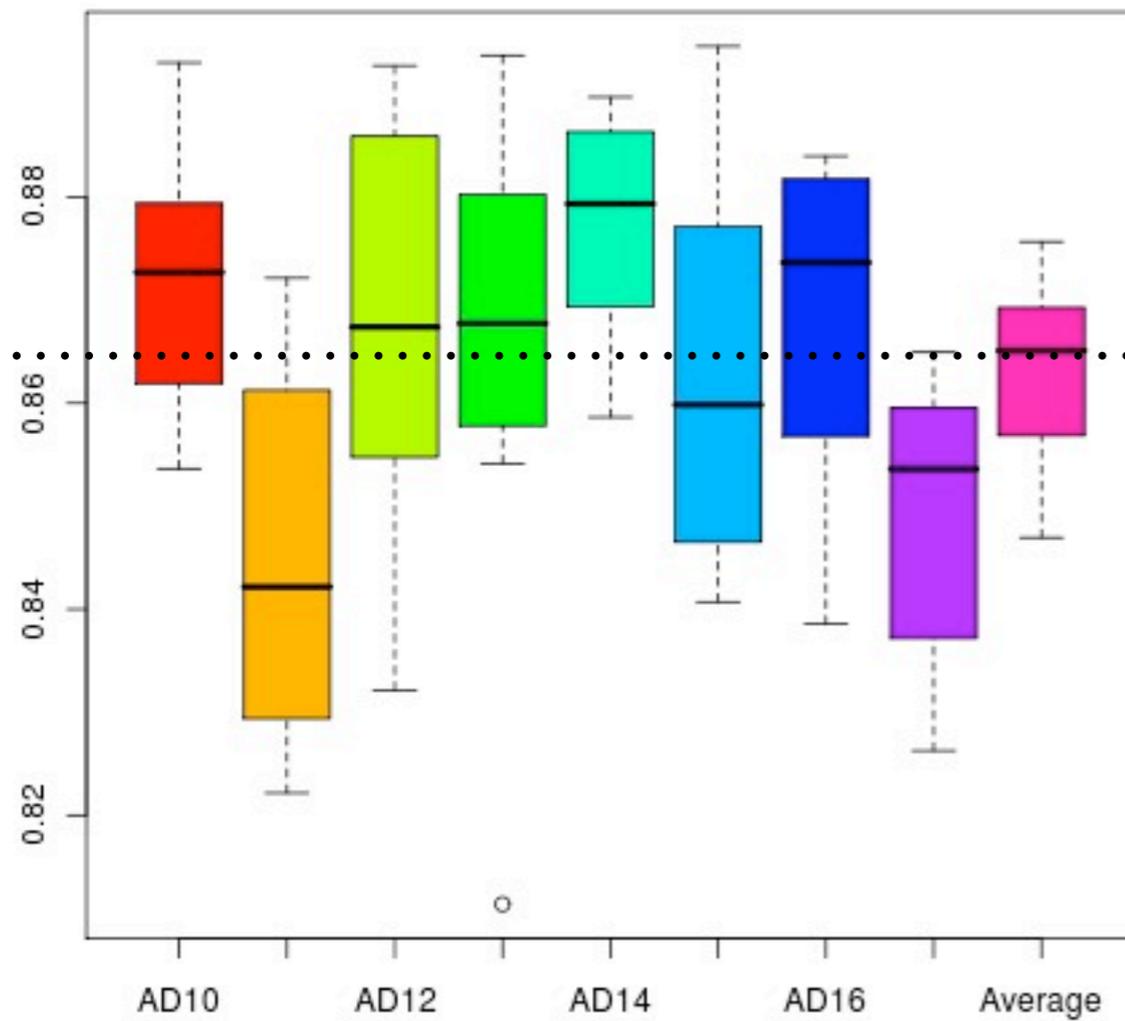
Evaluate brain overlap in neuroimages



# ITK Mattes MI vs FSL correlation ratio

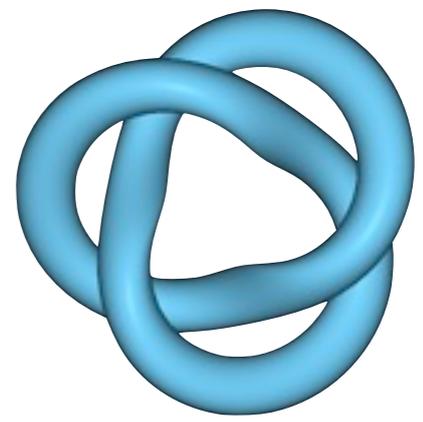


Evaluate brain overlap in neuroimages

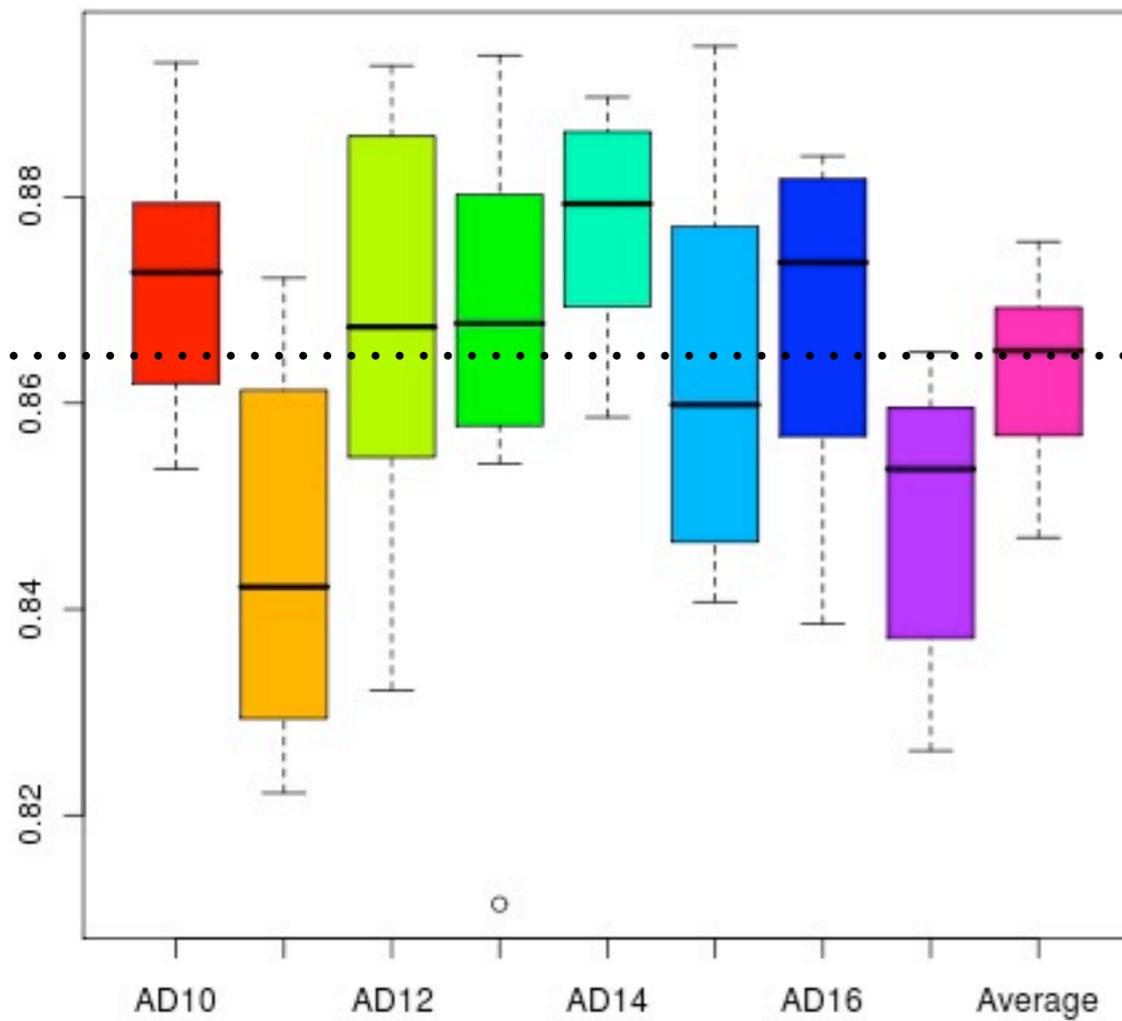


Default ANTs parameters  
and optimization.

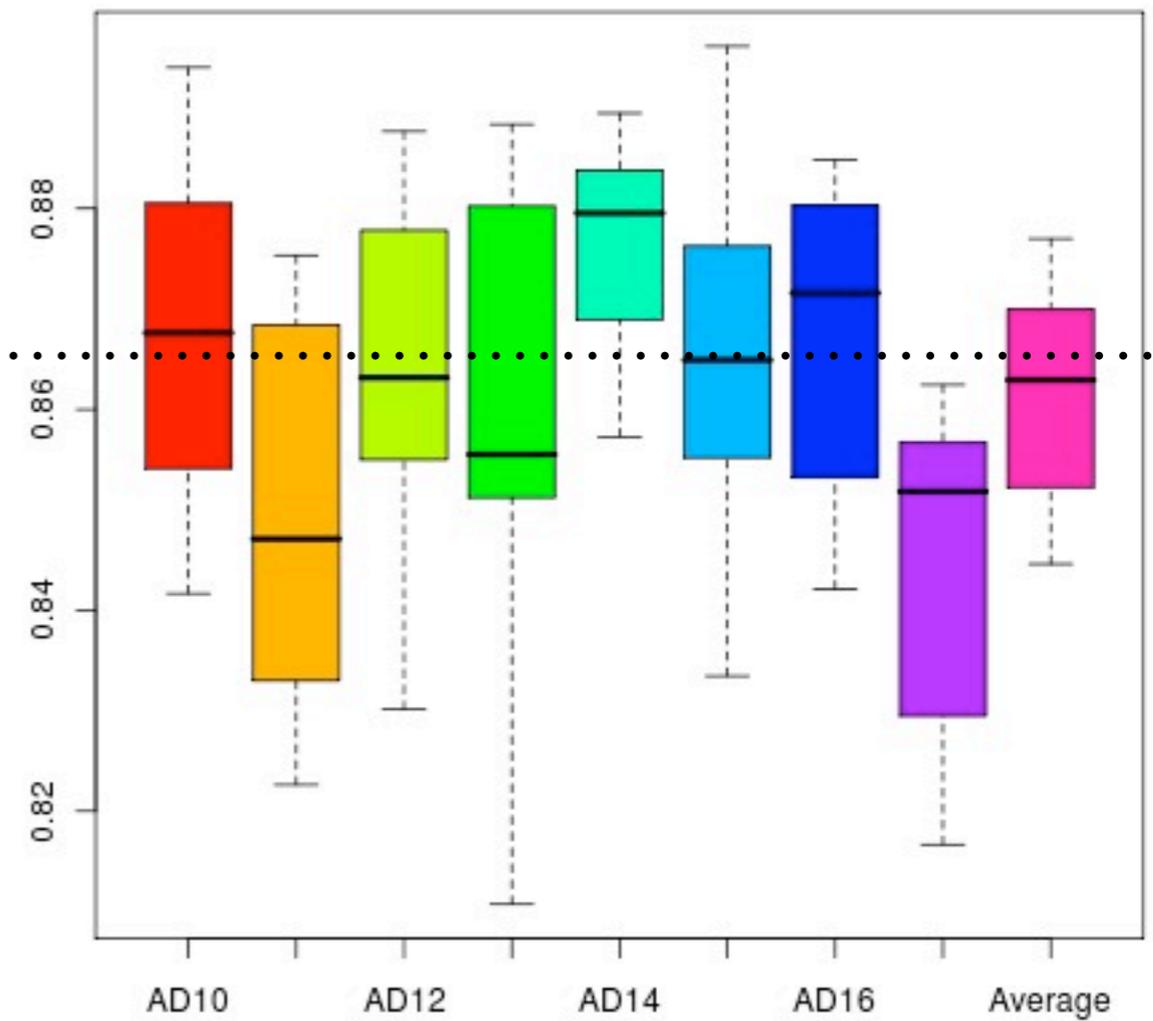
# ITK Mattes MI vs FSL correlation ratio



Evaluate brain overlap in neuroimages



Default ANTs parameters and optimization.



Default FSL parameters and optimization.

# Biased registration

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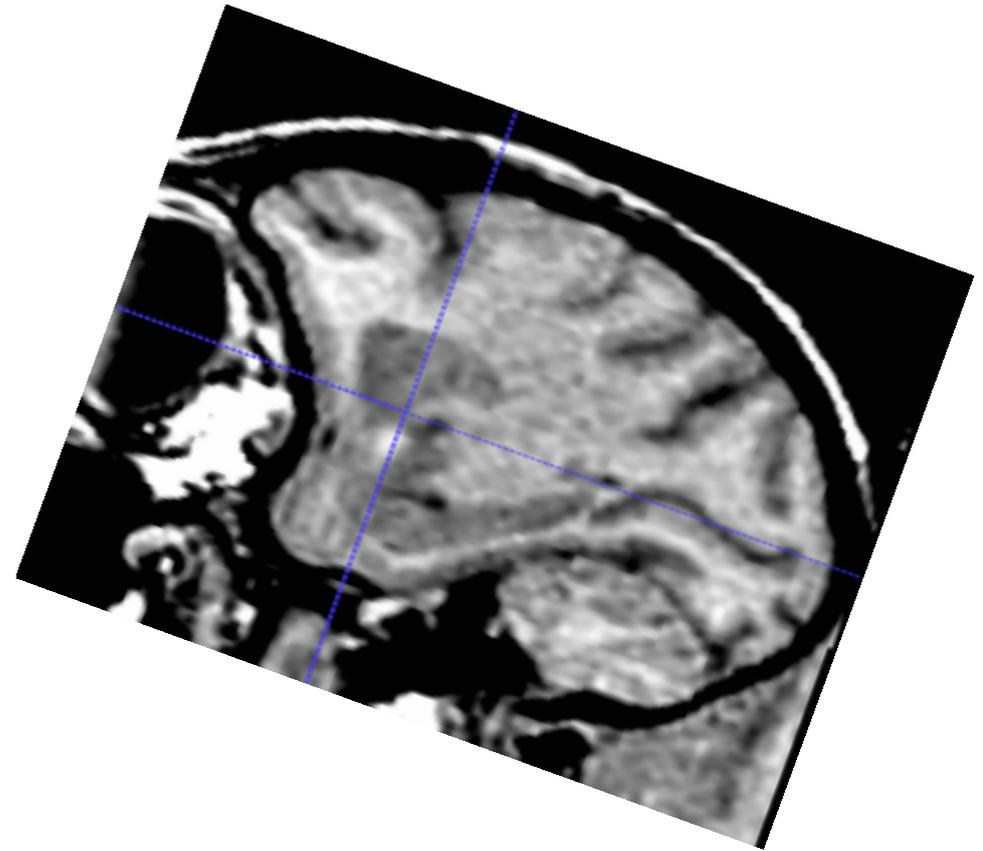
A

B

# Biased registration

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A

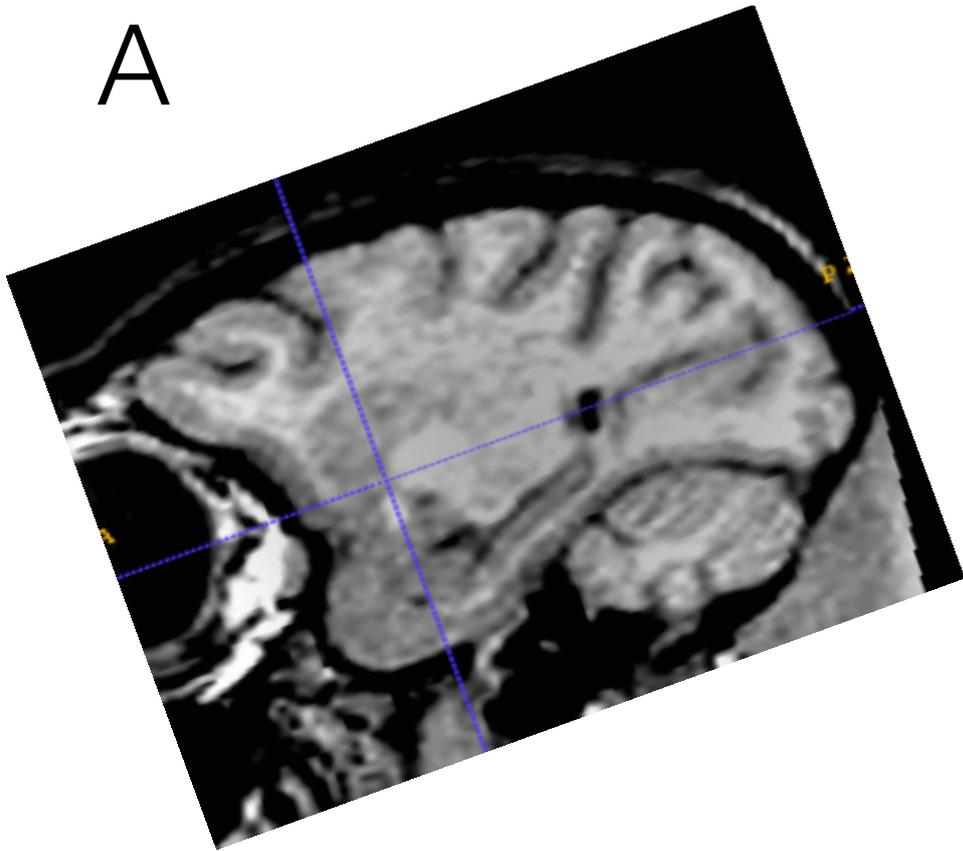


B

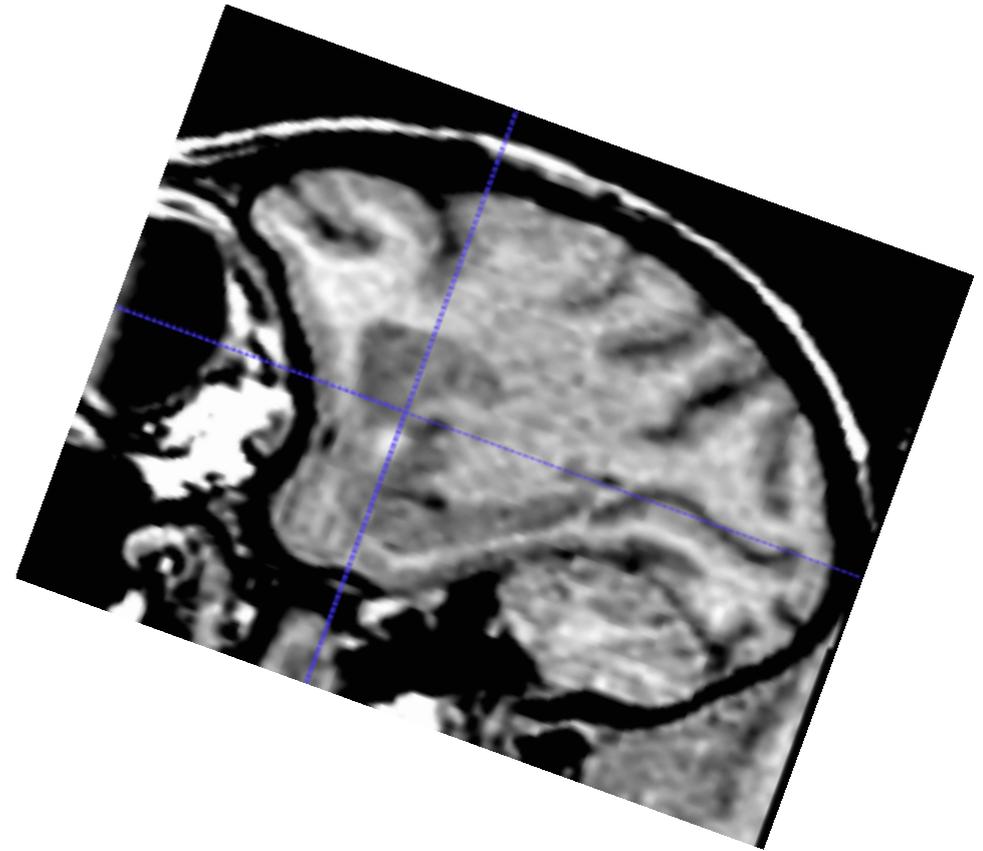
# Biased registration

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A

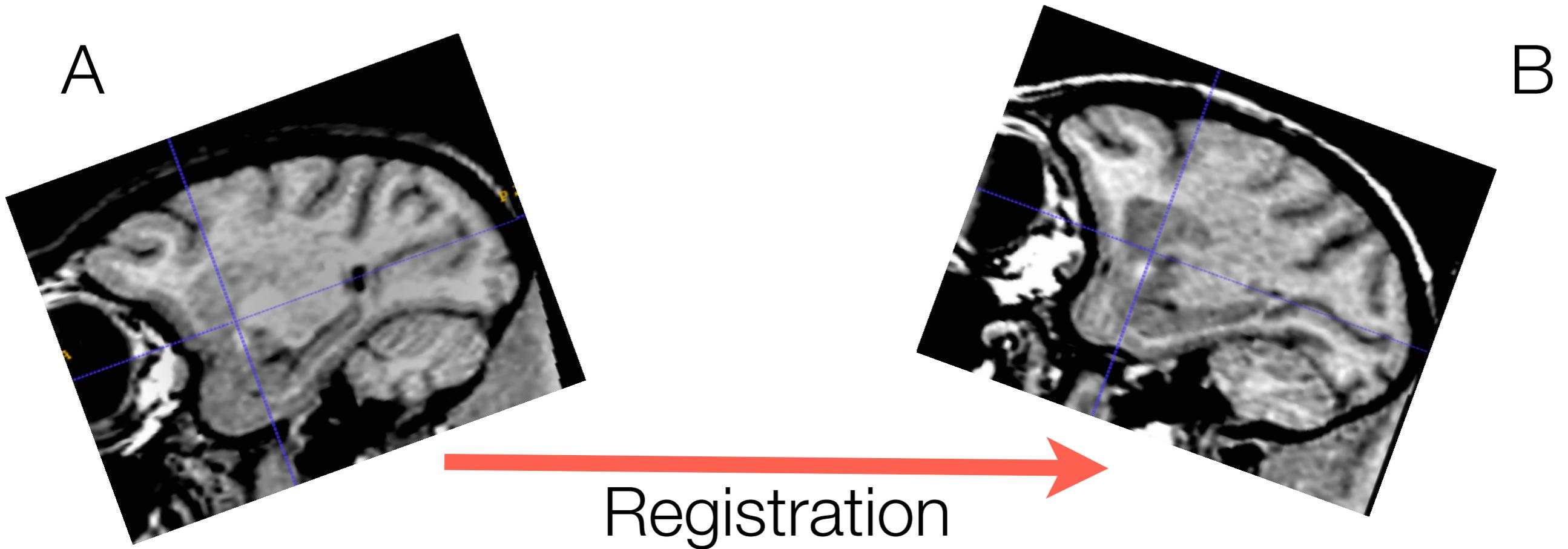


B



# Biased registration

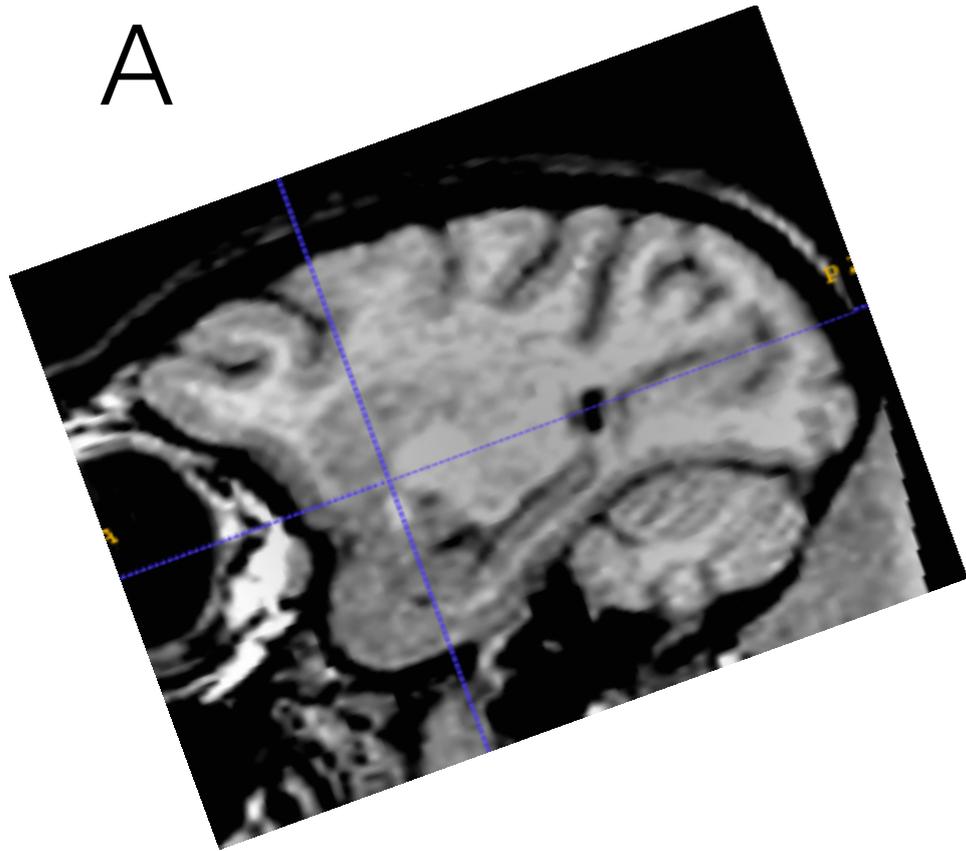
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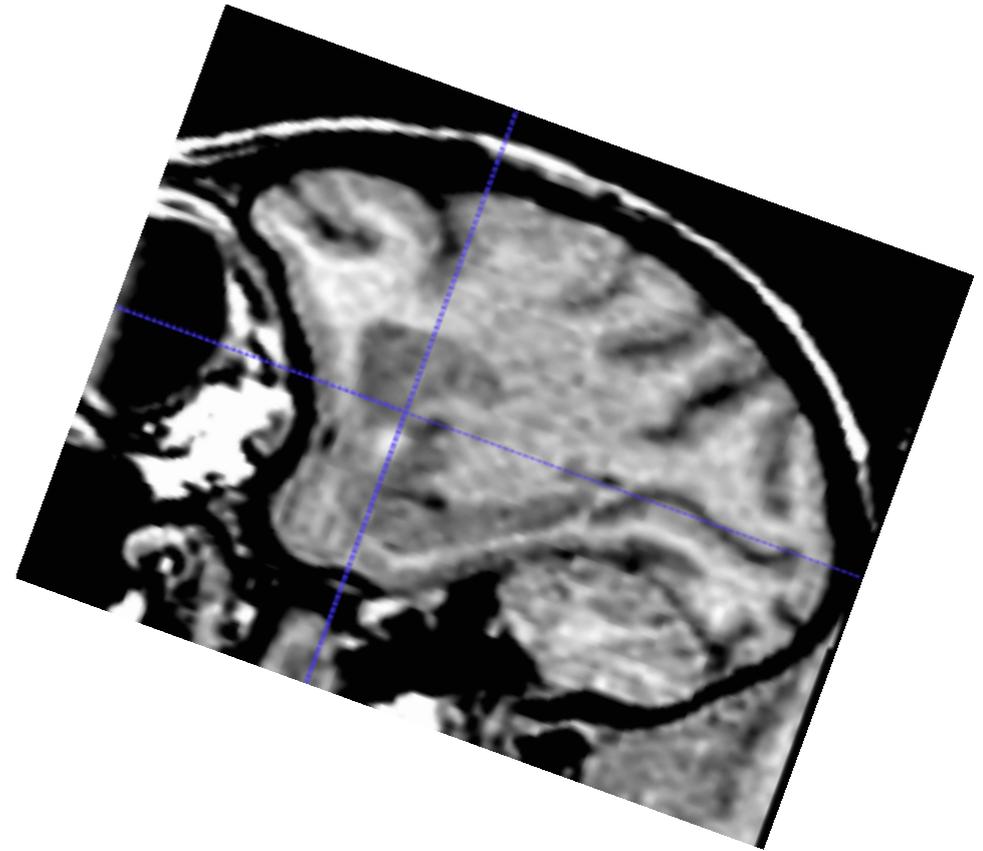
# Unbiased registration

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A



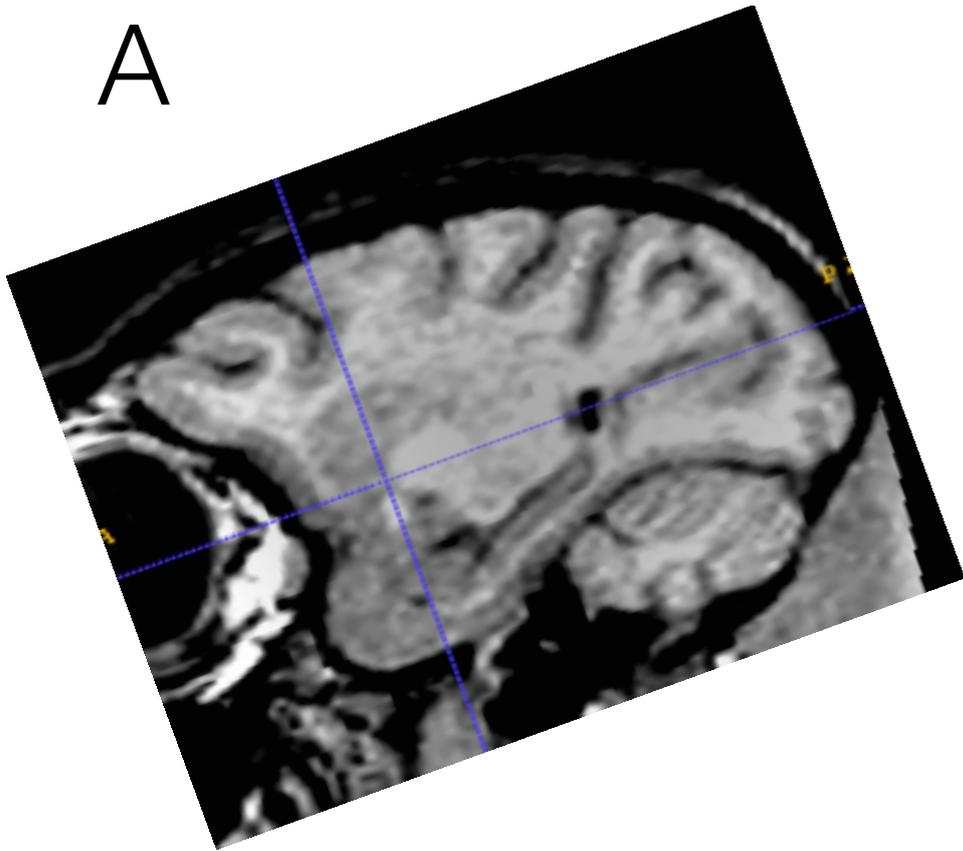
B



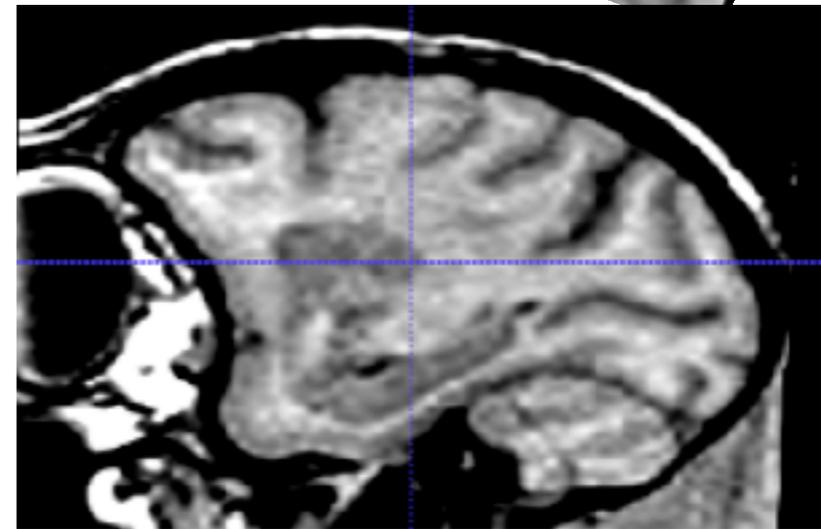
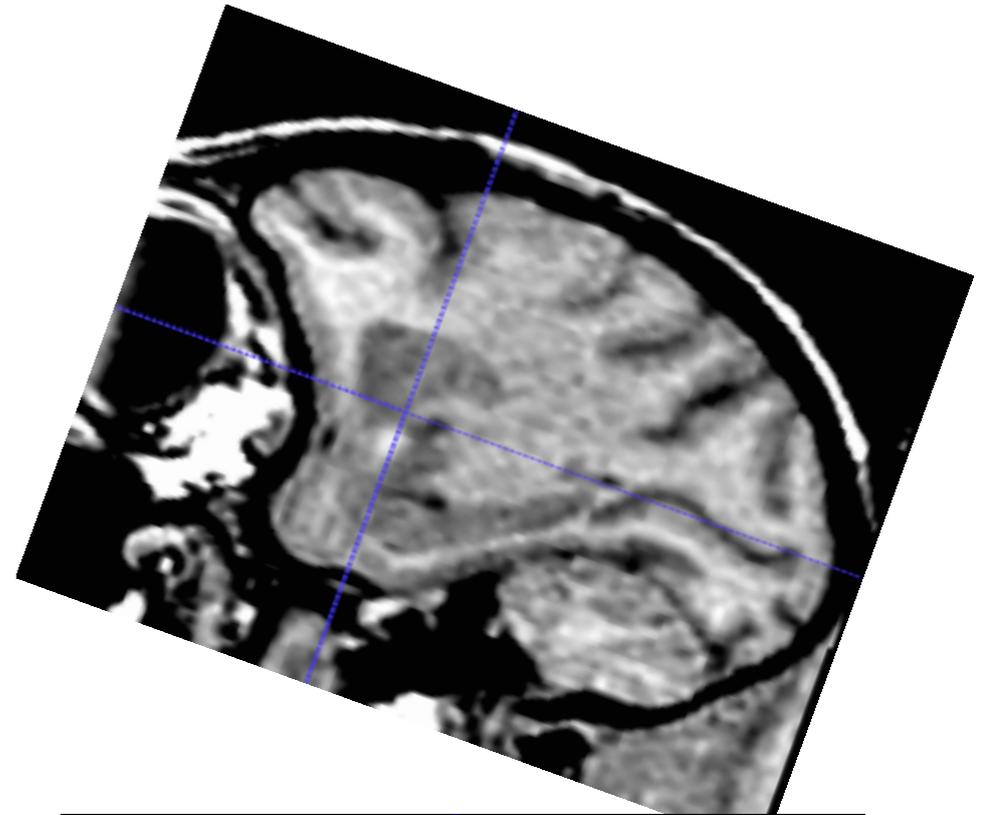
# Unbiased registration

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A



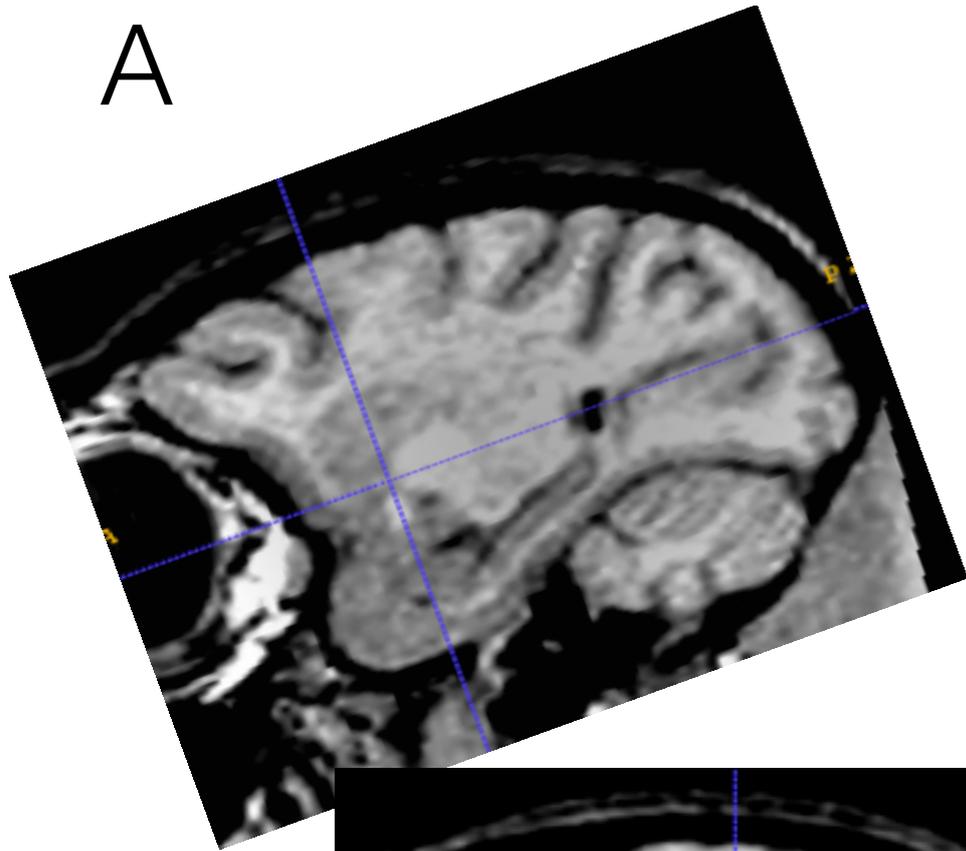
B



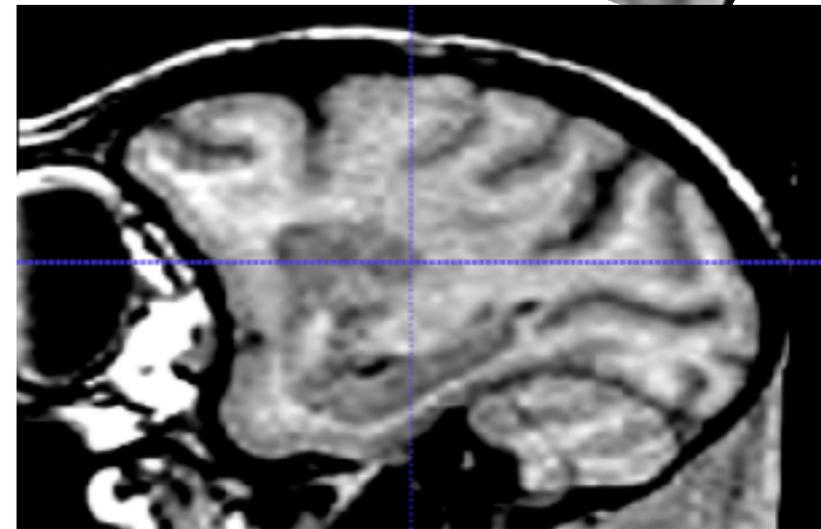
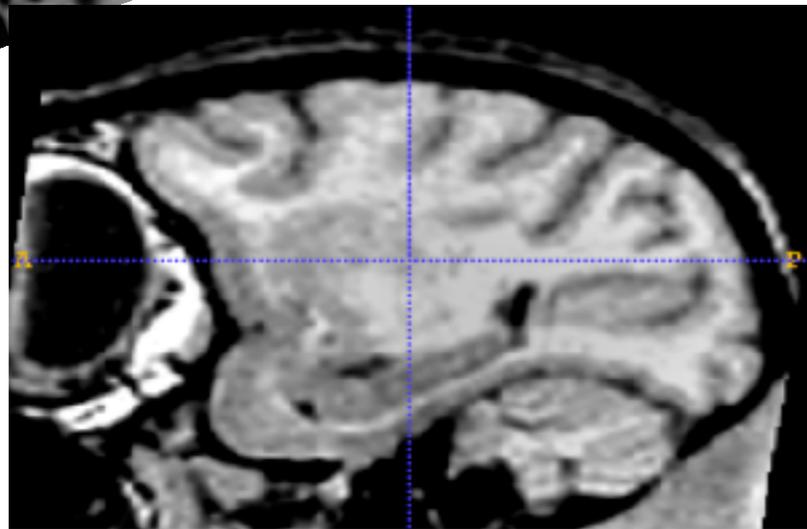
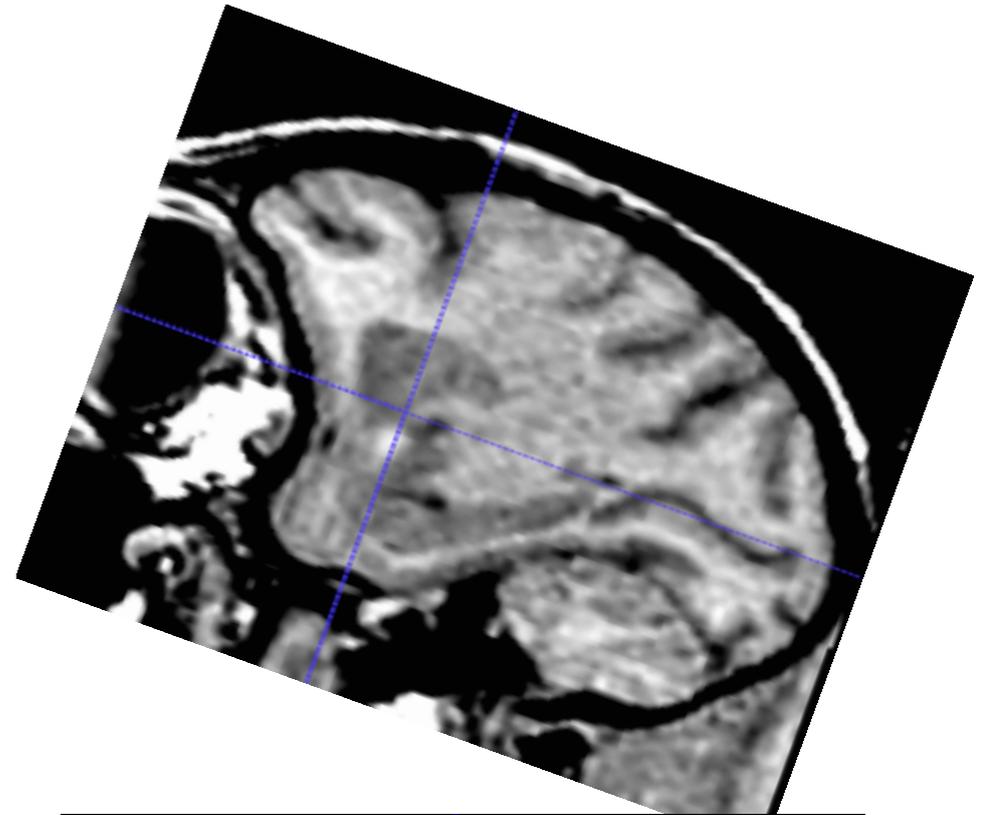
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A



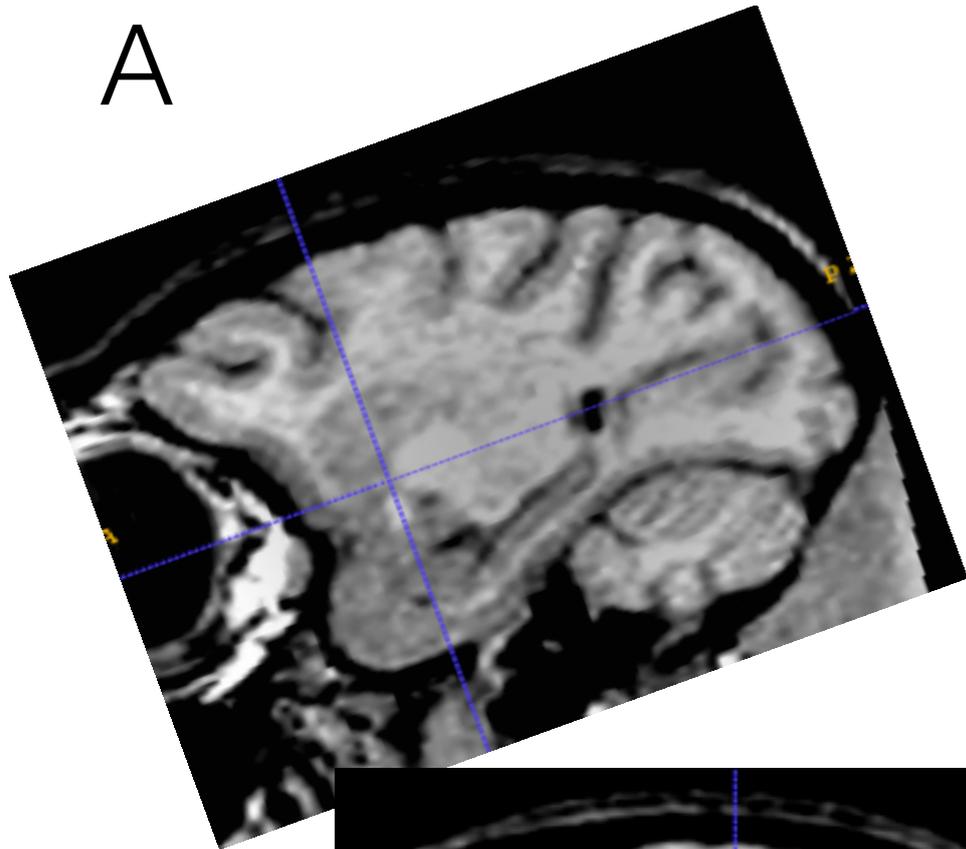
B



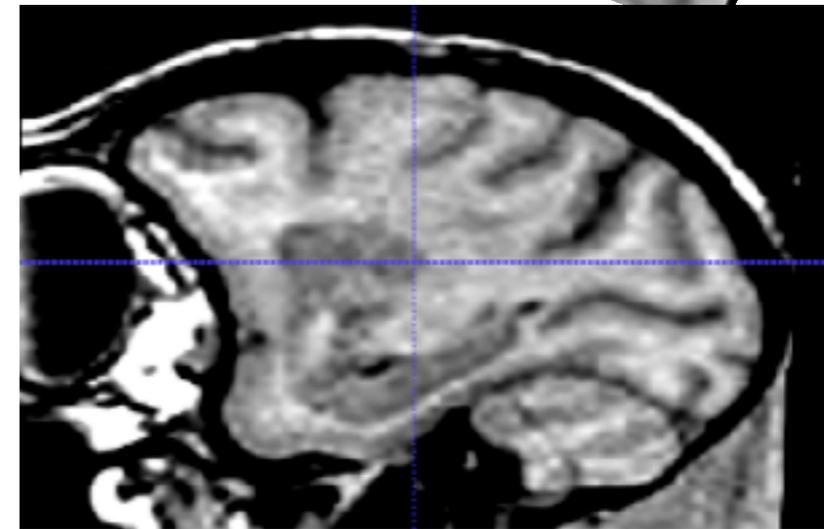
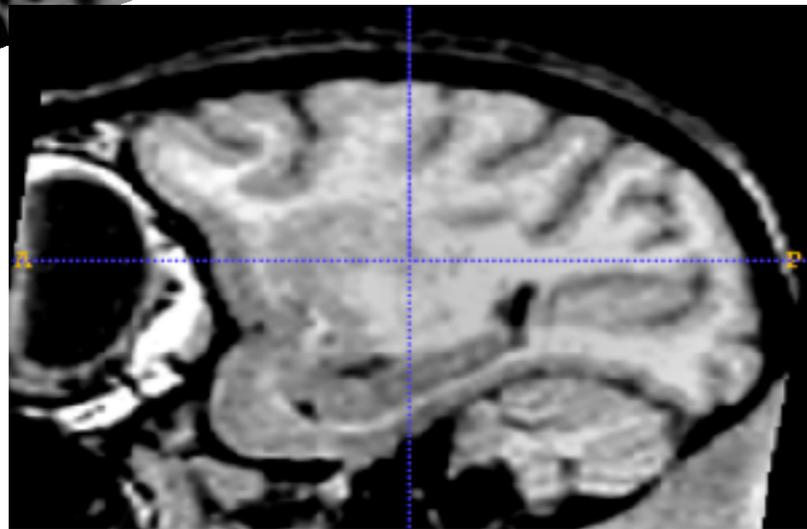
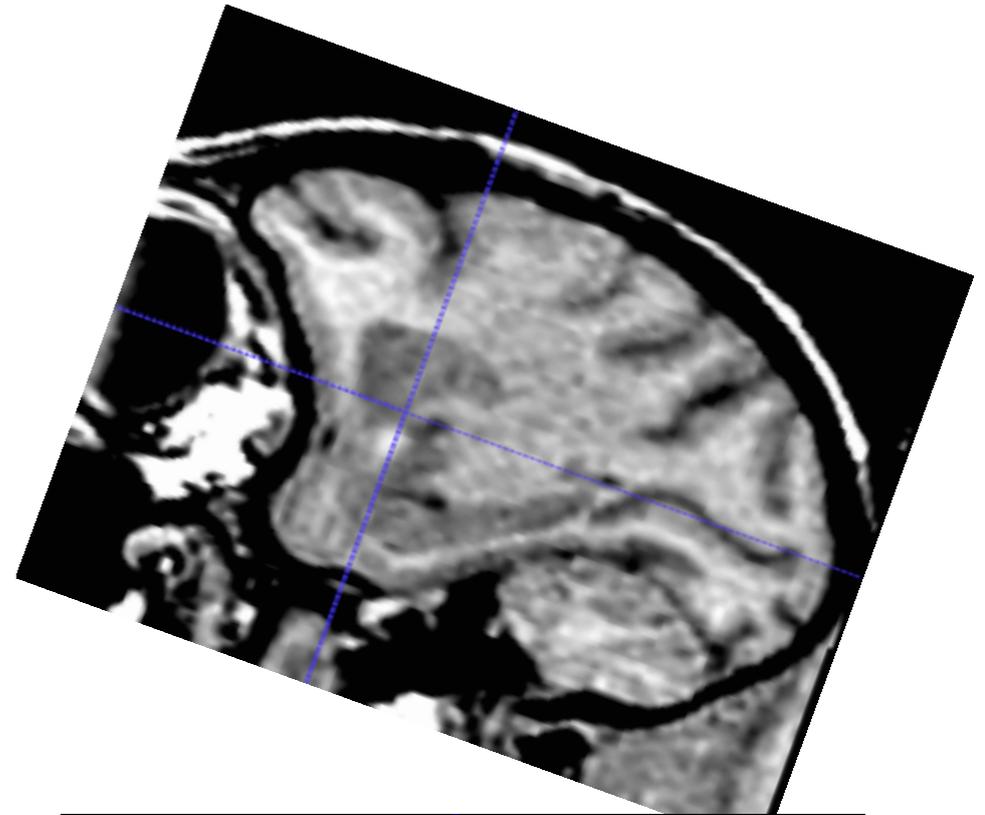
# Unbiased registration

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A

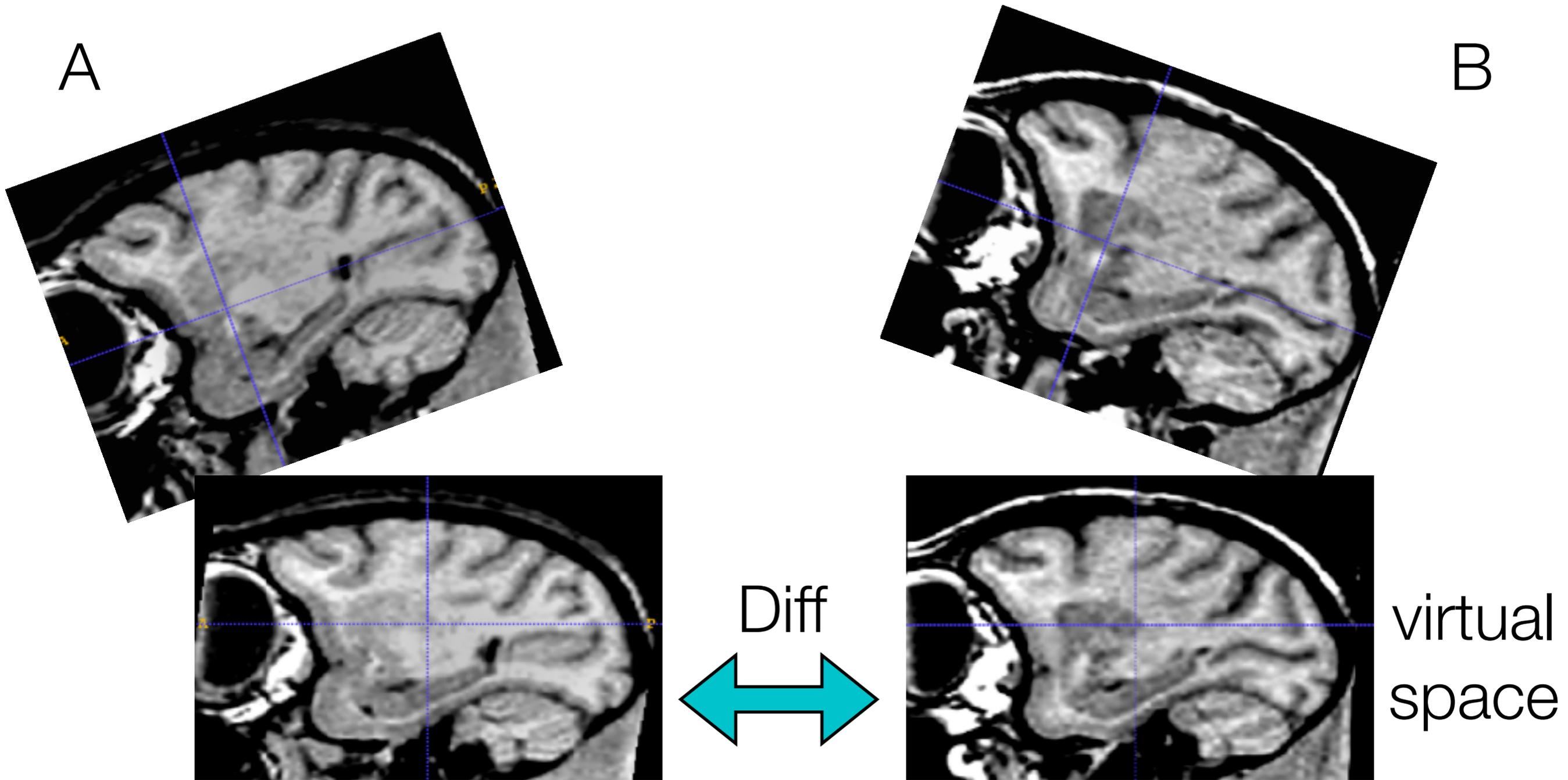


B

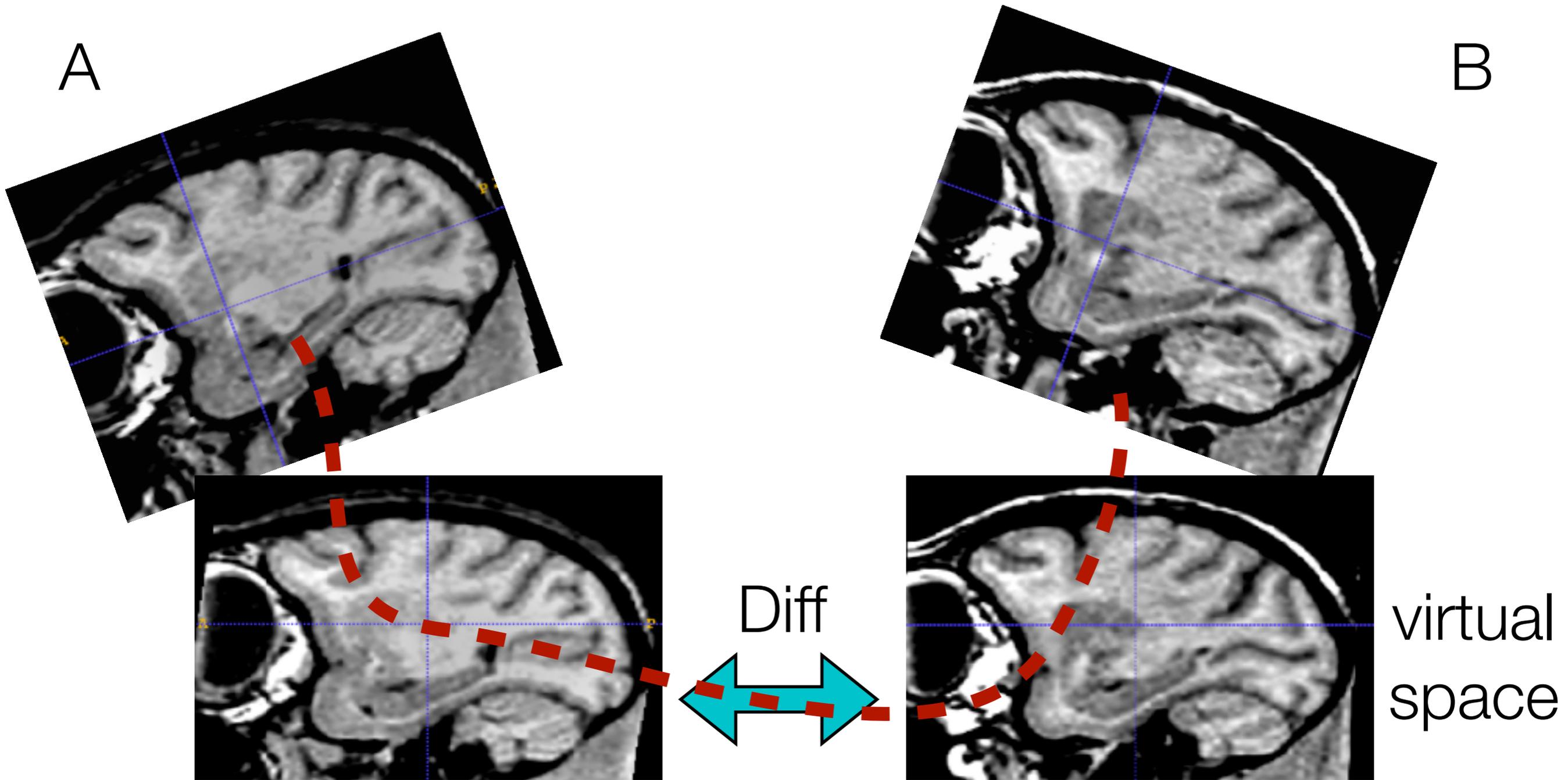


virtual  
space

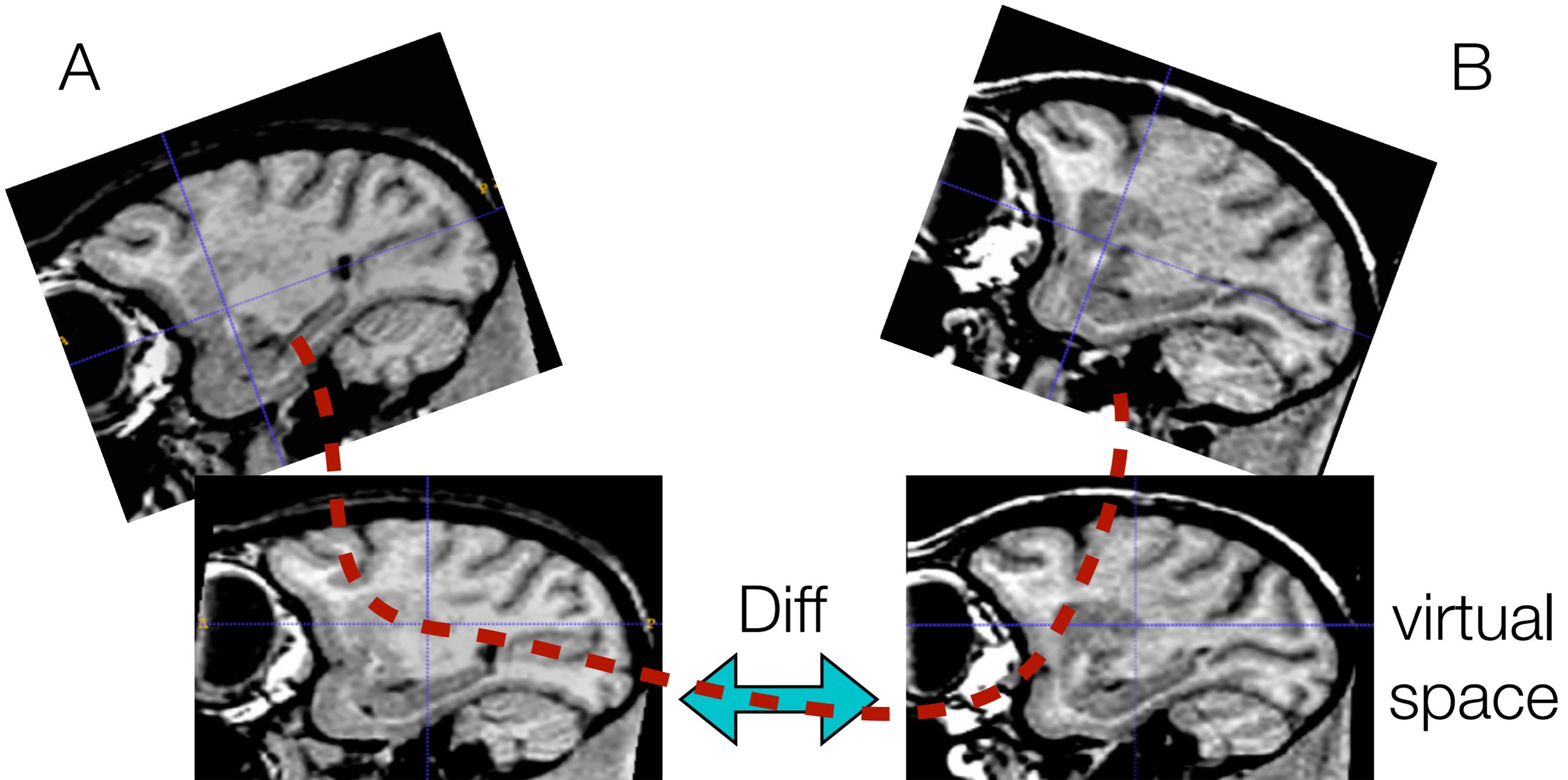
# Unbiased registration



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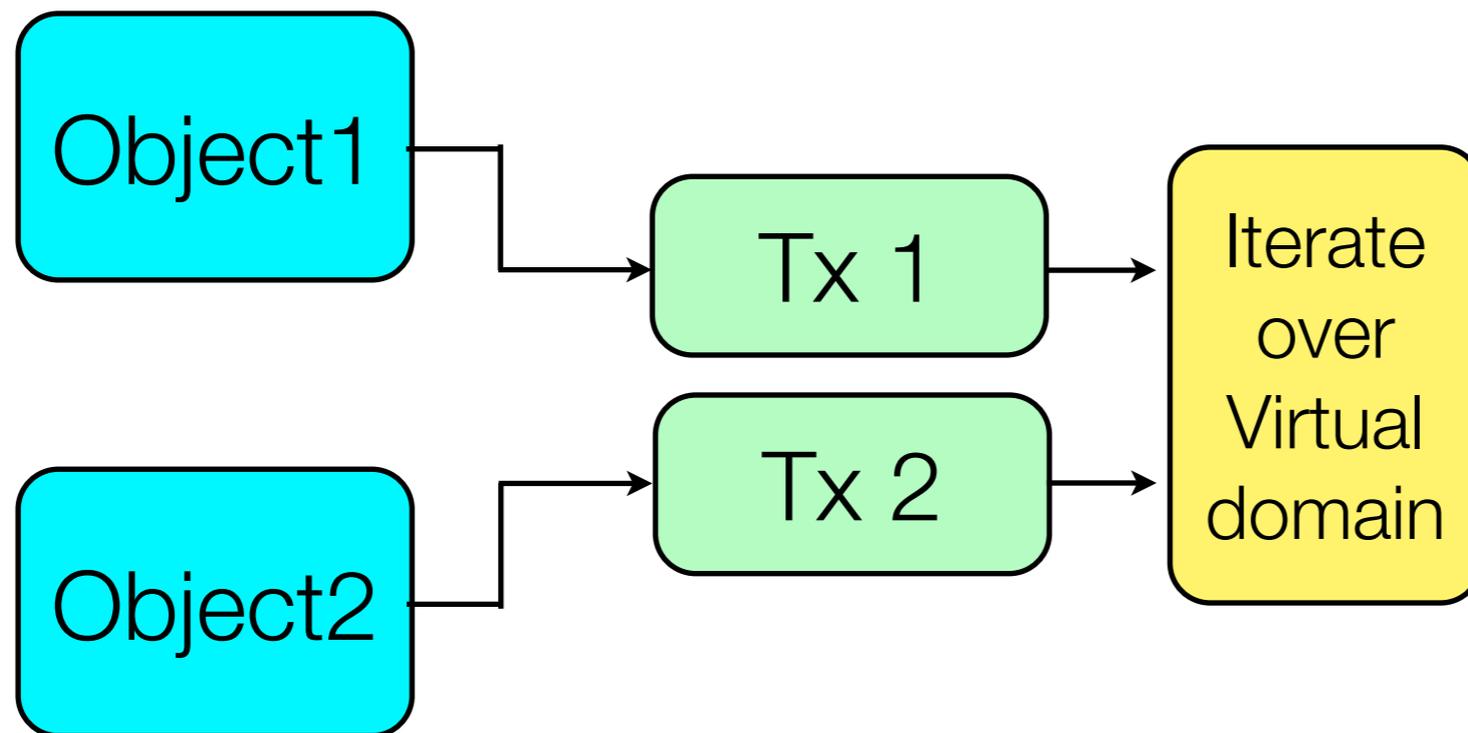
# Unbiased registration



Important for longitudinal studies (Yushkevich, et al, 2010)

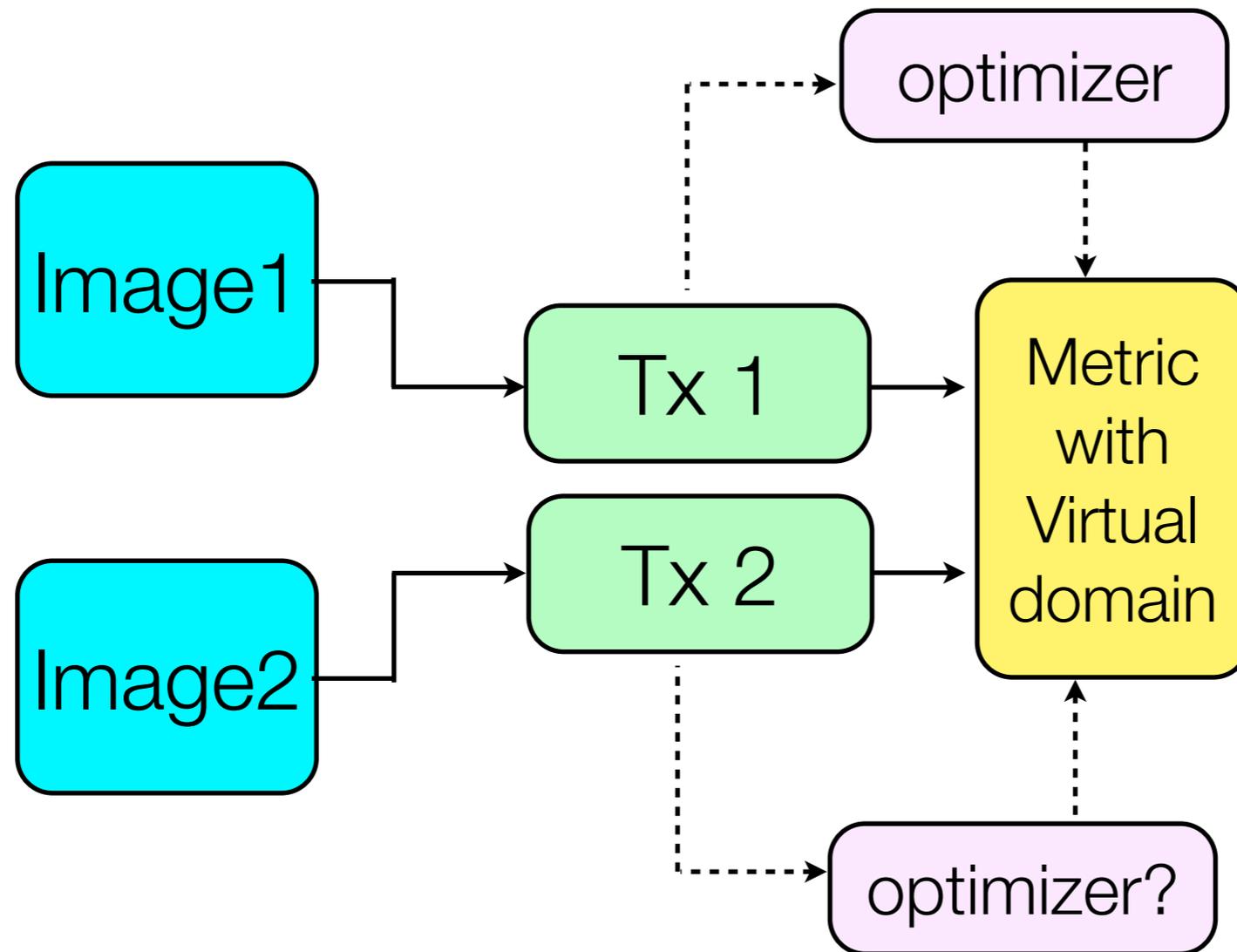
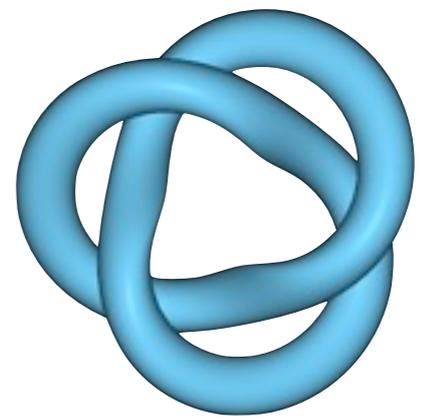
# Object to object metric

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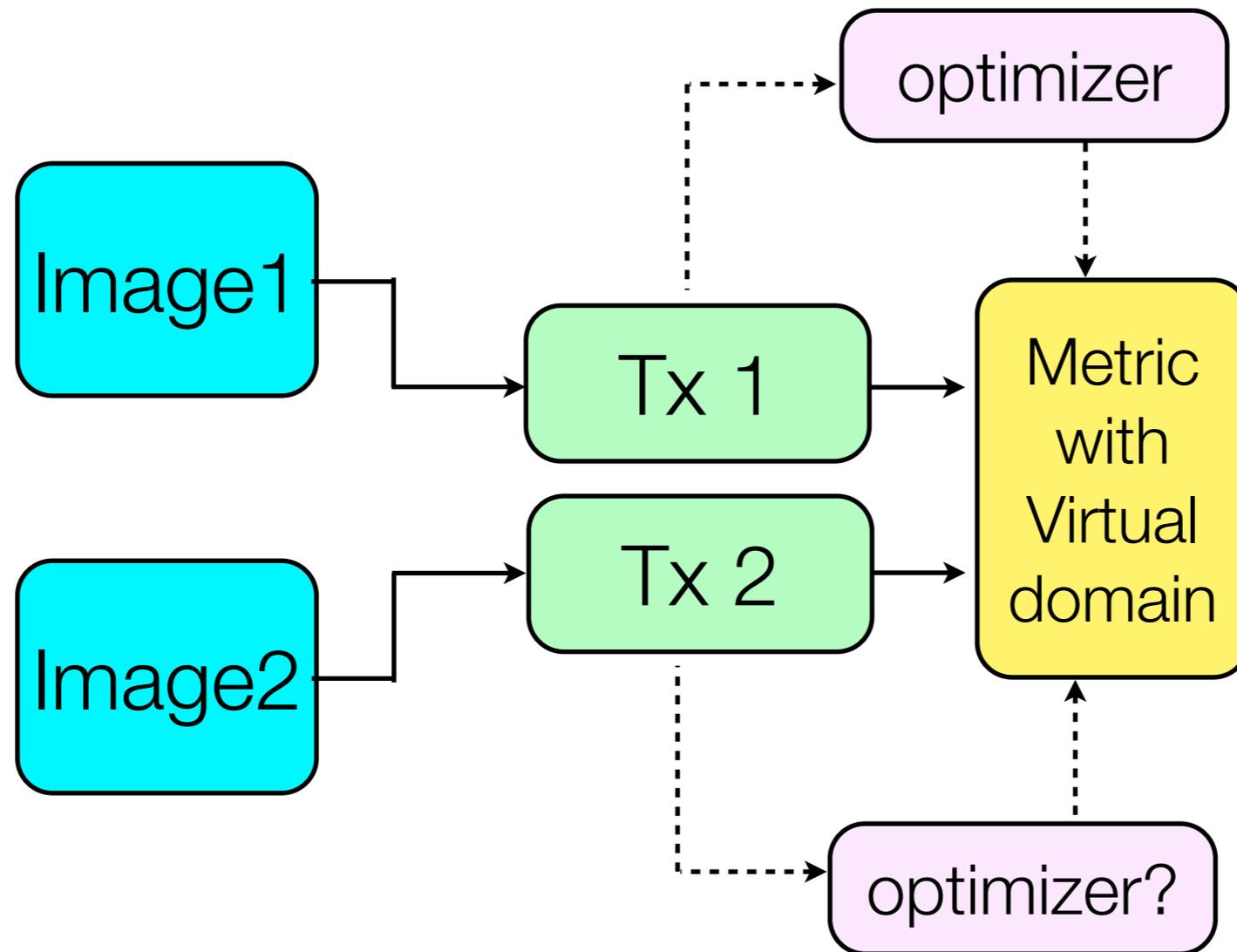
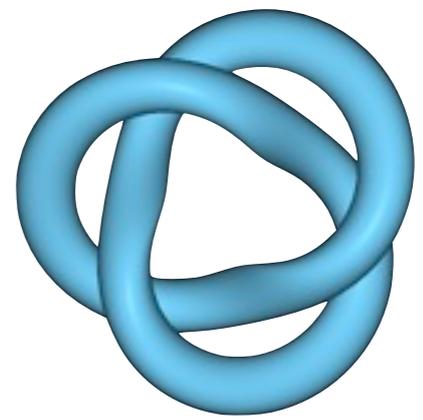


Requires a generic iterator type.

# Registration machinery object

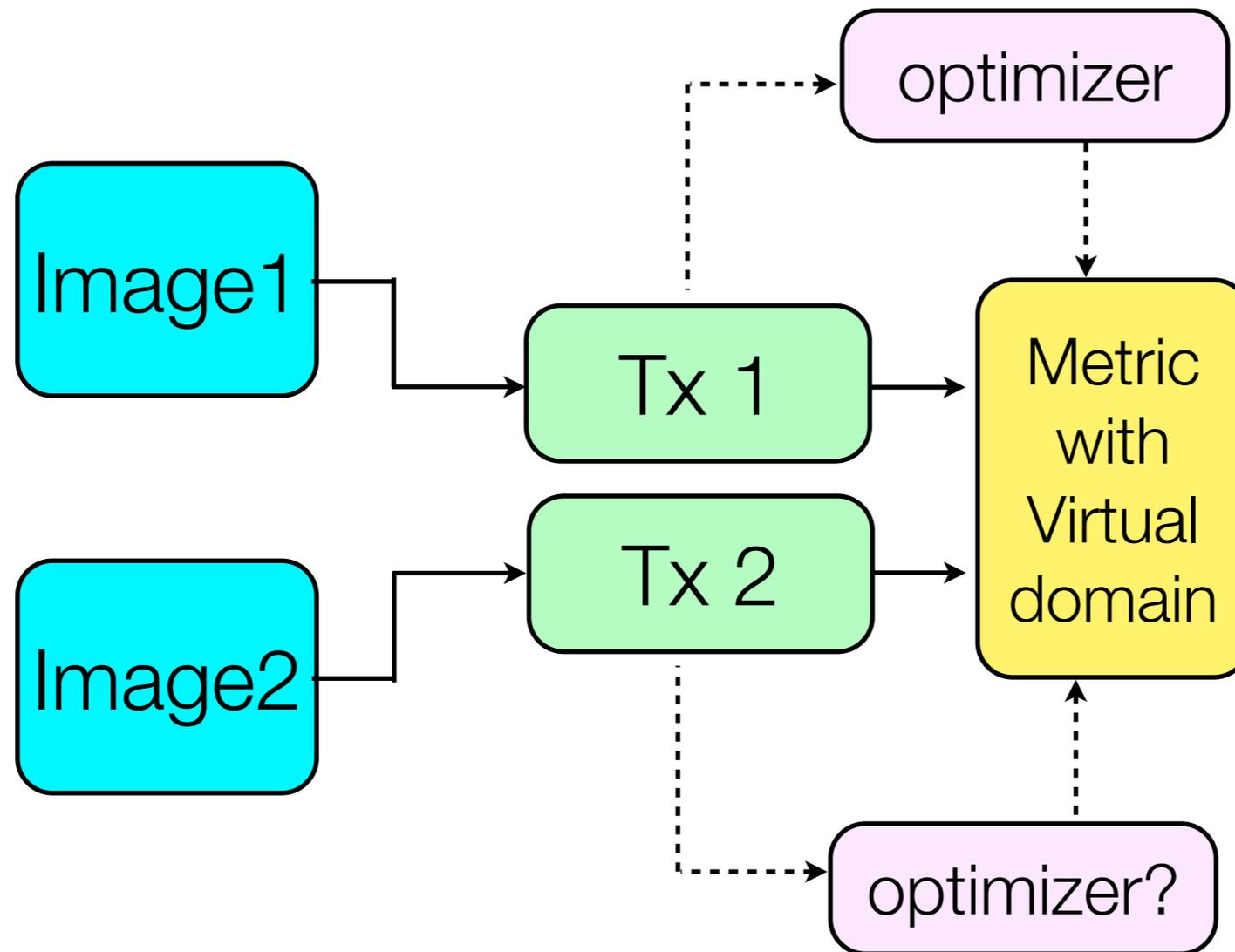
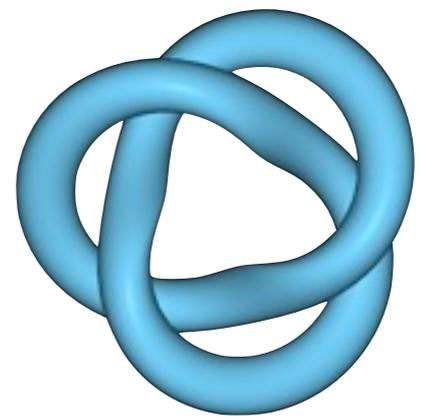


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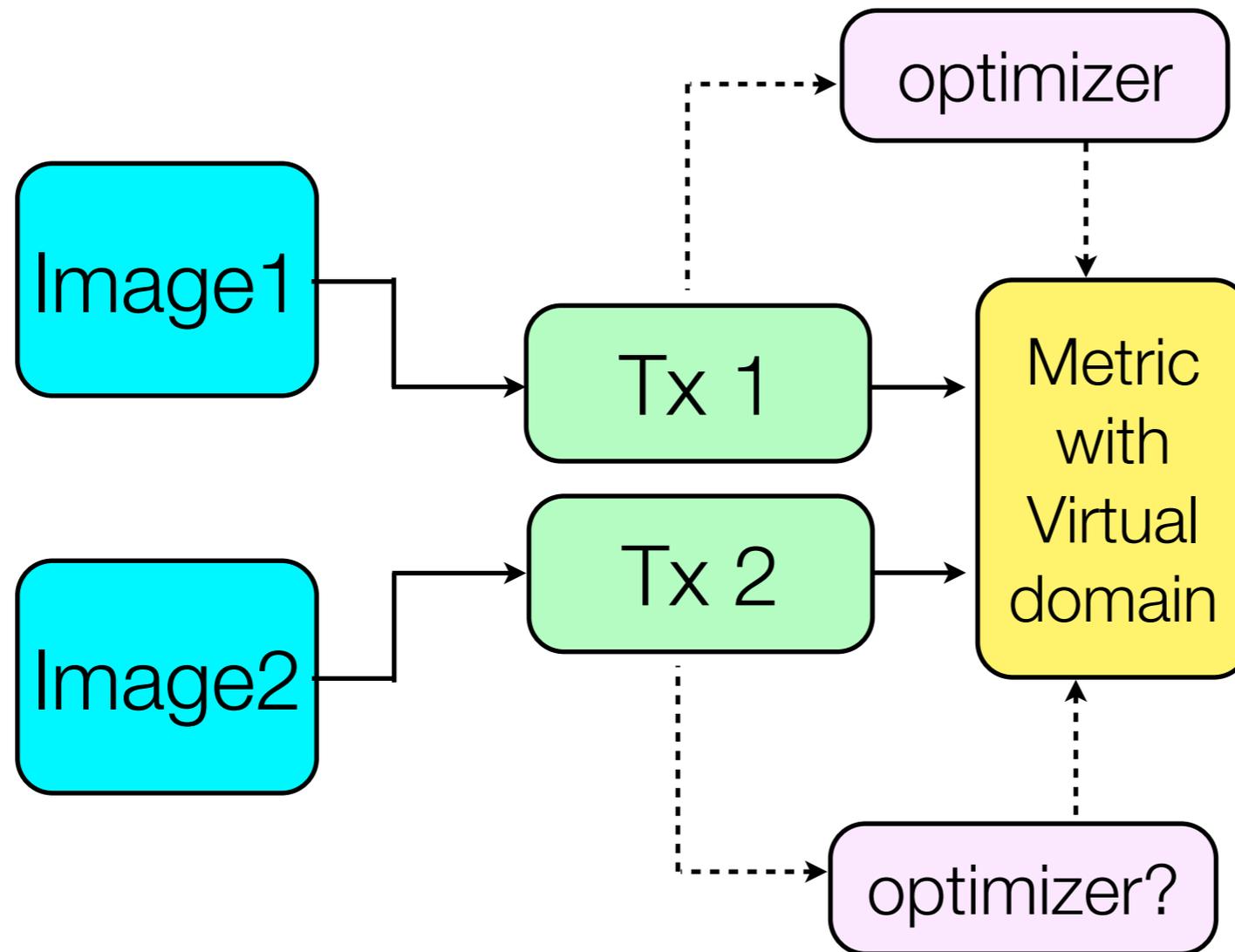
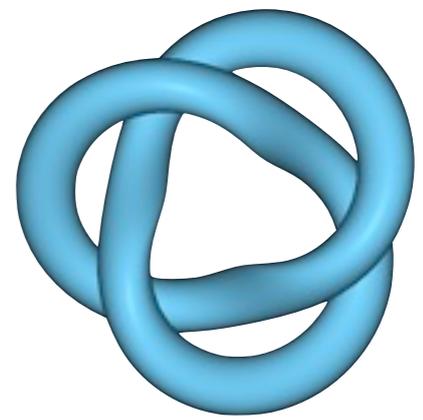
Virtual domain a critical component. Downsampling, more.

# Registration machinery object



Virtual domain a critical component. Downsampling, more.  
Tx1 and Tx2 are composite transforms.

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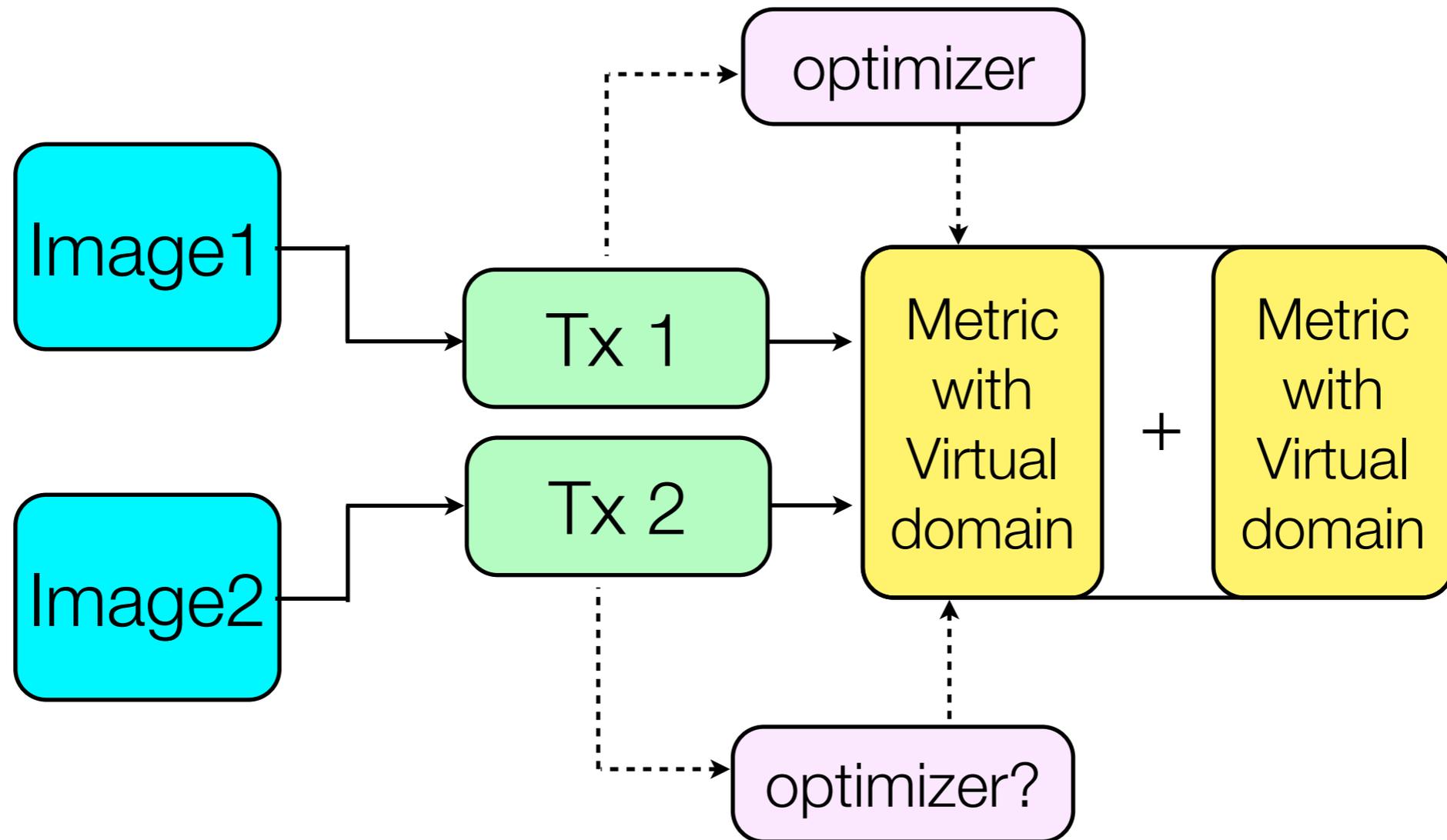
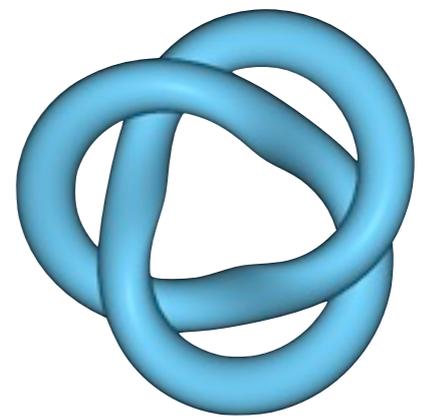


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Tx1 and Tx2 are composite transforms.

Tx3 (final output) may be a composite of Tx1 and Tx2.

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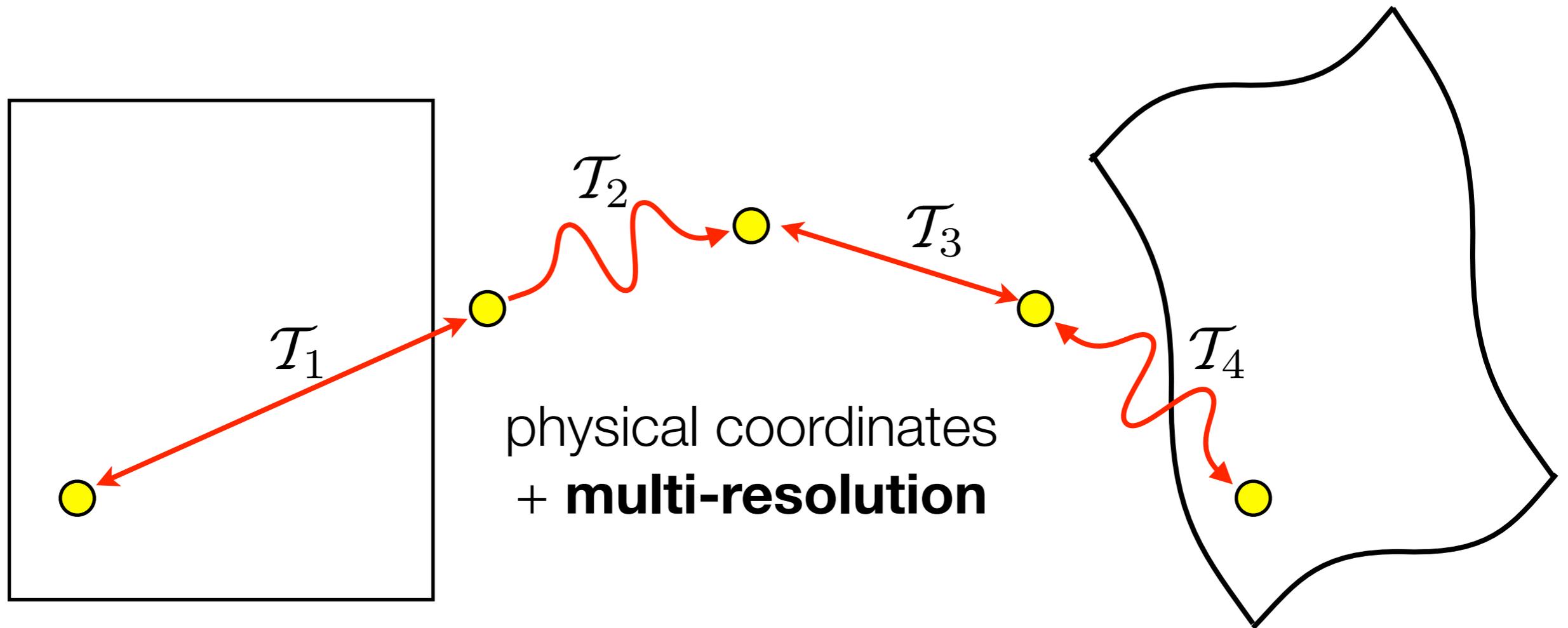


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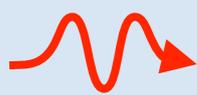
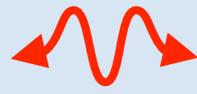
Tx3 (final output) may be a composite of Tx1 and Tx2.

# Composite transform



$$\mathcal{T} = \mathcal{T}_1 \circ \mathcal{T}_2 \circ \mathcal{T}_3 \circ \mathcal{T}_4$$

## Transformation Legend

-  linear
-  deformable
-  symmetric deformable

Accompanied by composite I/O.  
Details need to be worked out.

# Deformable transformation objects

---

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---

`./ITK/Code/Review/itkDeformationFieldTransform.h`

# Deformable transformation objects

---

`./ITK/Code/Review/itkDeformationFieldTransform.h`

`./ITK/Code/Review/  
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# Deformable transformation objects

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Both can be applied through `ResampleImageFilter`.

# Deformable transformation objects

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Both can be applied through `ResampleImageFilter`.  
Should therefore remove `WarpImageFilter`

# Deformable transformation objects

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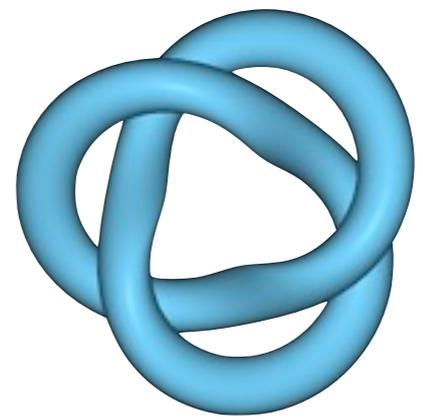
`./ITK/Code/Review/  
itkBSplineDeformationFieldTransform.h`

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This helps us unify the PDE and linear registration frameworks.

# Registration machinery code 1

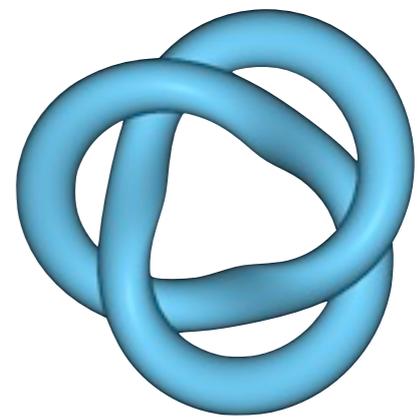
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```
typedef itk::Transform<double,ImageDimension> TransformType;
typedef itk::IdentityTransform<double,ImageDimension> IdentityTransformType;
typedef itk::CompositeTransform<double,ImageDimension> CompositeTransformType;
typedef itk::TranslationTransform<double,ImageDimension> TranslationTransformType;
typedef itk::DeformationFieldTransform<double,ImageDimension> DeformationTransformType;
typedef DeformationTransformType::DeformationFieldType FieldType;
IdentityTransformType::Pointer transformF = IdentityTransformType::New();
DeformationTransformType::Pointer transformM1 = DeformationTransformType::New();
TranslationTransformType::Pointer transformM2 = TranslationTransformType::New();
TranslationTransformType::Pointer transformM3 = TranslationTransformType::New();
CompositeTransformType::Pointer transformM = CompositeTransformType::New();
```

# Registration machinery code 2

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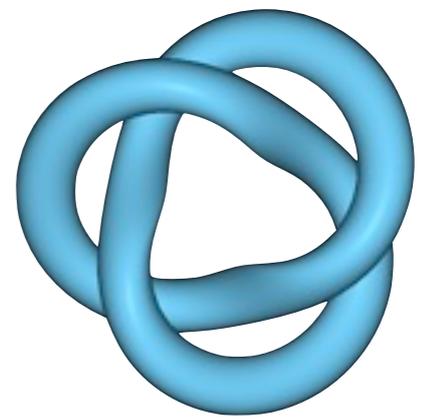
```
typedef itk::DemonsImageToImageMetric<ImageType, ImageType> ObjectMetricType;
ObjectMetricType::Pointer objectMetric = ObjectMetricType::New();
```

```
/** Set up the virtual reference space */
```

```
objectMetric->SetVirtualDomainSpacing(fixed_image->GetSpacing());
objectMetric->SetVirtualDomainSize(fixed_image->GetLargestPossibleRegion());
objectMetric->SetVirtualDomainOrigin(fixed_image->GetOrigin());
objectMetric->SetVirtualDomainDirection(fixed_image->GetDirection());
```

# Registration machinery code 3

---



```
transformM1->SetDeformationField(field);  
transformM1->SetInverseDeformationField(field);
```

```
transformM->AddTransform(transformM1);  
transformM->AddTransform(transformM2);
```

```
/** Define the input images and their transforms */
```

```
objectMetric->SetFixedImage(fixed_image);  
objectMetric->SetMovingImage(moving_image);  
objectMetric->SetFixedImageTransform(transformF);  
objectMetric->SetMovingImageTransform(transformM);
```

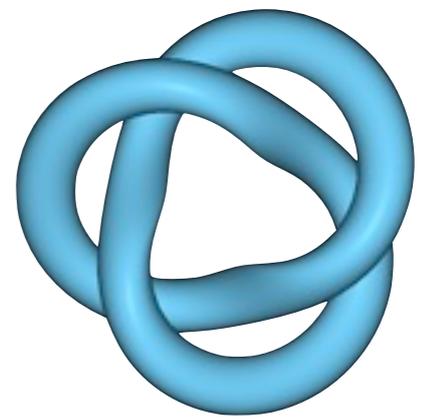
```
/** Compute one iteration of the metric */
```

```
objectMetric->ComputeMetricAndDerivative();
```

---

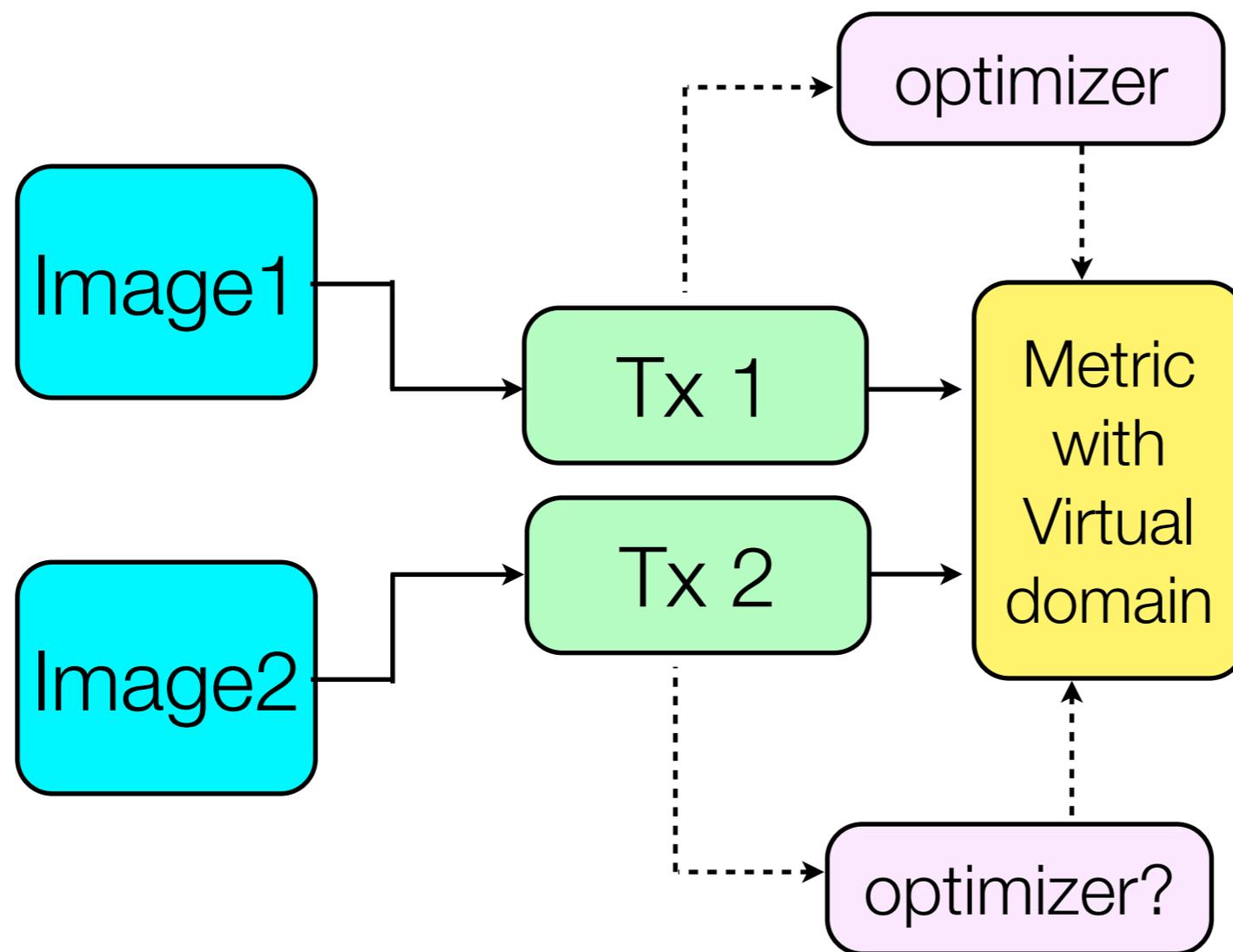
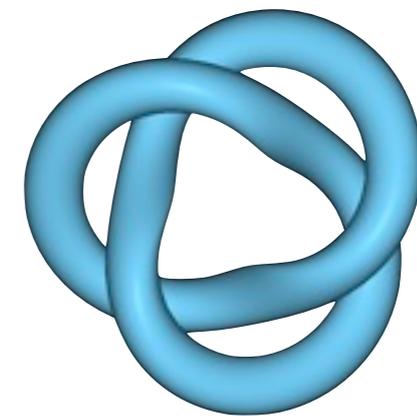
# Object to object metric code

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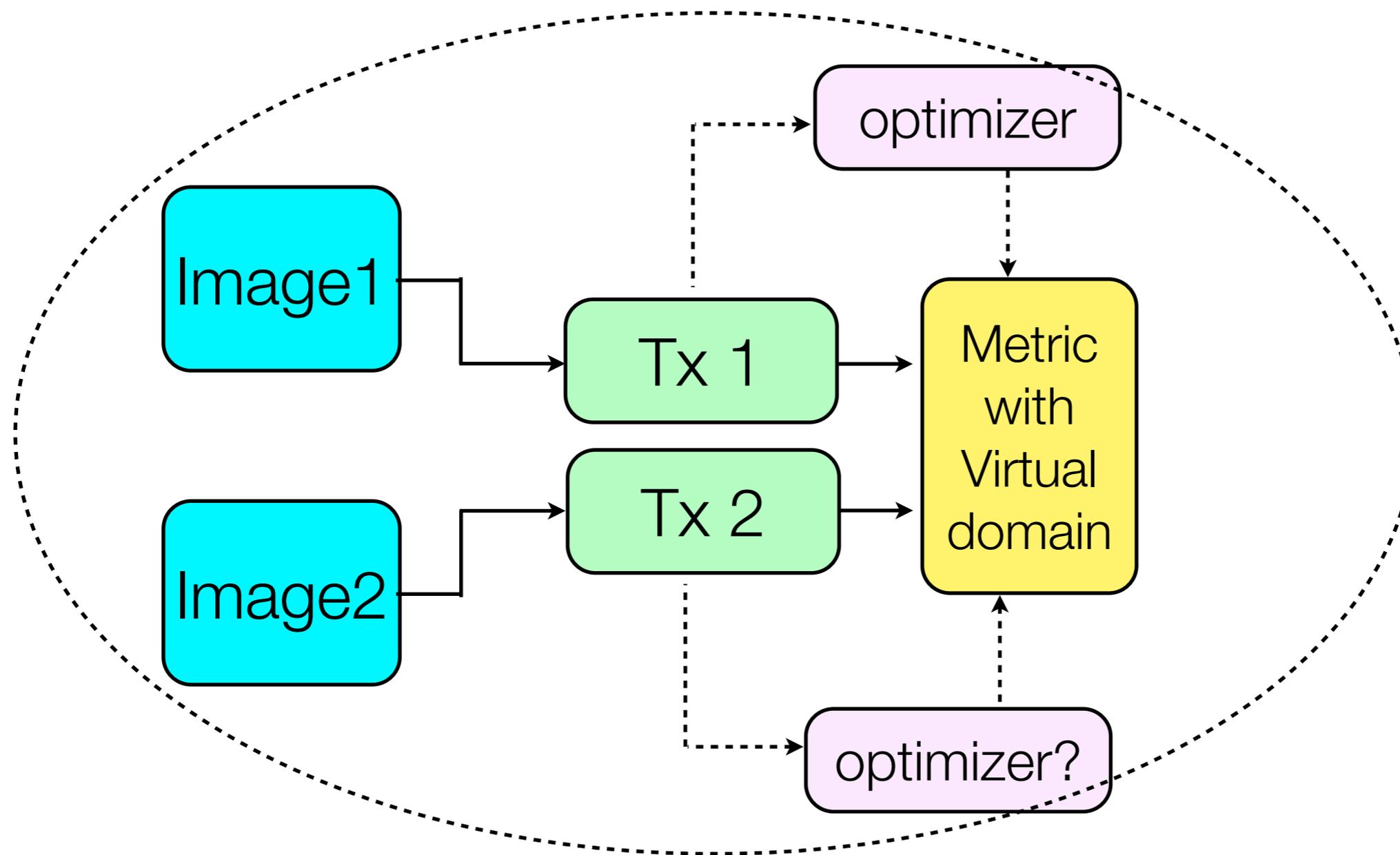
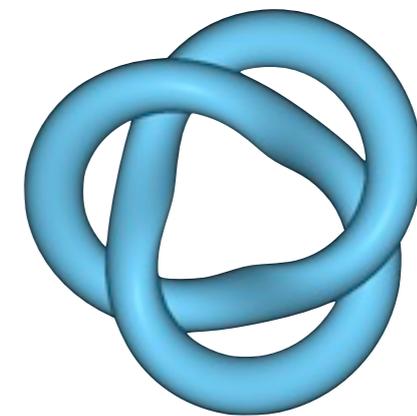


```
this->m_VirtualImage->TransformIndexToPhysicalPoint(ItV.GetIndex(),mappedPoint);  
  
// Use generic transform to compute mapped position  
mappedFixedPoint = this->m_FixedImageTransform->TransformPoint(mappedPoint);  
mappedMovingPoint = this->m_MovingImageTransform->TransformPoint(mappedPoint);  
if ( !this->m_FixedInterpolator->IsInsideBuffer(mappedFixedPoint) ||  
      !this->m_MovingInterpolator->IsInsideBuffer(mappedMovingPoint) )  
    sampleOk=false;  
if ( sampleOk )  
{  
    double metricval=this->ComputeLocalContributionToMetricAndDerivative(mappedFixedPoint,m
```

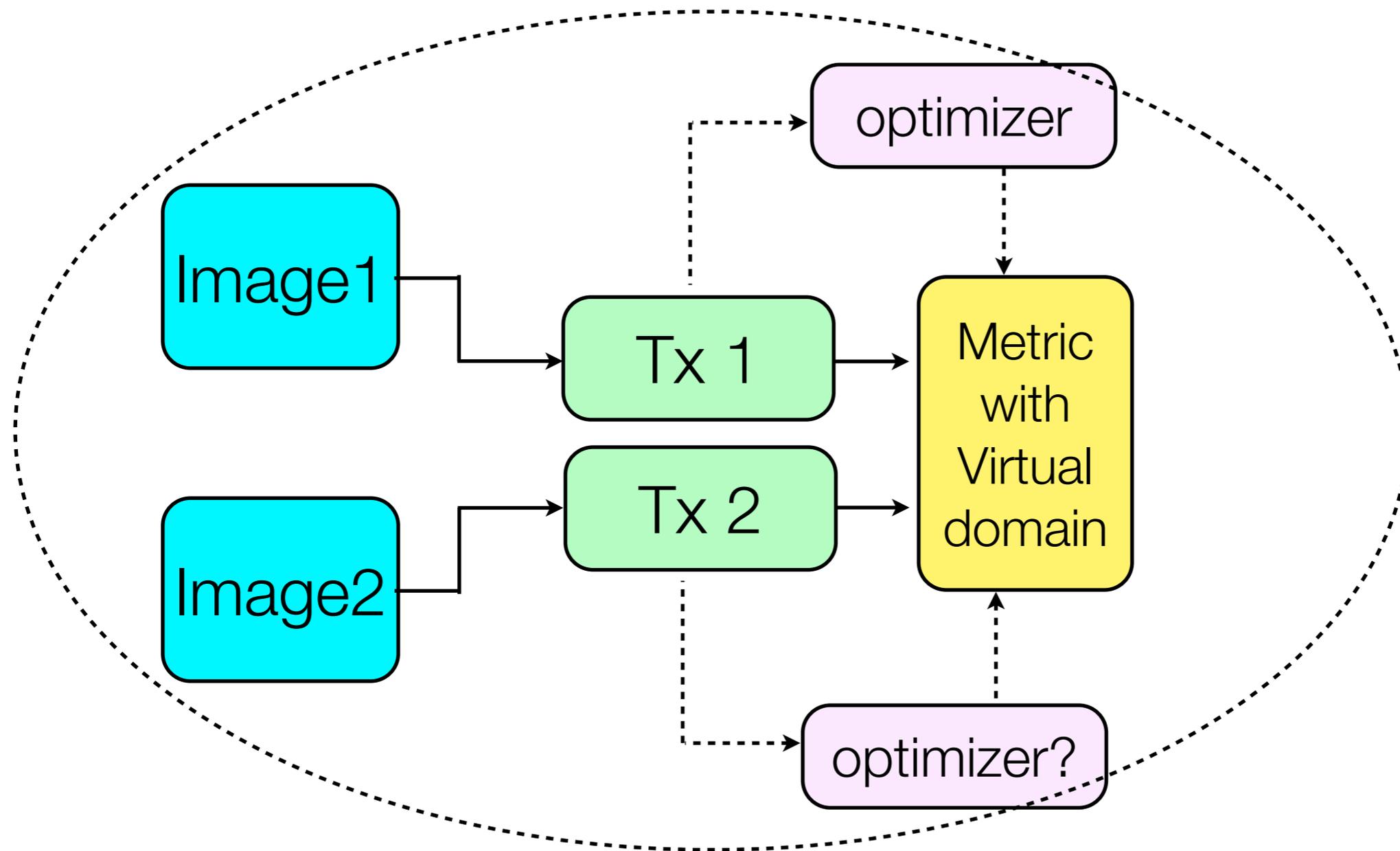
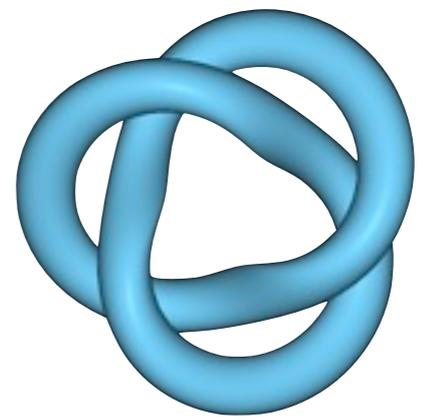
# Automated parameter setting



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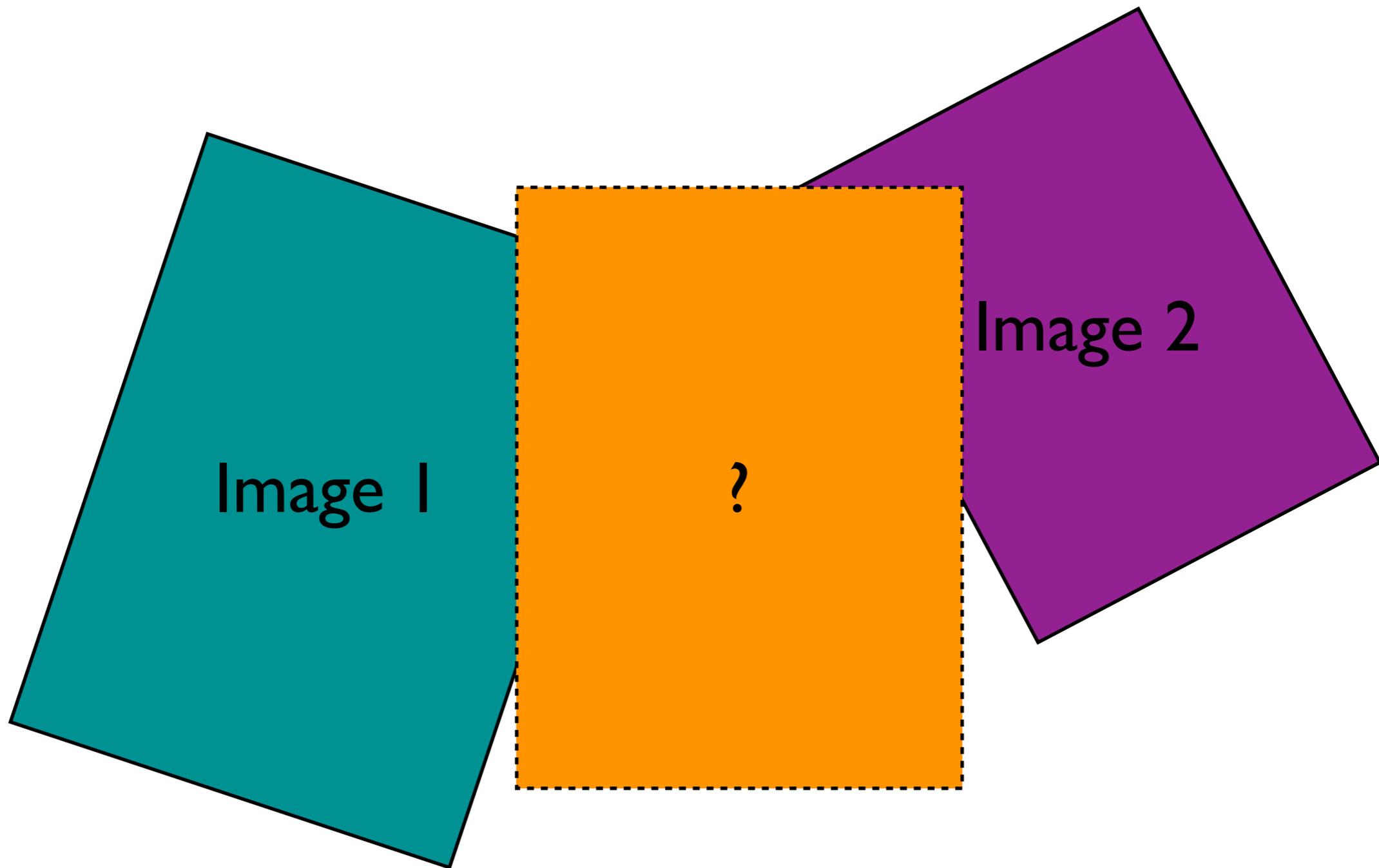
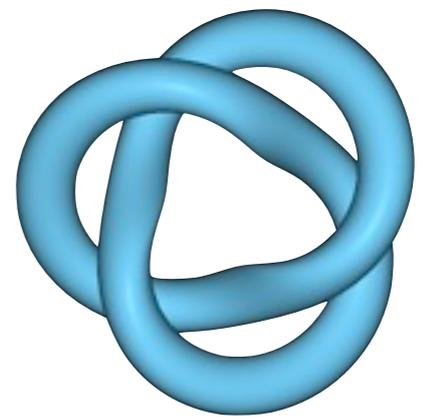
# Automated parameter setting



Takes the registration machinery object as input and sets the optimizer parameters according to a TBD algorithm.

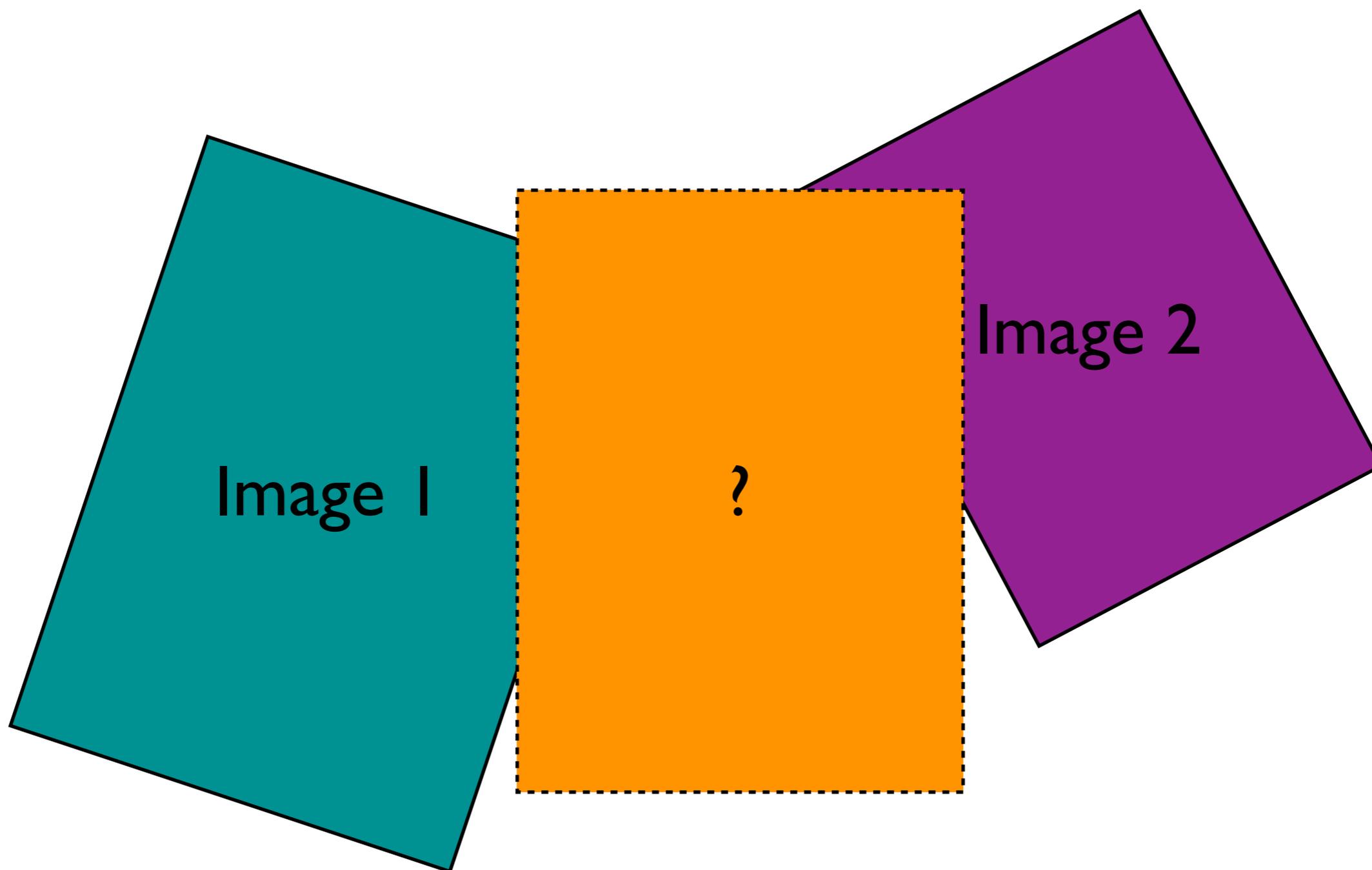
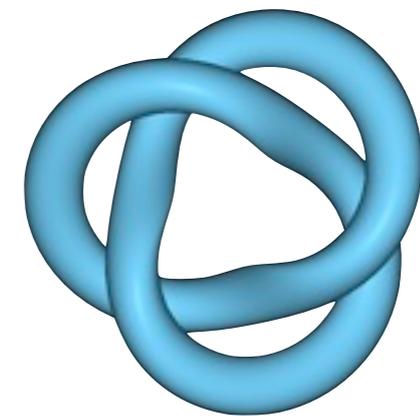
# Virtual space initializer

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# Virtual space initializer

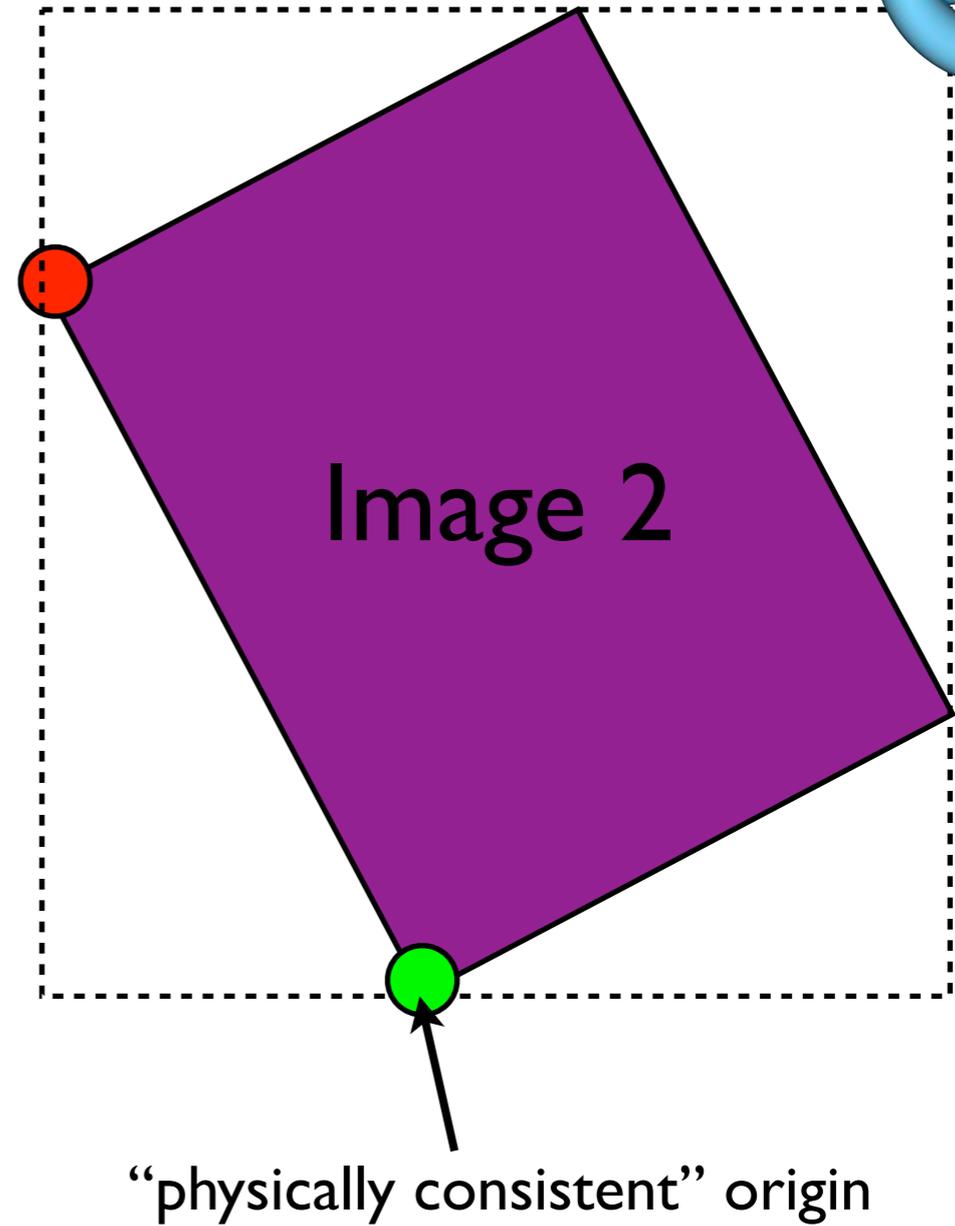
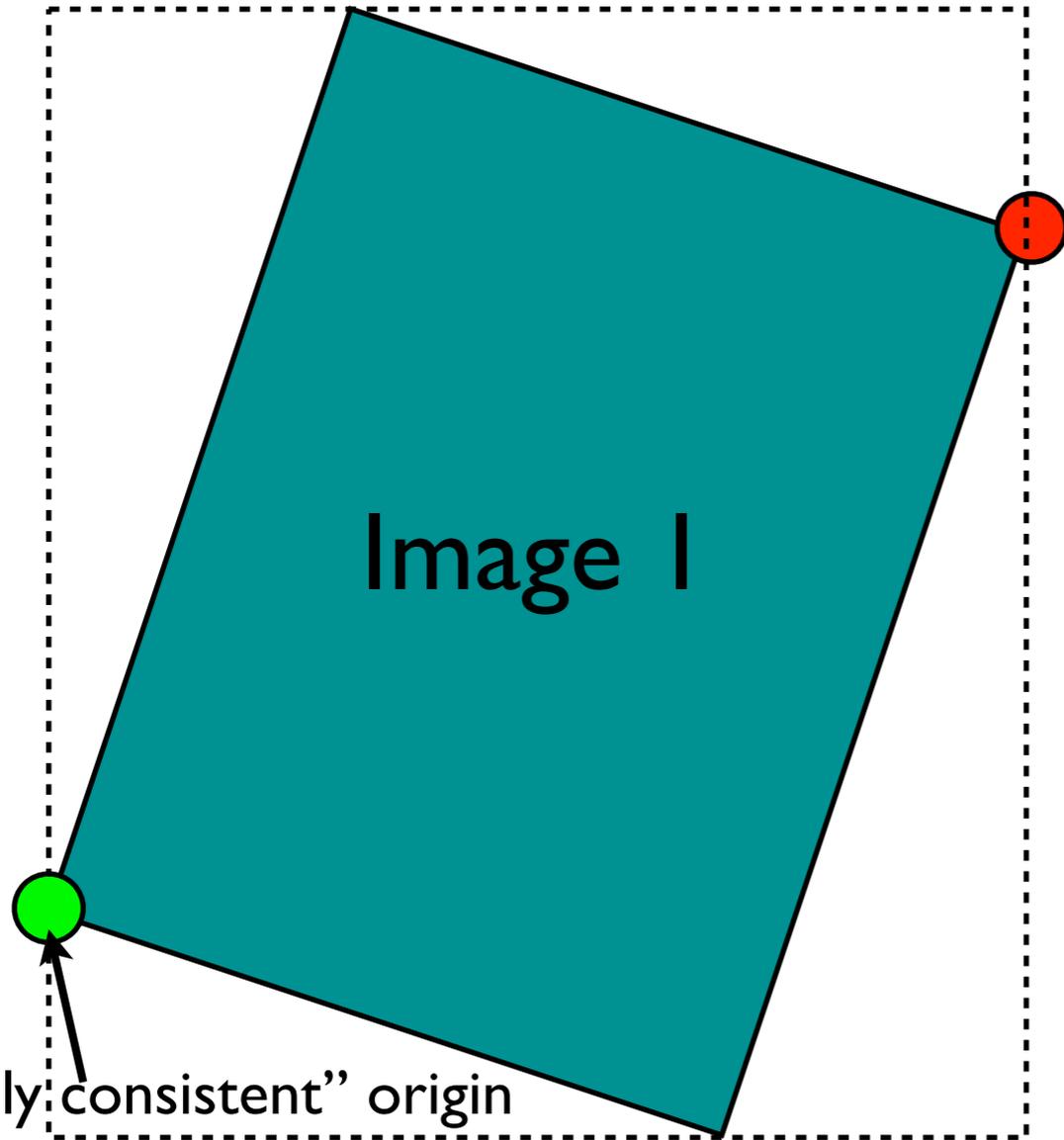
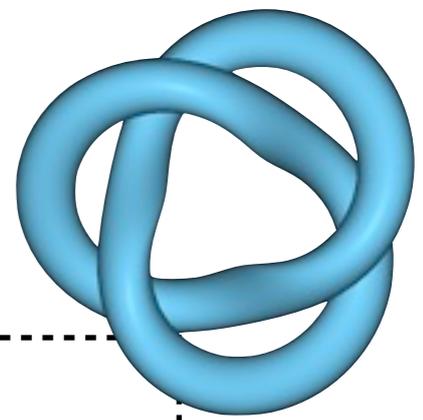
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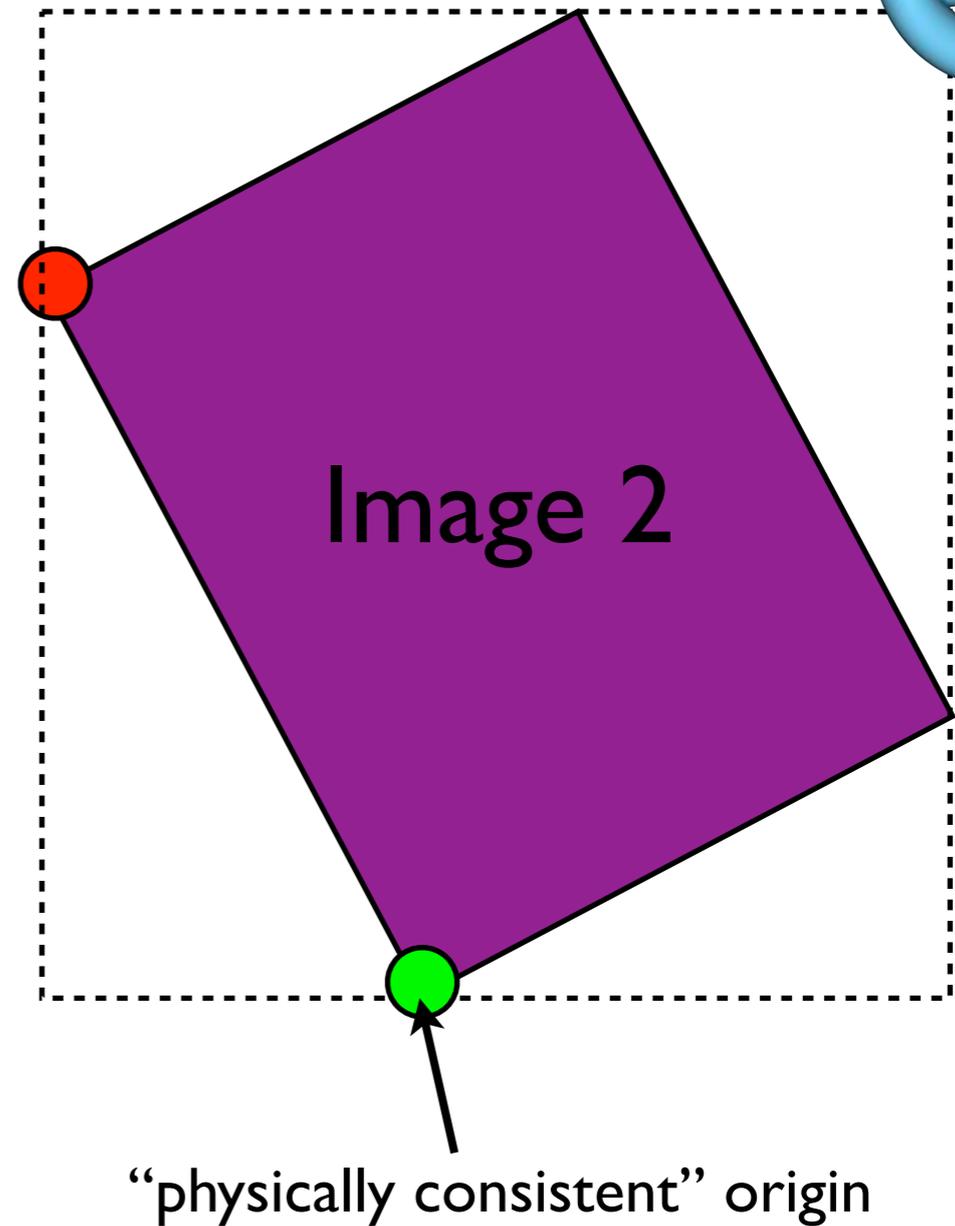
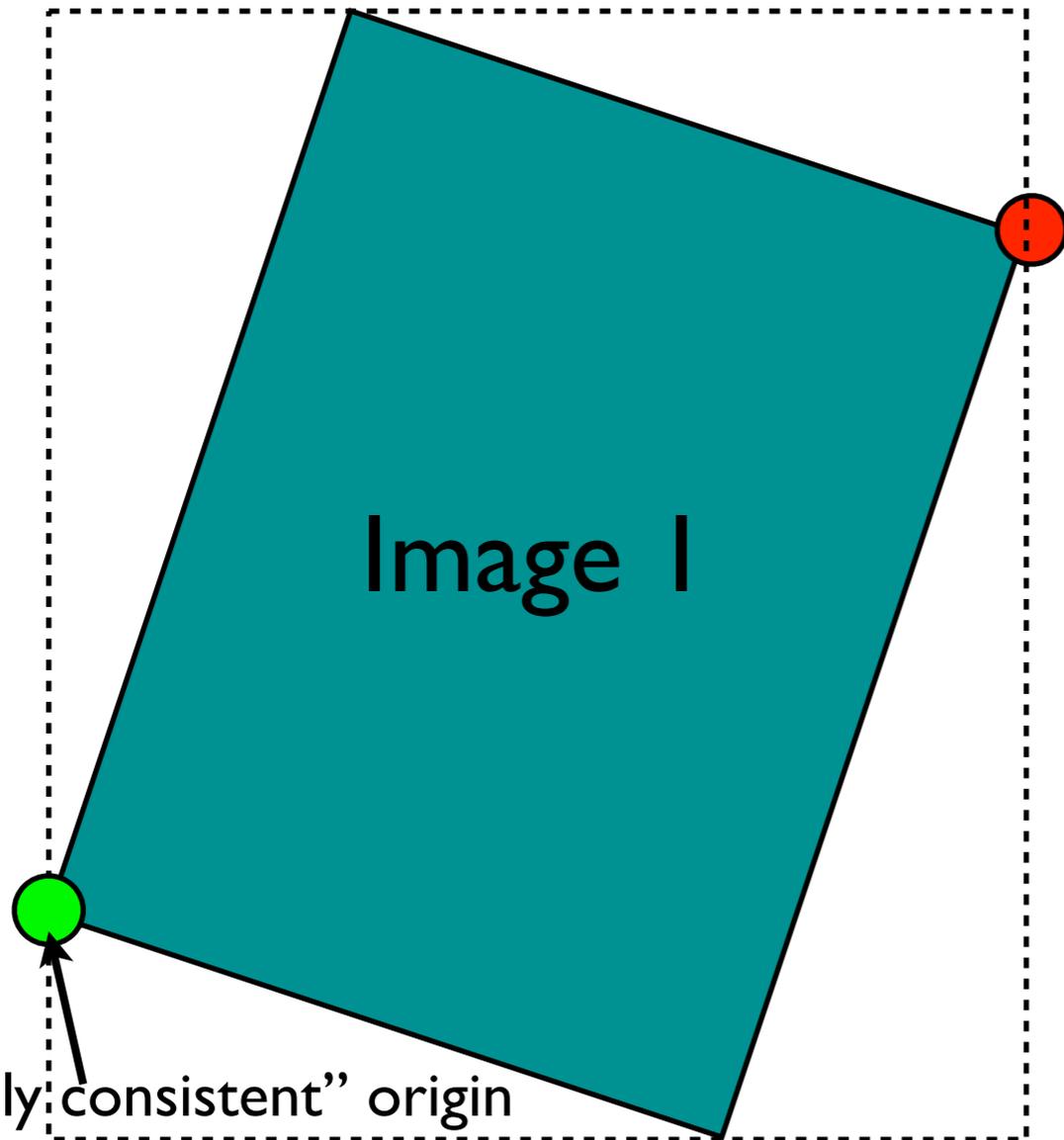
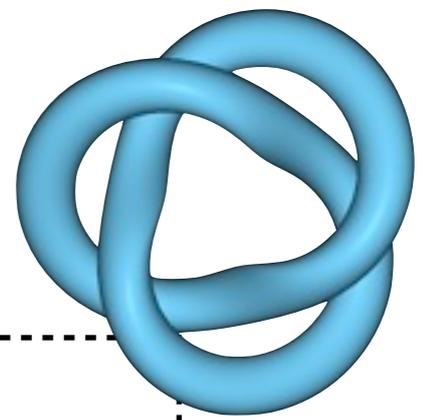
what is the best “average domain”?

# Virtual space initializer

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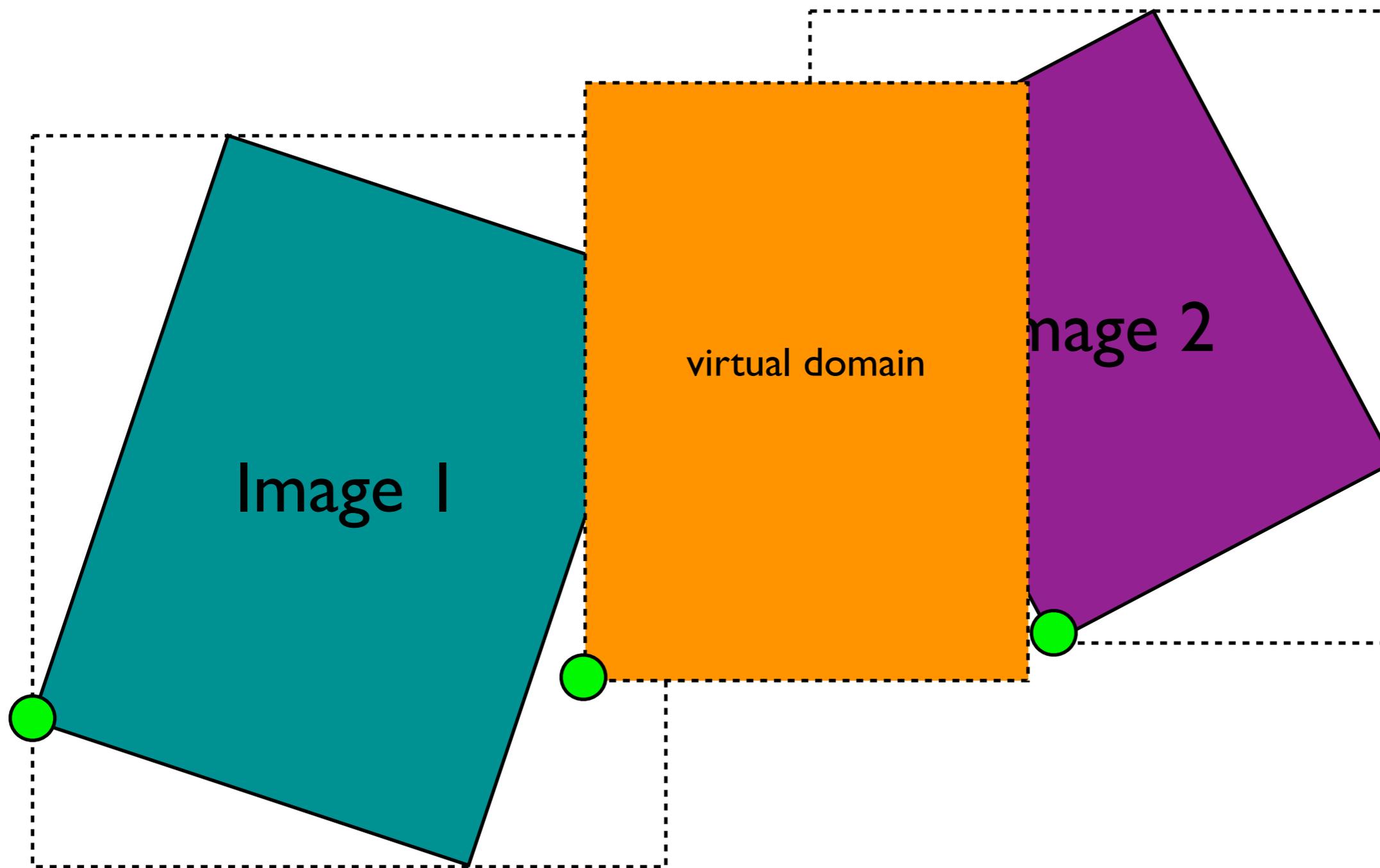
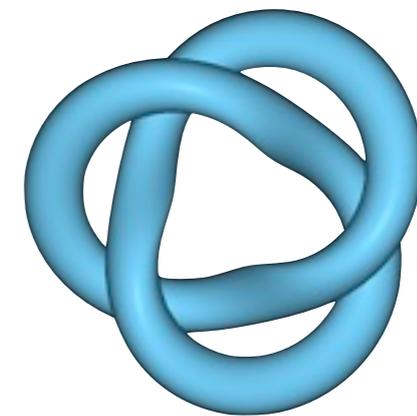
# Virtual space initializer



what is the best “average domain”?

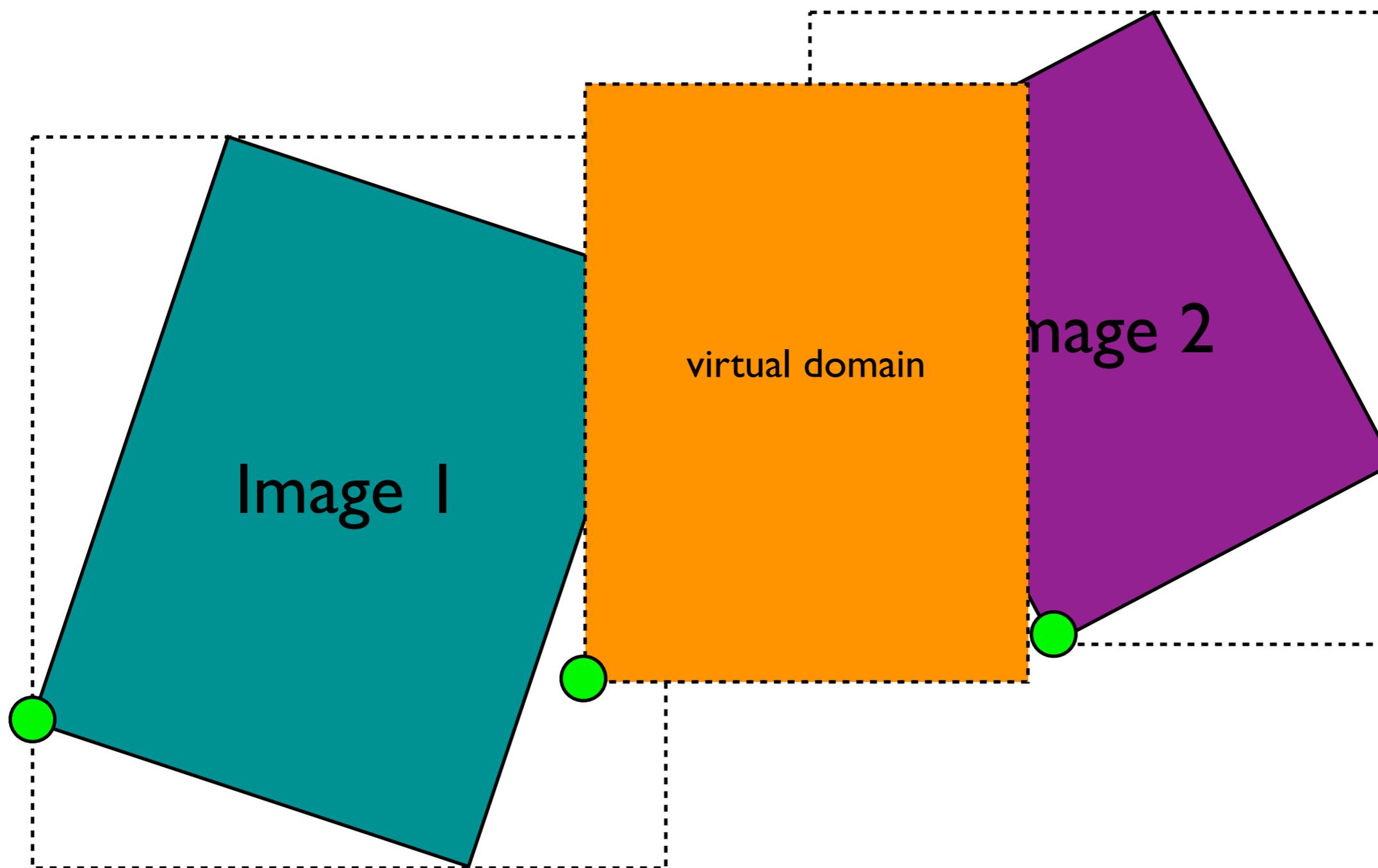
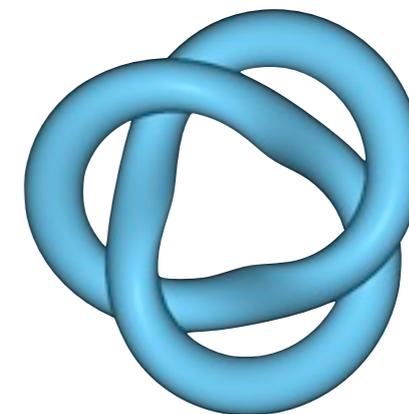
# Virtual space initializer

---



# Virtual space initializer

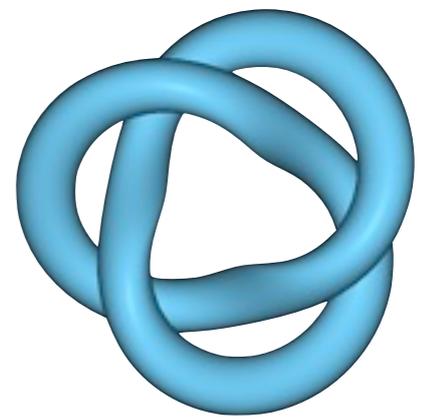
---



what is the best “average domain”?

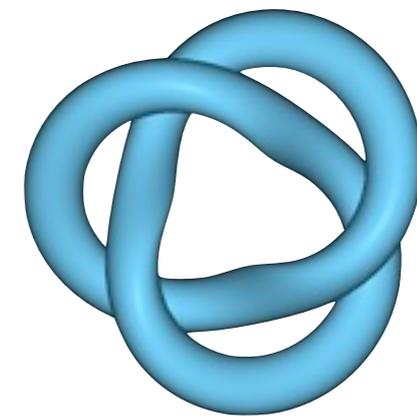
# Changes to transform + metric

---



# Changes to transform + metric

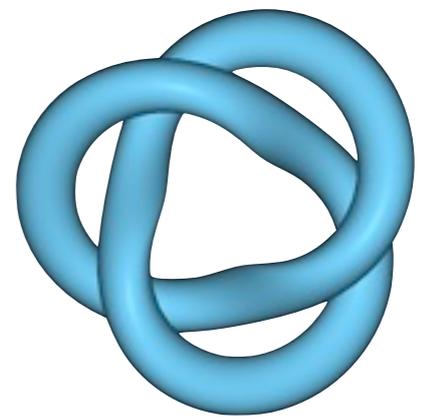
---



GetLocalJacobian

# Changes to transform + metric

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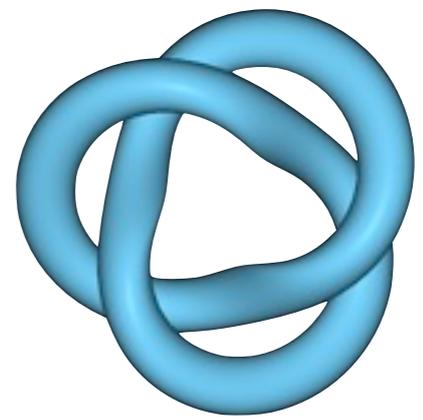


GetLocalJacobian

GetLocalContributionToMetricAndDerivative

# Changes to transform + metric

---



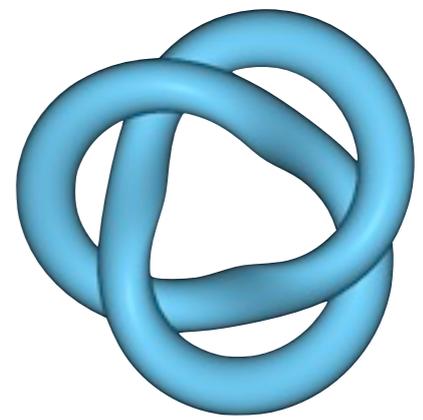
GetLocalJacobian

GetLocalContributionToMetricAndDerivative

Revised framework supports dense metric computation with or without use of Jacobian

# Changes to transform + metric

---



GetLocalJacobian

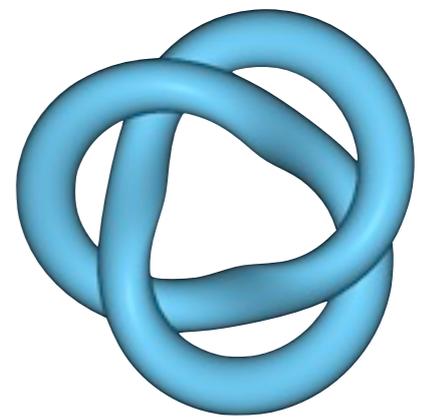
GetLocalContributionToMetricAndDerivative

Revised framework supports dense metric computation with or without use of Jacobian

Critical for efficient deformable registration

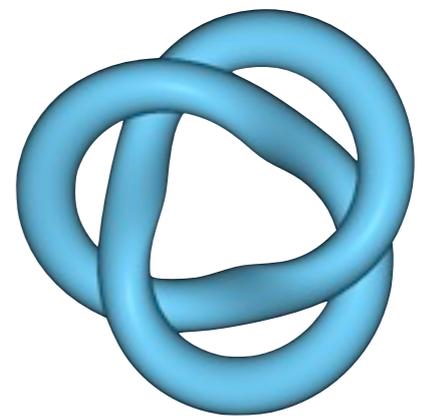
# Neighborhood correlation metric

---



# Neighborhood correlation metric

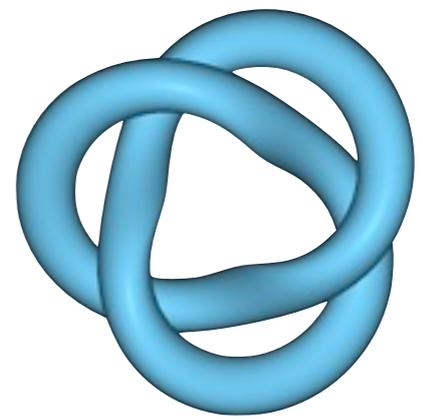
---



Sliding window implementation of both metric and derivative.

# Neighborhood correlation metric

---

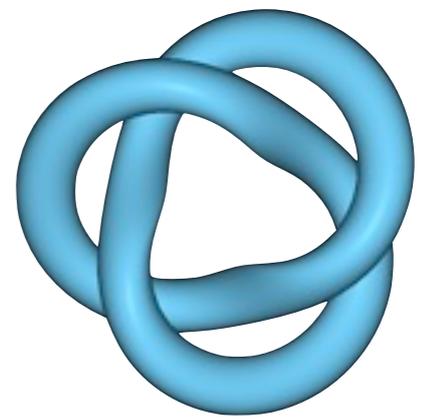


Sliding window implementation of both metric and derivative.

Users sets the window radius.

# Neighborhood correlation metric

---



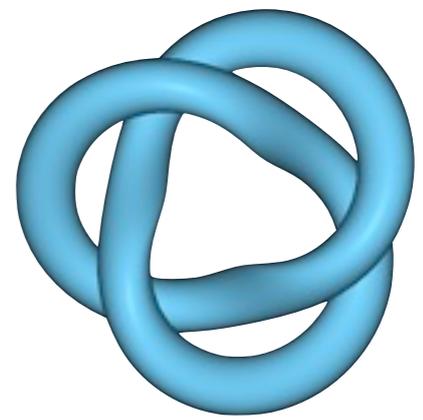
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Multi-threaded. MI, MSQ, Global CC goals. NMI?

# Neighborhood correlation metric

---



Sliding window implementation of both metric and derivative.

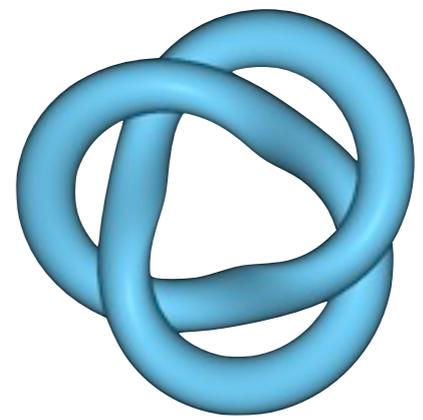
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Multi-threaded. MI, MSQ, Global CC goals. NMI?

Is currently on Github.

# Neighborhood correlation metric

---



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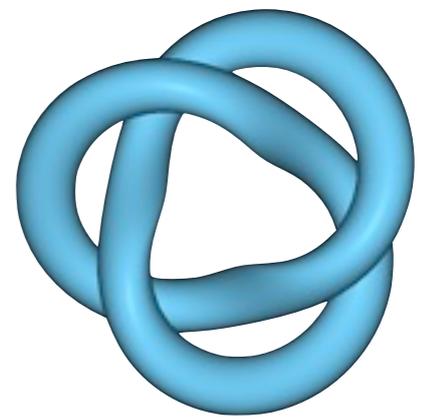
Users sets the window radius.

Multi-threaded. MI, MSQ, Global CC goals. NMI?

Is currently on Github.

Independent metric development needs to be unified.

# Transducer function (@ github)

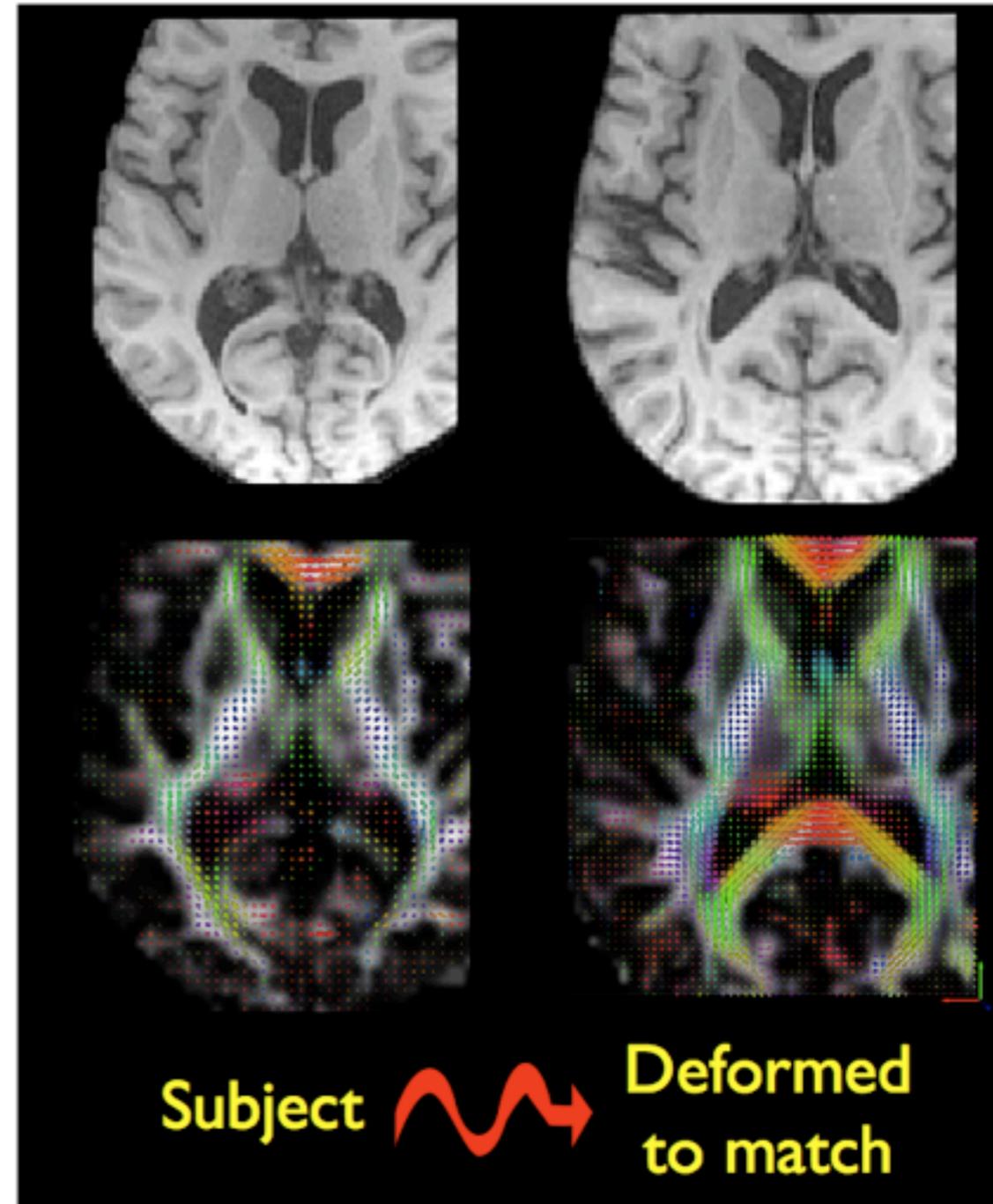


$$E(\phi, \mathbf{I}, \mathbf{J}) = \sum_i \lambda_i S_i(\phi, I_i, J_i)$$
$$\phi \in Diff_0$$

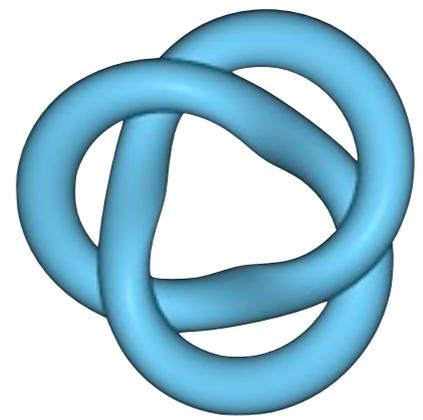
$$S_i \in \{ MI, CC, \|\cdot\|^2,$$

$$PSE, \|\cdot\|_{Dev}, JTB \}$$

$$\phi T = (D\phi)T(\phi)$$



# Transducer function (@ github)



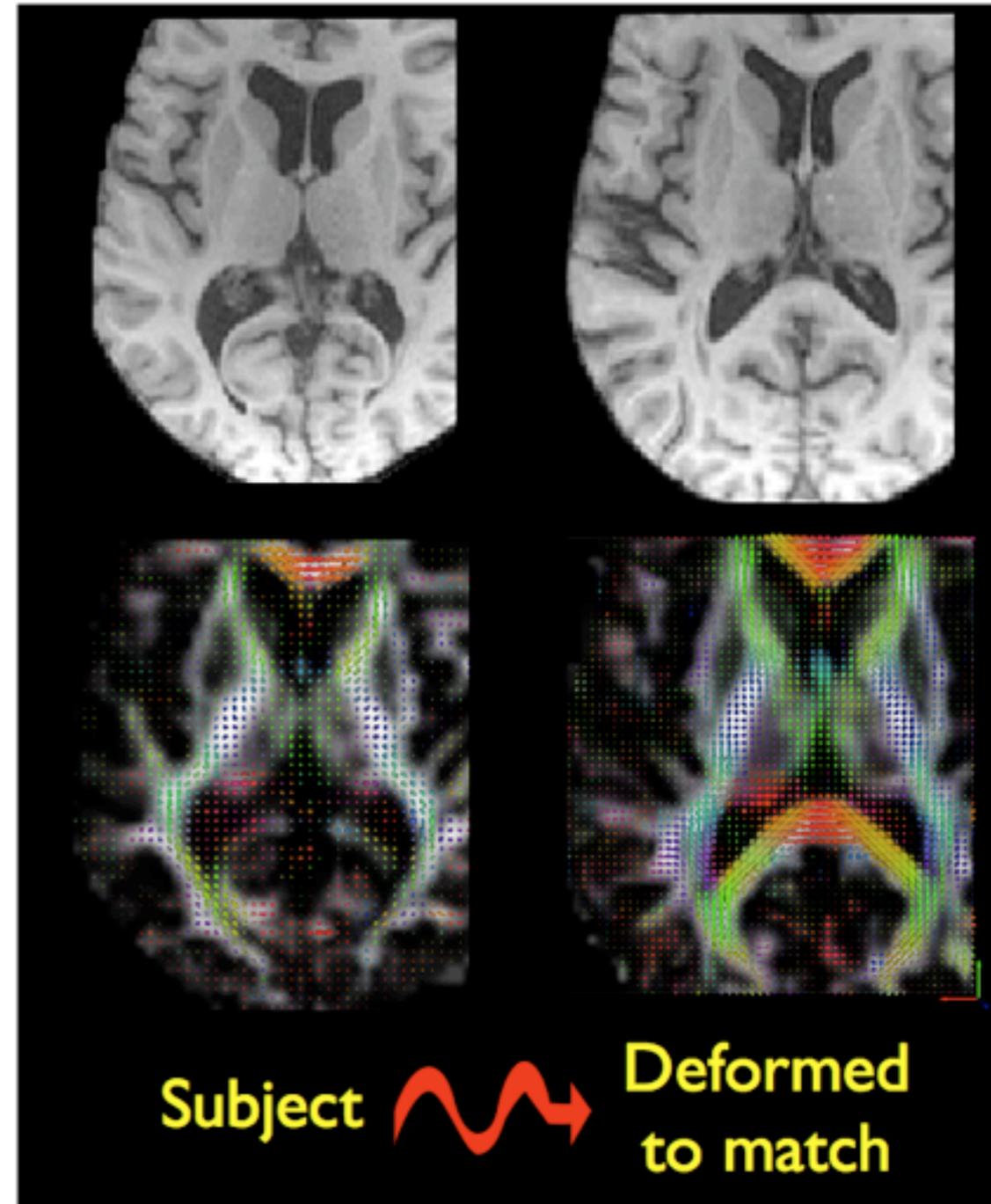
Add to the resample image filter.

$$E(\phi, \mathbf{I}, \mathbf{J}) = \sum_i \lambda_i S_i(\phi, I_i, J_i)$$
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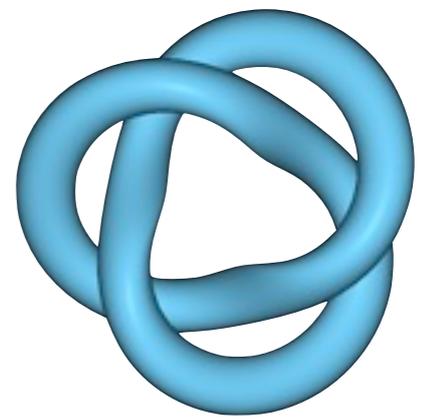
$$S_i \in \{ MI, CC, \|\cdot\|^2,$$

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$$\phi T = (D\phi)T(\phi)$$



# Transducer function (@ github)



Add to the resample image filter.

Need to make efficient for the case when

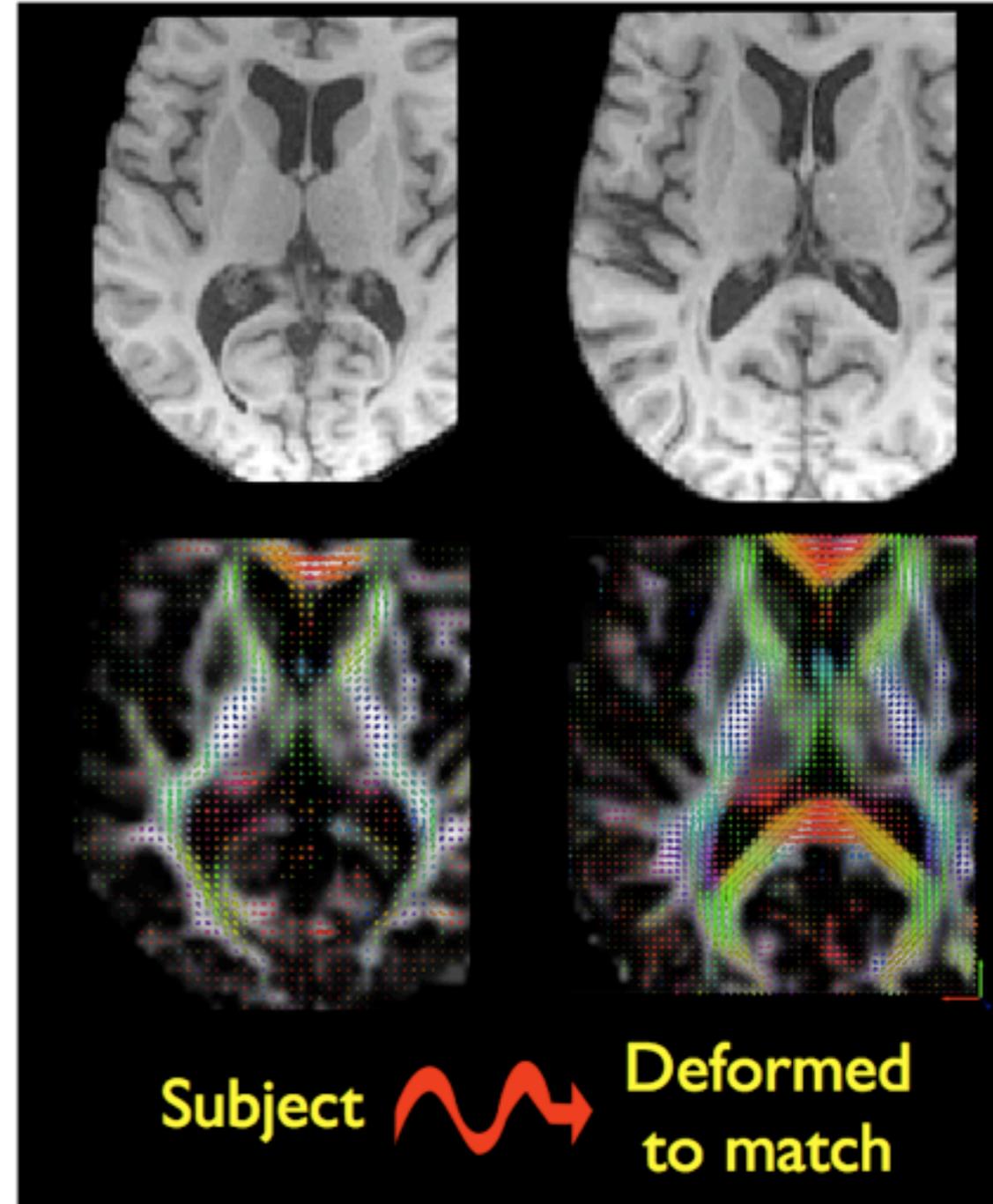
Transducer=Identity

$$E(\phi, \mathbf{I}, \mathbf{J}) = \sum_i \lambda_i S_i(\phi, I_i, J_i)$$
$$\phi \in Diff_0$$

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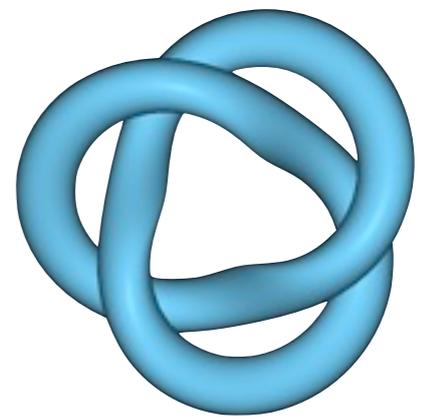
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# B-splines in the Insight Toolkit

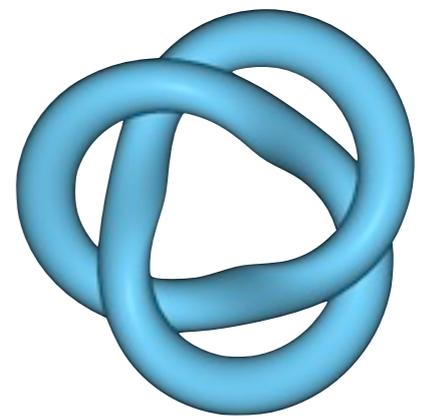
---



# B-splines in the Insight Toolkit

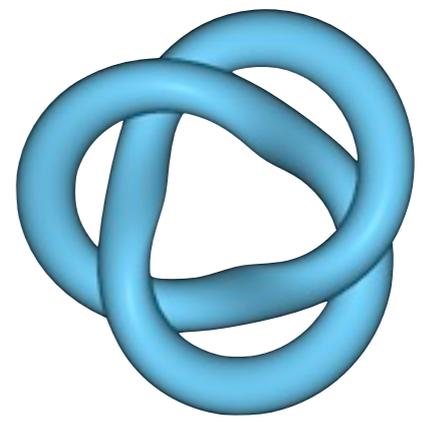
---

A couple classes to discuss:



# B-splines in the Insight Toolkit

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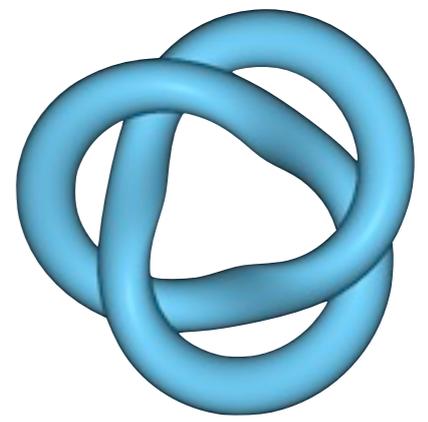


A couple classes to discuss:

- BSplineScatteredData

# B-splines in the Insight Toolkit

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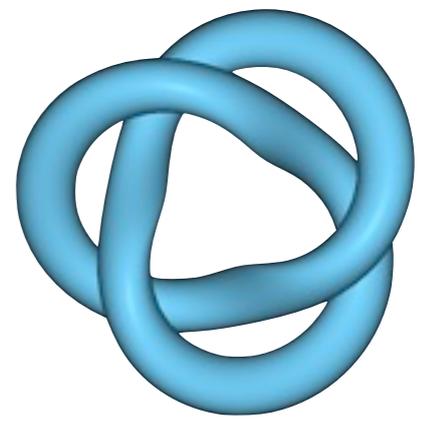


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  - nick cleverly sped this up

# B-splines in the Insight Toolkit

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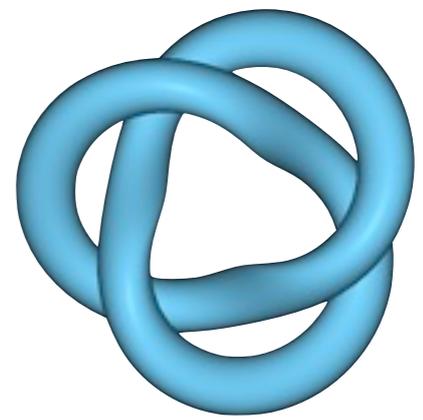


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# B-splines in the Insight Toolkit

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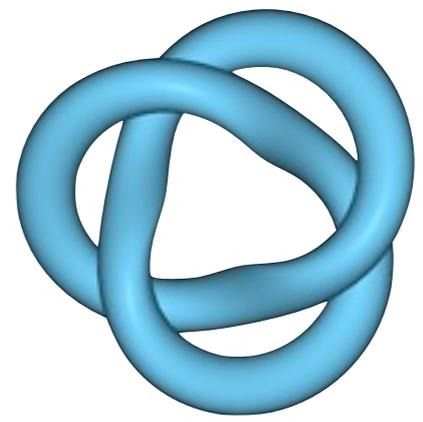


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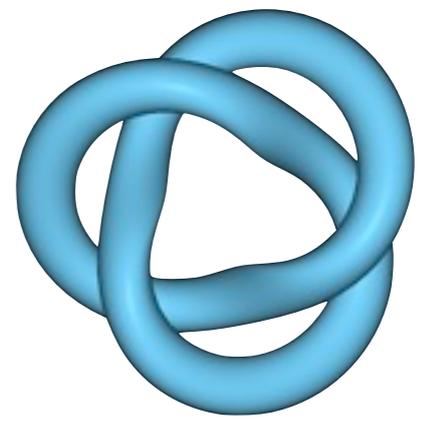


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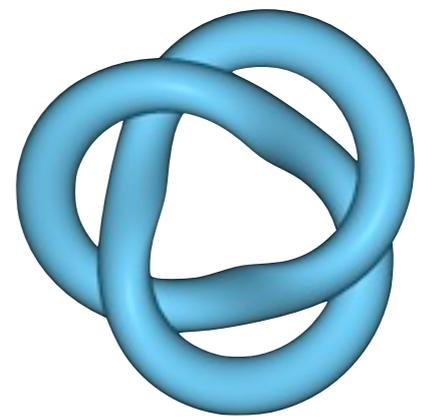


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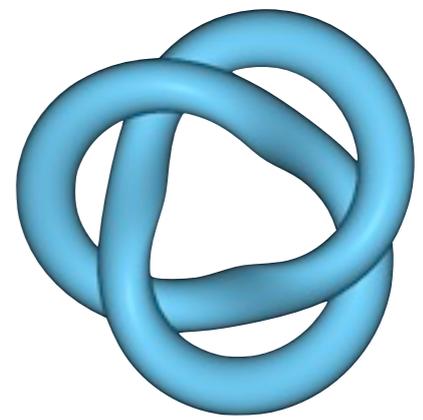


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  - redefining how users sets b-spline grid in a more intuitive way

# B-splines in the Insight Toolkit

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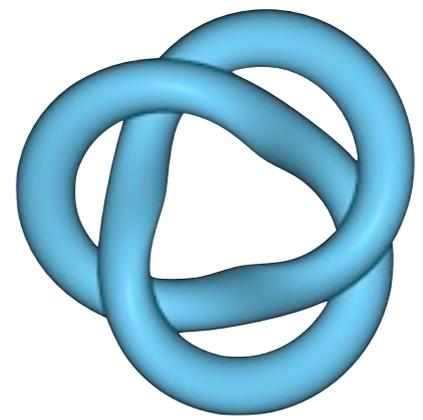


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# B-splines in the Insight Toolkit

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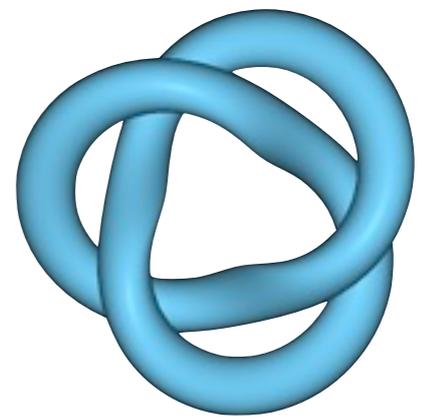


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- BSplineTransformInitializer (rename this)

# B-splines in the Insight Toolkit

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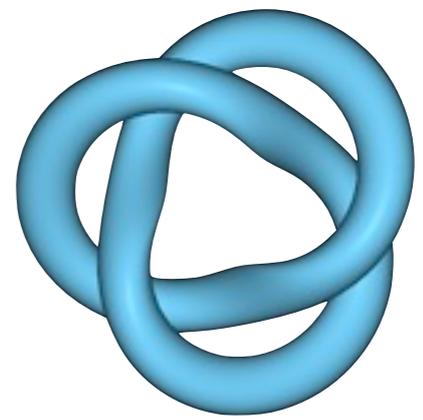


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  - fixed bug in domain definition

# B-splines in the Insight Toolkit

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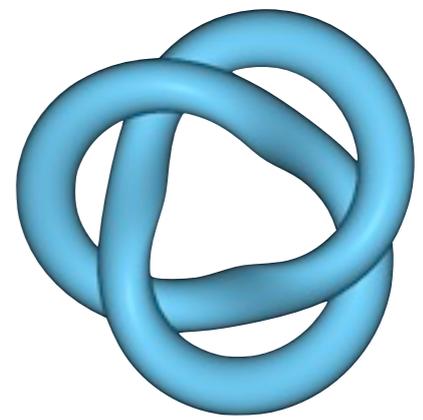


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  - nick generalized the initialization to N-dimensions

# B-splines in the Insight Toolkit

---

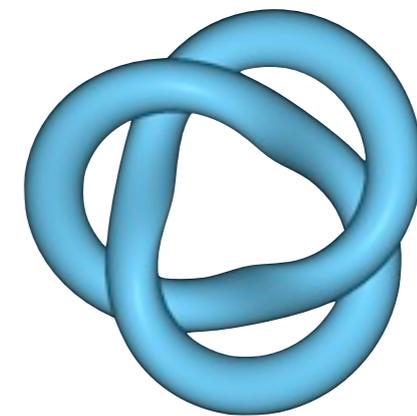


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  - redefining how users sets b-spline grid in a more intuitive way
- BSplineDeformationFieldTransform or BSplineDenseDeformationFieldTransform
- BSplineTransformInitializer (rename this)
  - fixed bug in domain definition
  - nick generalized the initialization to N-dimensions
- Rename these transforms?

# B-spline transform domain

---

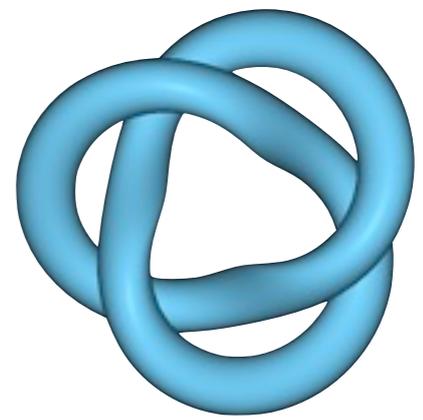


itkBSplineDeformableTransform (lines 179-187)

```
// Set the valid region
// If the grid spans the interval [start, last].
// The valid interval for evaluation is [start+offset, last-offset]
// when spline order is even.
// The valid interval for evaluation is [start+offset, last-offset)
// when spline order is odd.
// Where offset = floor(spline / 2 ).
// Note that the last pixel is not included in the valid region
// with odd spline orders.
```

# B-spline transform domain

---



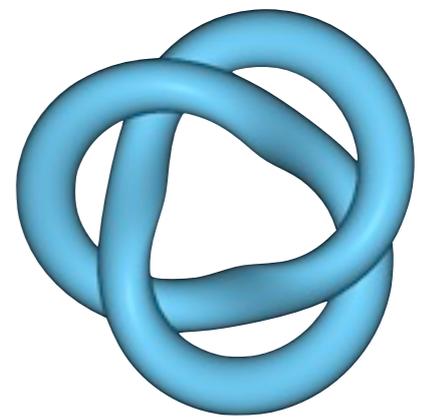
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// Note that the last pixel is not included in the valid region
// with odd spline orders.
```

This is slightly different from what I understand about B-spline domains.

# Single element domains with c.p. grid

---



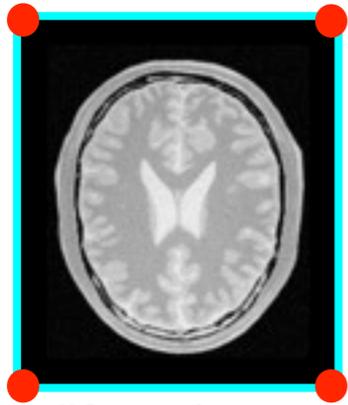
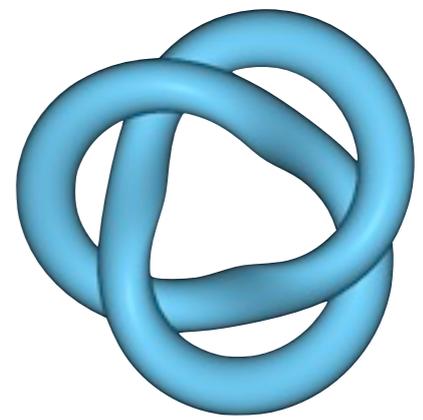
$C^0$  splines  
SplineOrder = 1

$C^1$  splines  
SplineOrder = 2

$C^2$  splines  
SplineOrder = 3

# Single element domains with c.p. grid

---



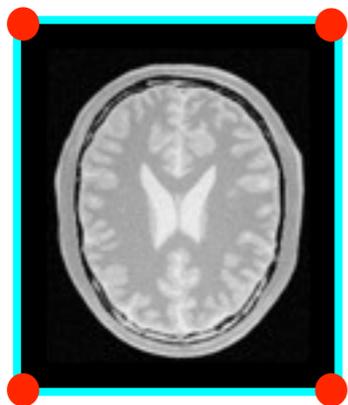
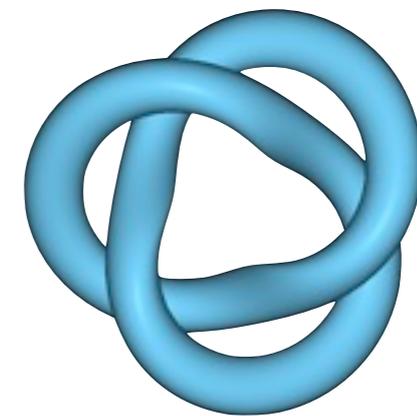
$C^0$  splines  
SplineOrder = 1

$C^1$  splines  
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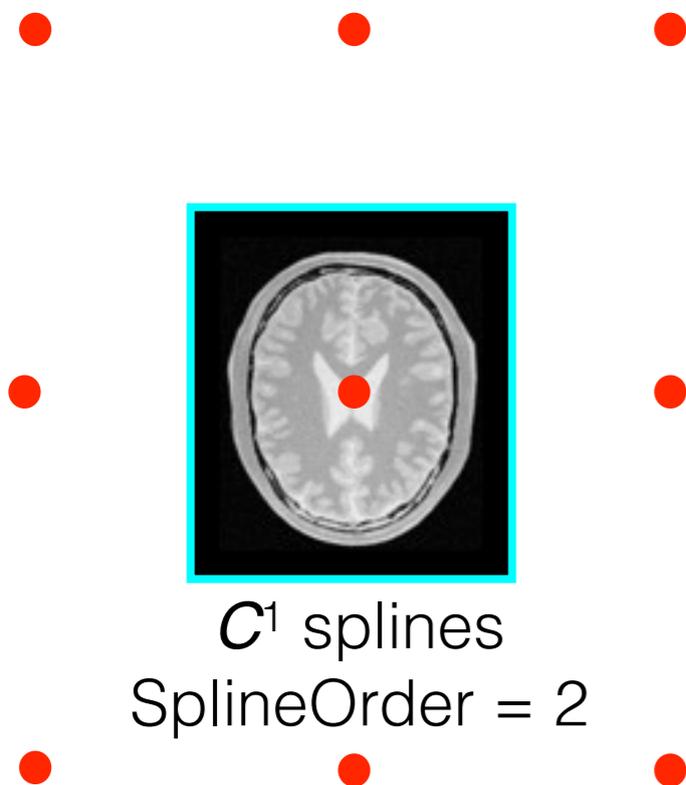
$C^2$  splines  
SplineOrder = 3

# Single element domains with c.p. grid

---



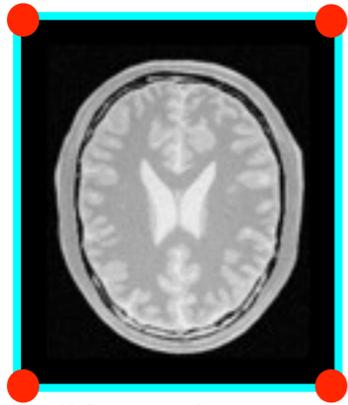
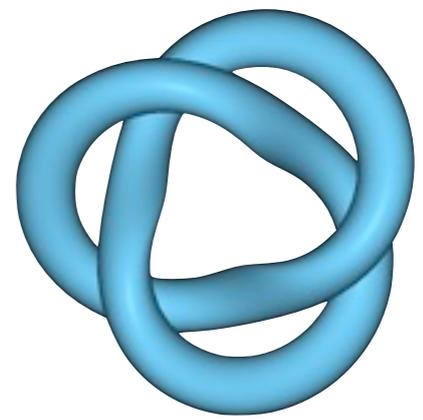
$C^0$  splines  
SplineOrder = 1



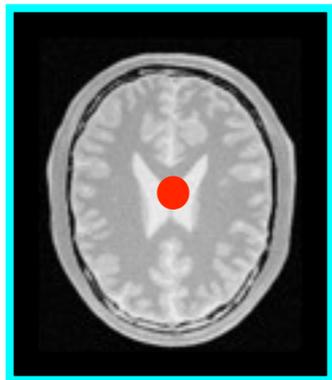
$C^1$  splines  
SplineOrder = 2

$C^2$  splines  
SplineOrder = 3

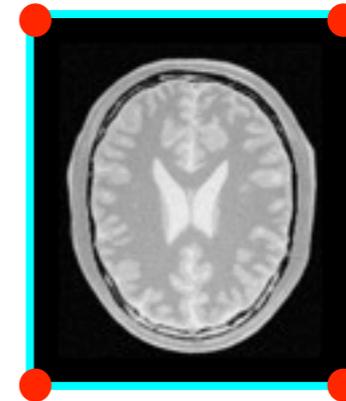
# Single element domains with c.p. grid



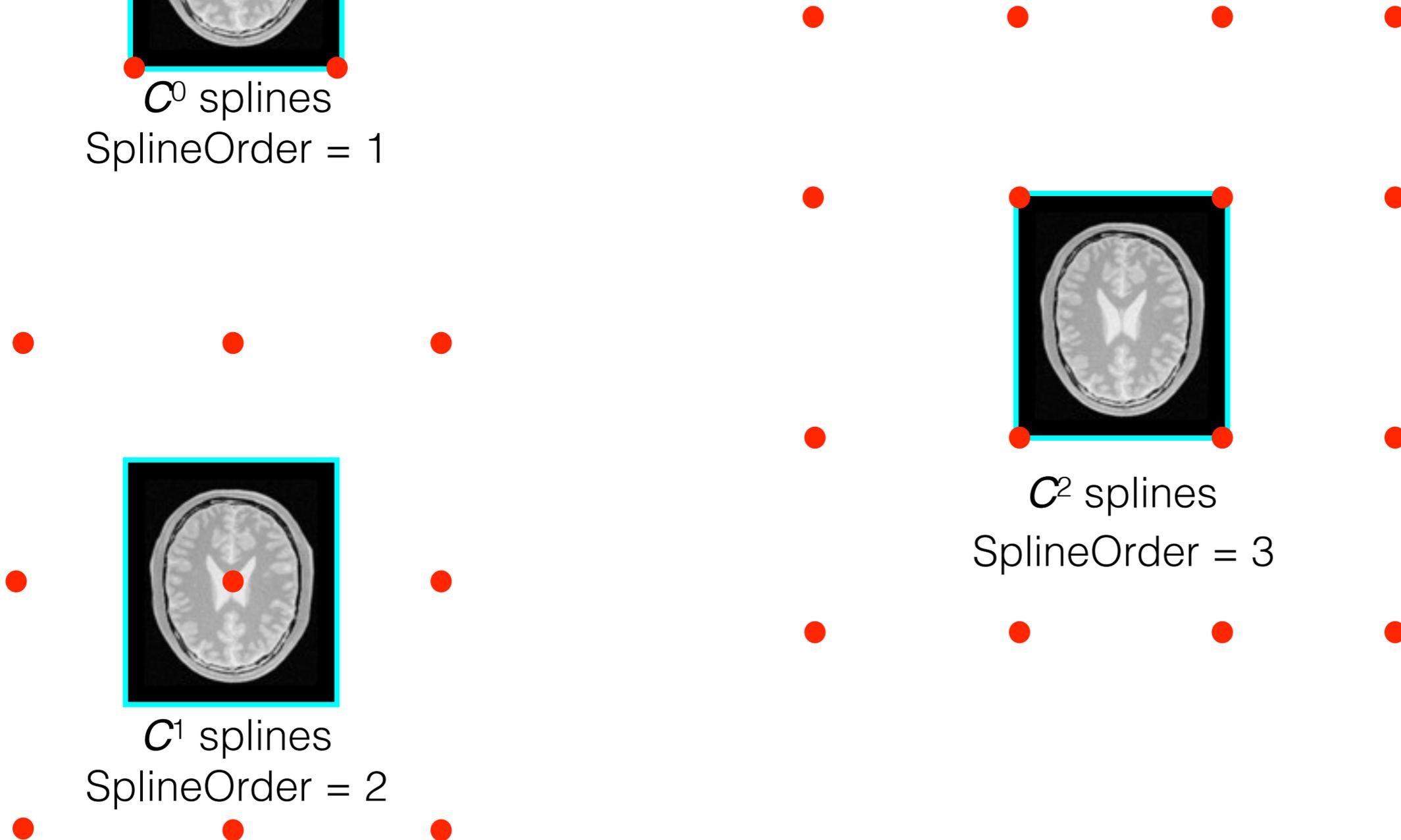
$C^0$  splines  
SplineOrder = 1



$C^1$  splines  
SplineOrder = 2

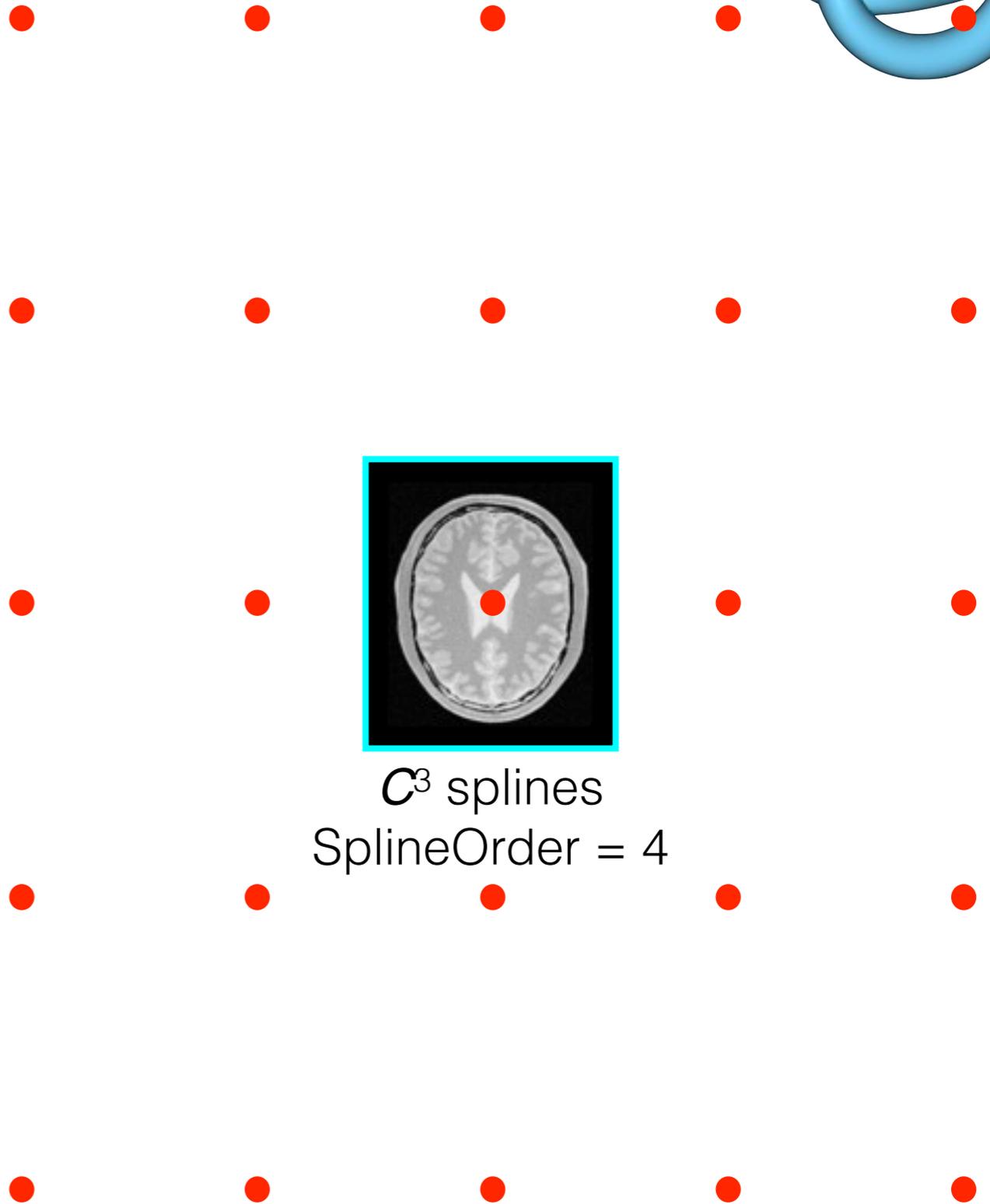
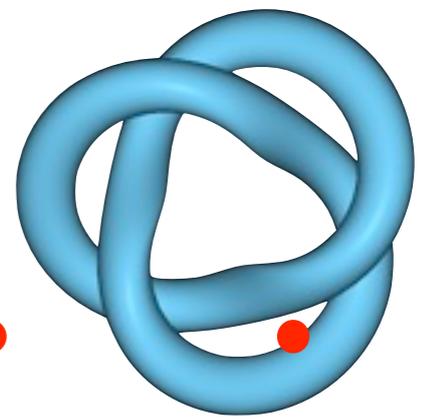


$C^2$  splines  
SplineOrder = 3



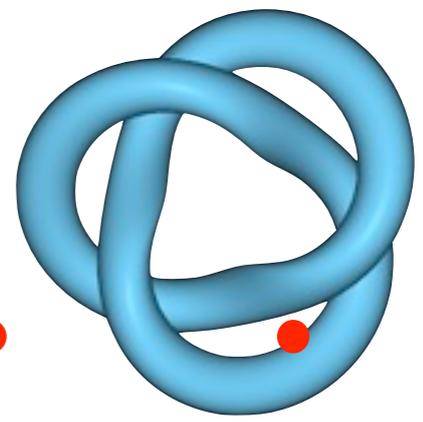
# Domain summary

---

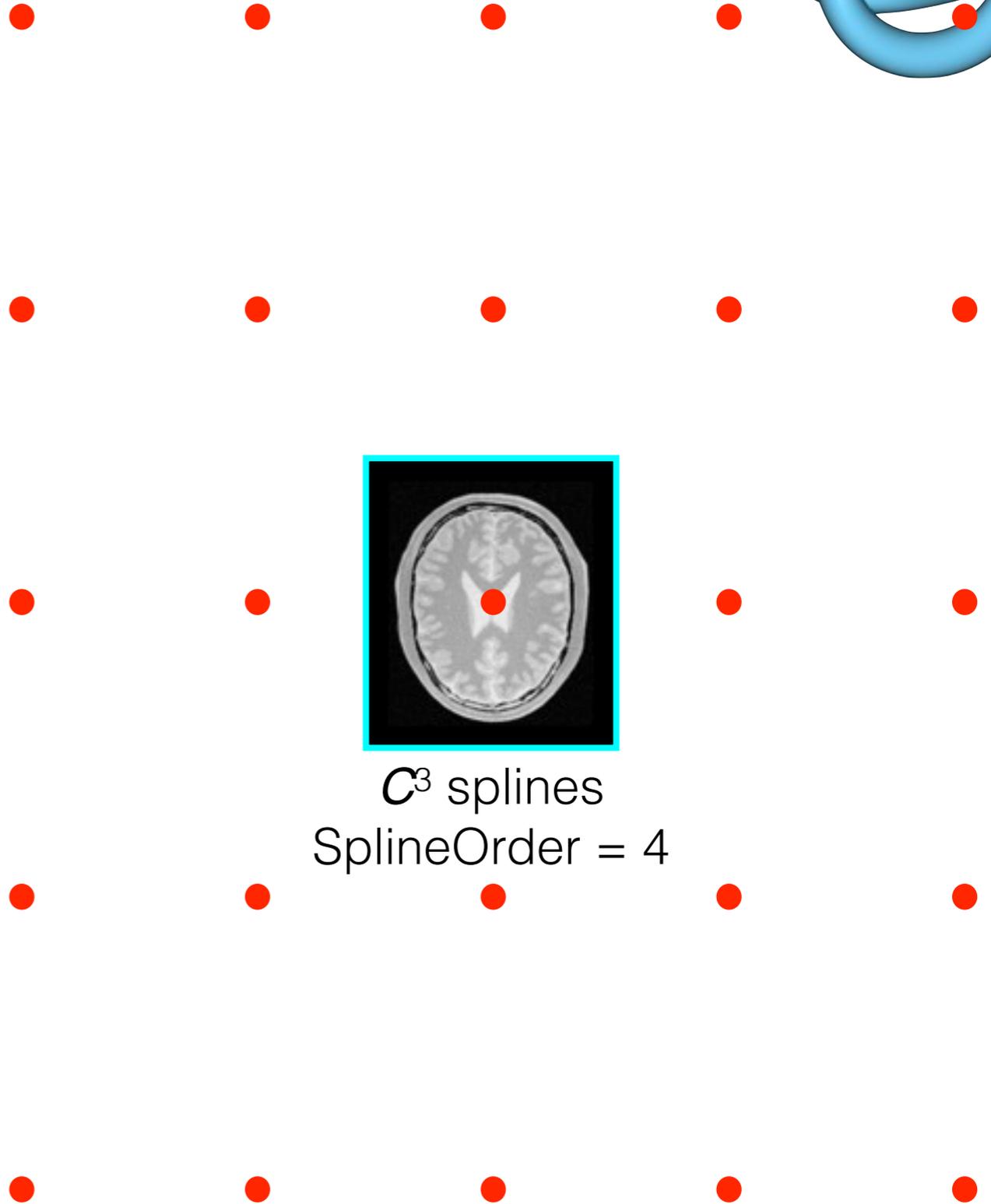


# Domain summary

---

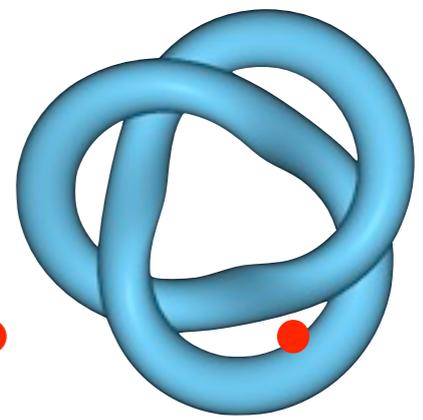


`meshSize[d] = numberOfControlPoints[d] - SplineOrder`



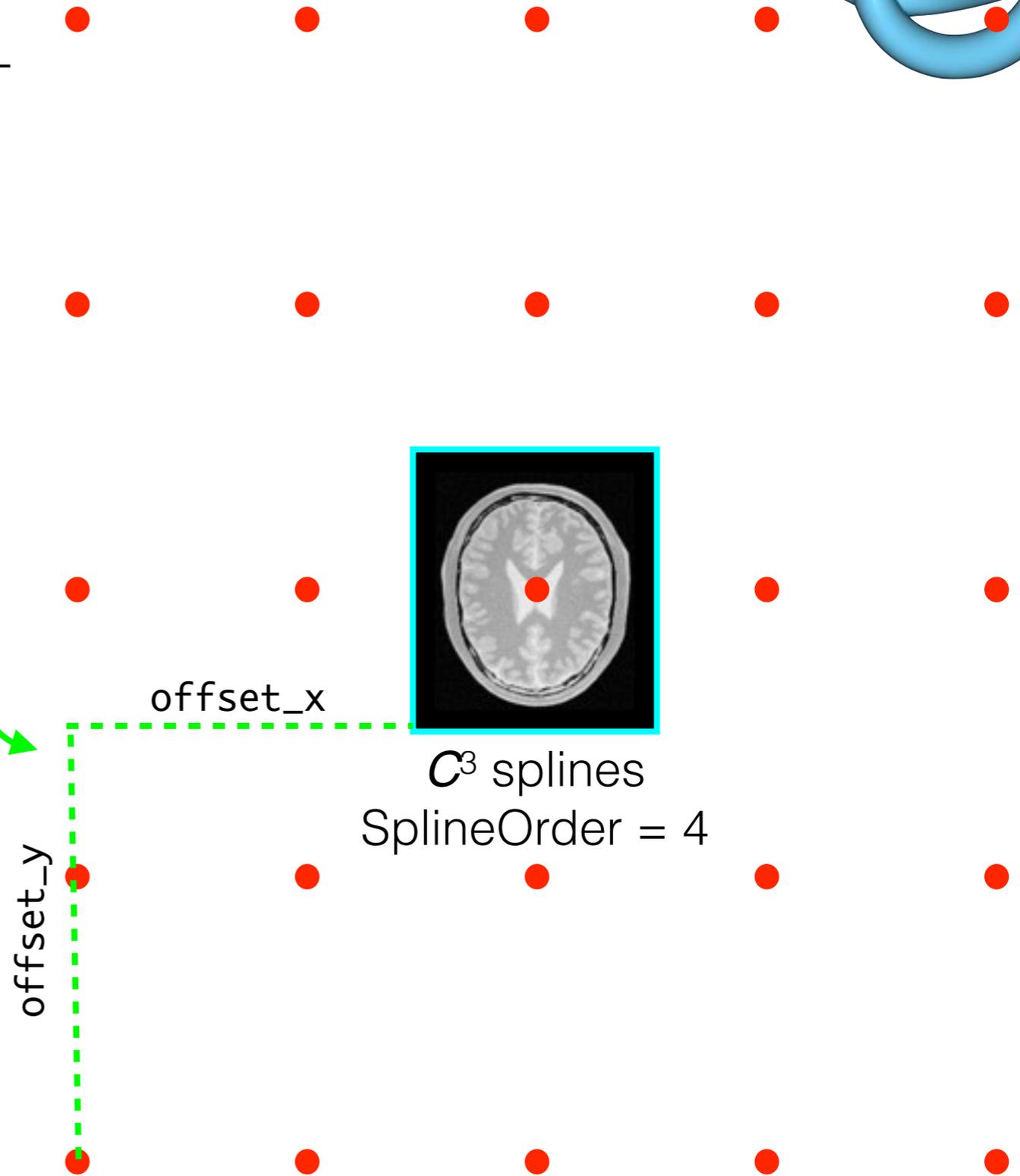
$C^3$  splines  
SplineOrder = 4

# Domain summary

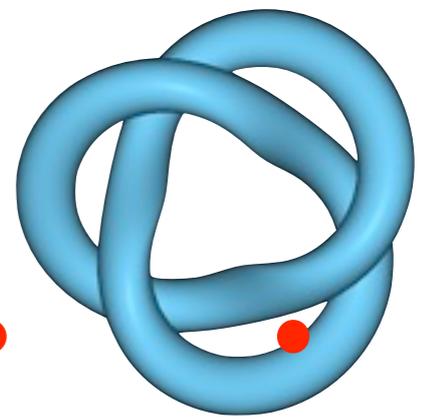


$\text{meshSize}[d] = \text{numberOfControlPoints}[d] - \text{SplineOrder}$

$\text{offset}[d] = 0.5 * (\text{SplineOrder} - 1) * \text{gridSpacing}[d]$



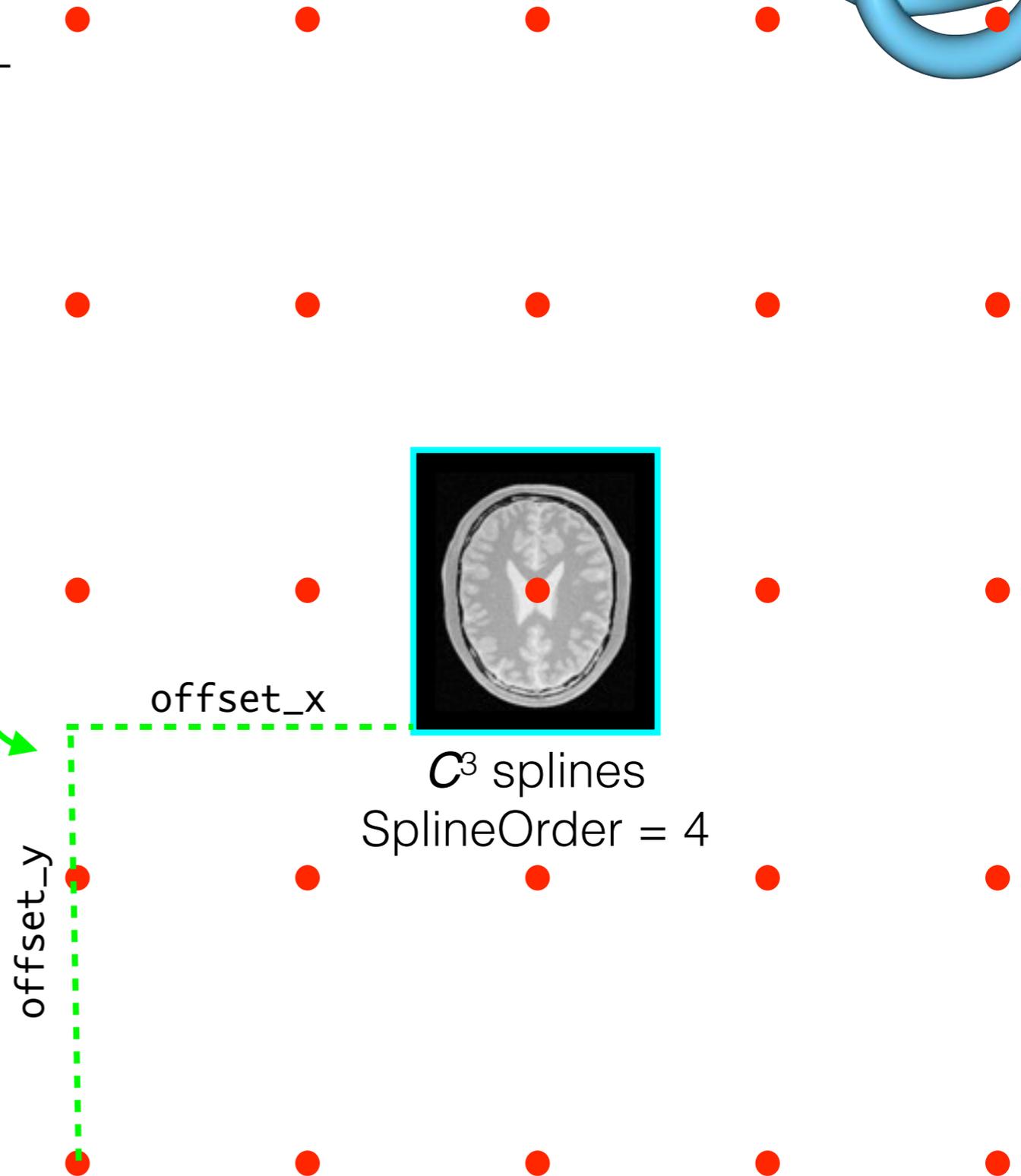
# Domain summary



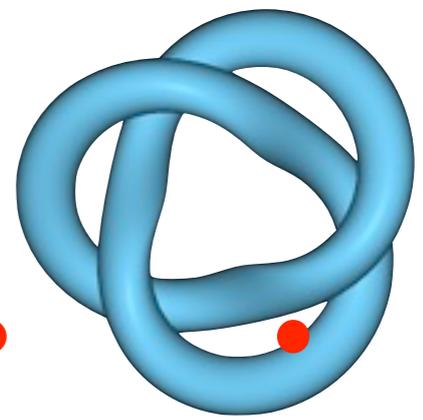
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control point grid is centered on the domain



# Domain summary

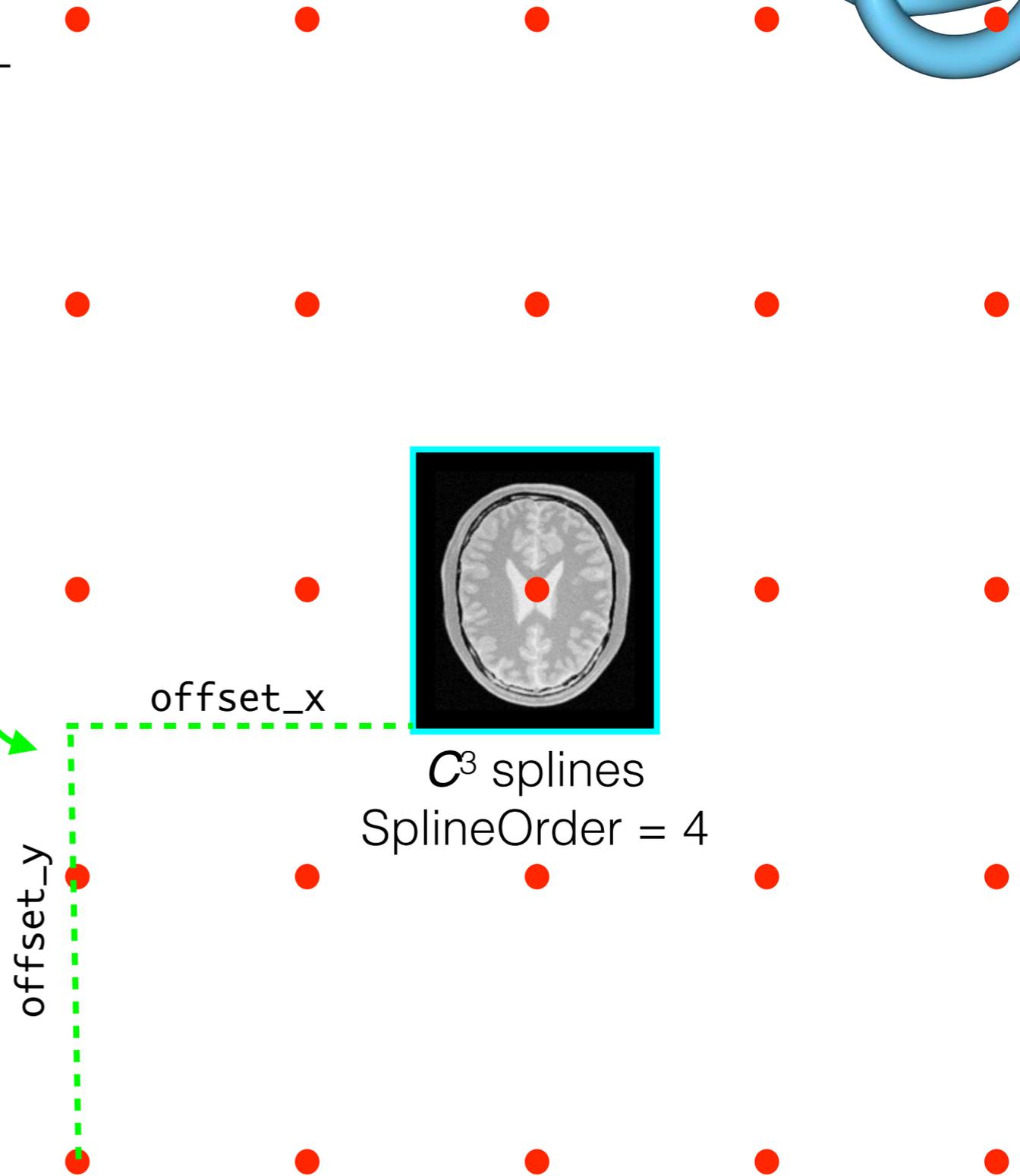
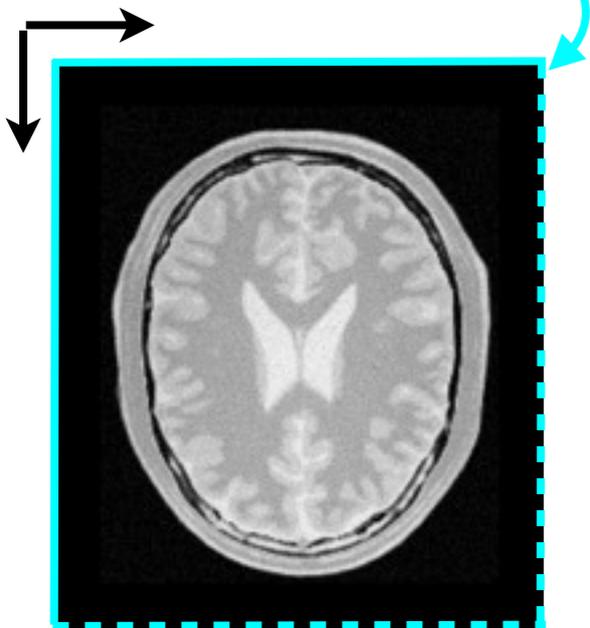


$$\text{meshSize}[d] = \text{numberOfControlPoints}[d] - \text{SplineOrder}$$

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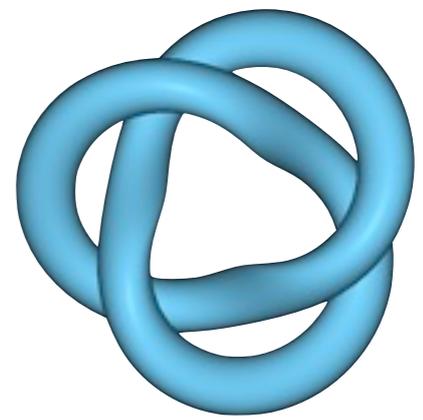
control point grid is centered on the domain

The domain interval is right open-ended, i.e.



# B-spline transform domain changes

---



Proposed interface change:

```
transform->SetTransformDomainOrigin( origin );  
transform->SetTransformDomainPhysicalDimensions( dimensions );  
transform->SetTransformDomainDirection( direction );  
transform->SetTransformDomainMeshSize( meshSize );
```

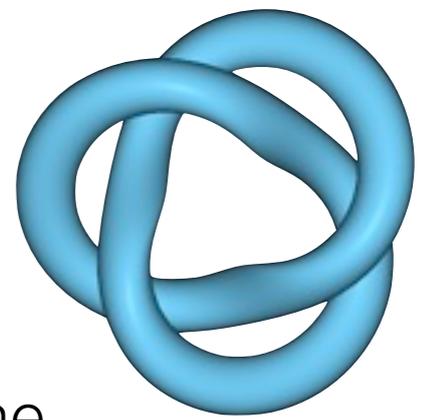
This seems to me a much more B-spline-novice friendly interface as the B-spline domain is continuous over a certain finite domain and a typical user can intuit a uniform, rectilinear mesh uniformly placed over that domain of interest (perhaps more FEM-like?).

OLD

```
transform->SetControlPointGridSpacing( something )  
transform->SetControlPointGridOrigin( something )  
etc
```

# B-spline transform initializer

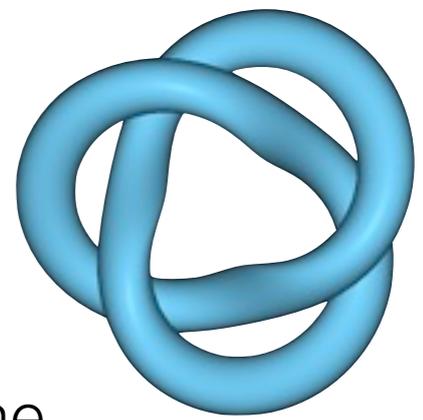
---



These changes would seemingly obviate the need for a transform initializer except for a “bug” pointed out by Hans Johnson. Since the number of control points in a specific direction directly influences the regularization in the direction, it’s important that the B-spline control point grid is placed relative to the image *as it resides in physical space*.

# B-spline transform initializer

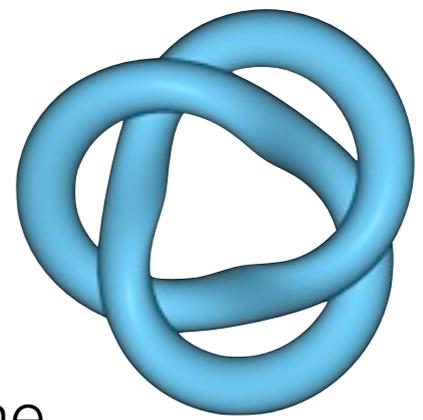
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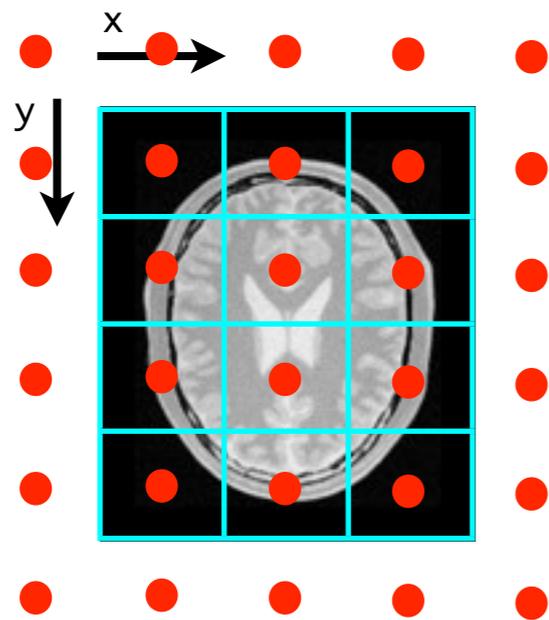
Example: current behavior of the initializer

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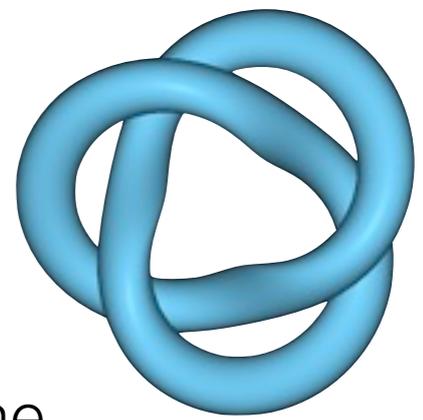
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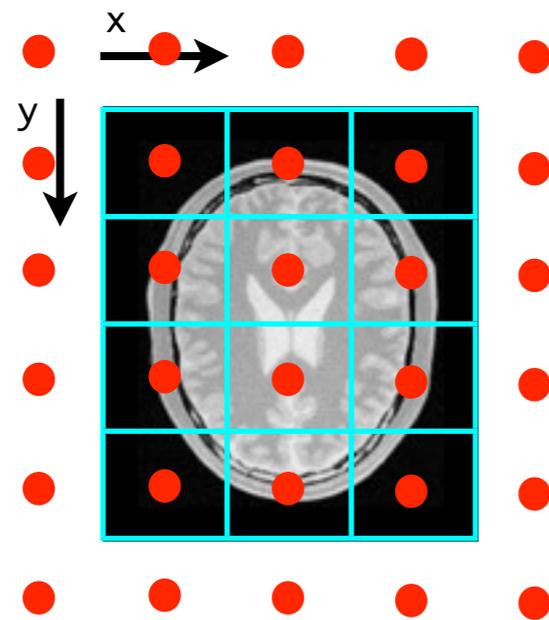
3x4 mesh, quadratic splines,  
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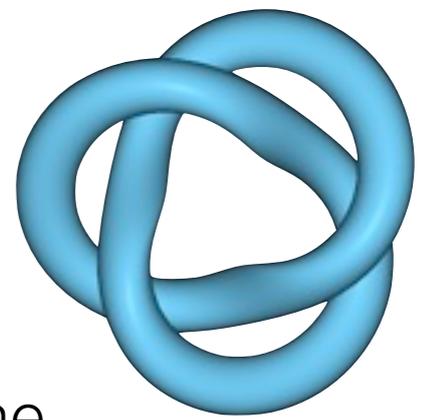
`itkPermuteAxesImageFilter`

direction cosines change but the image resides in physical space precisely as before



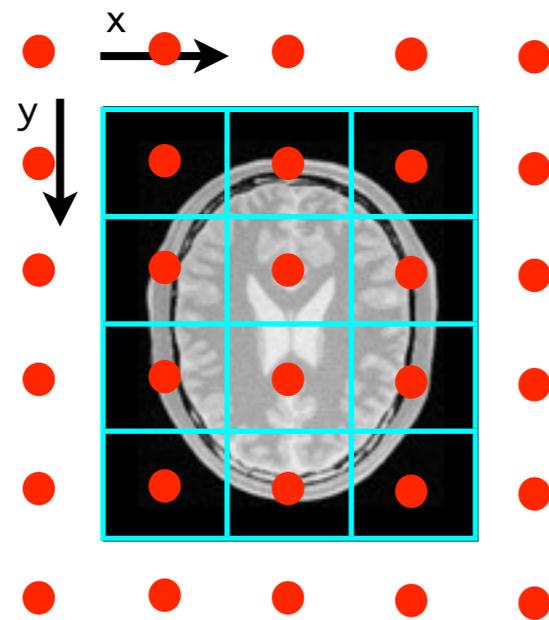
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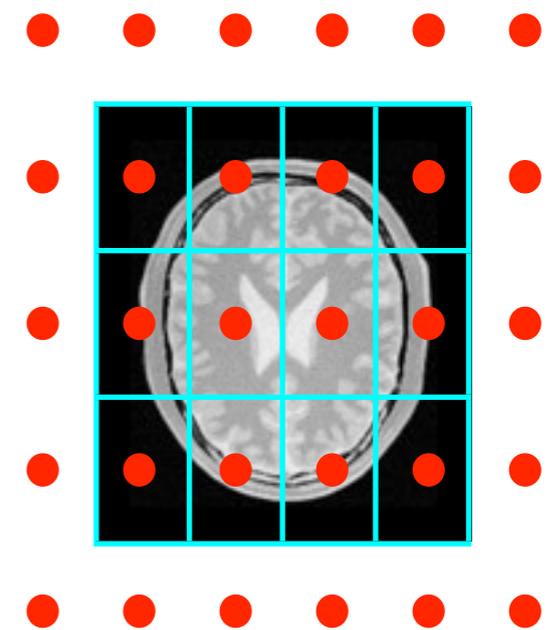
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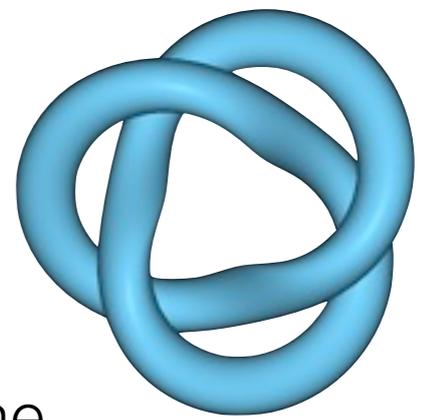
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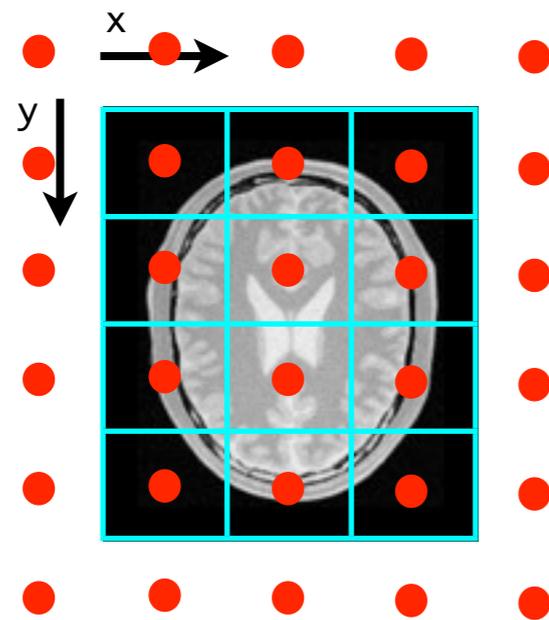
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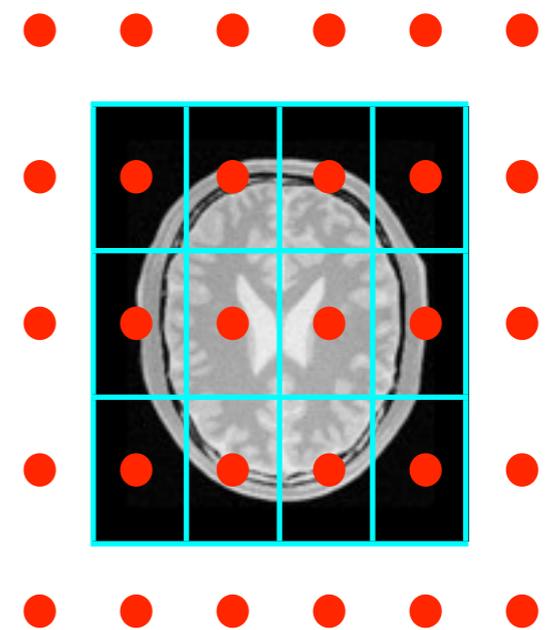
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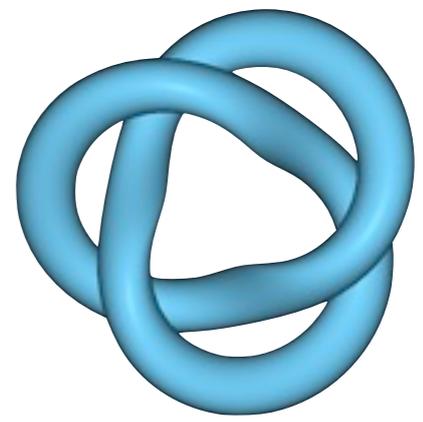


4x3 mesh, quadratic splines,  
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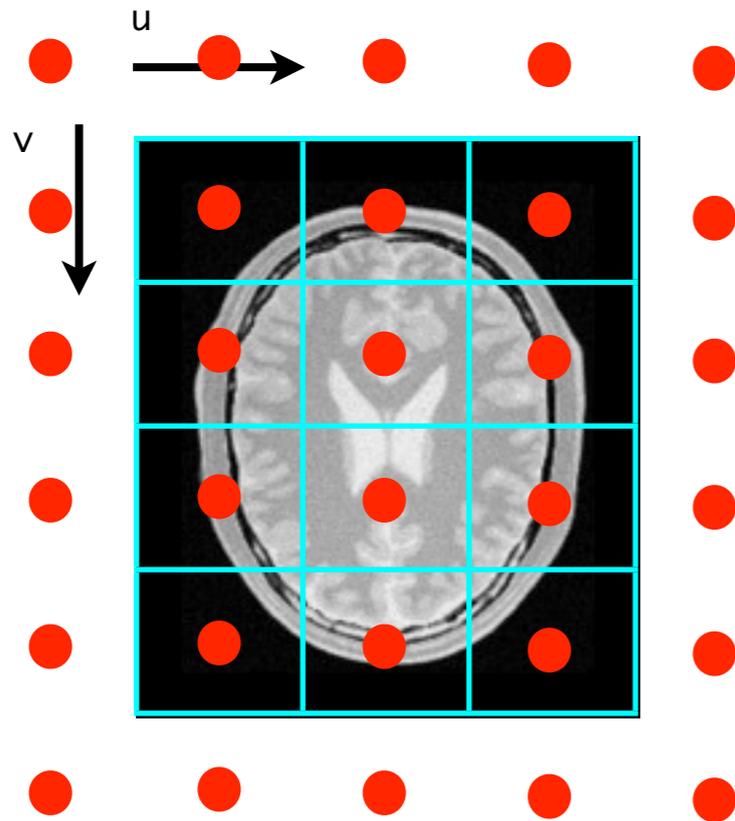
*To remedy this, we have introduced a new B-spline transform initializer which takes the n-D fixed image and calculates its location and pose based on the location of its 2<sup>D</sup> corners.*

# B-spline deformation field transform

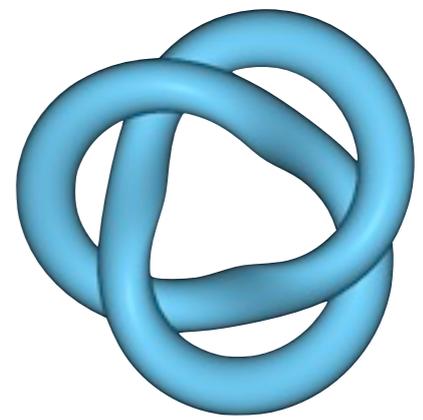
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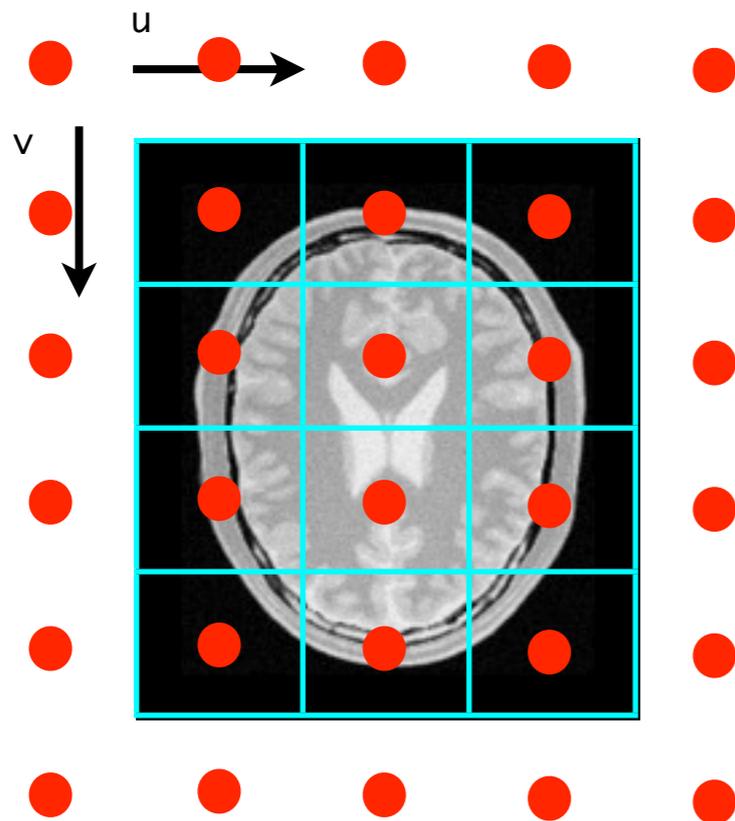
One of the other B-spline related issues we are hoping to address is the time it takes to perform image registration. Currently, various sampling strategies and large memory overhead are used to trim down the time it takes to perform registration. The following is another possibility.



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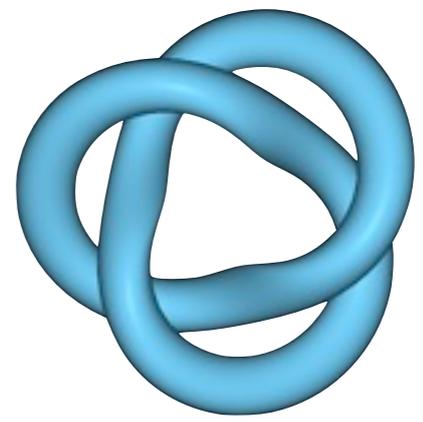


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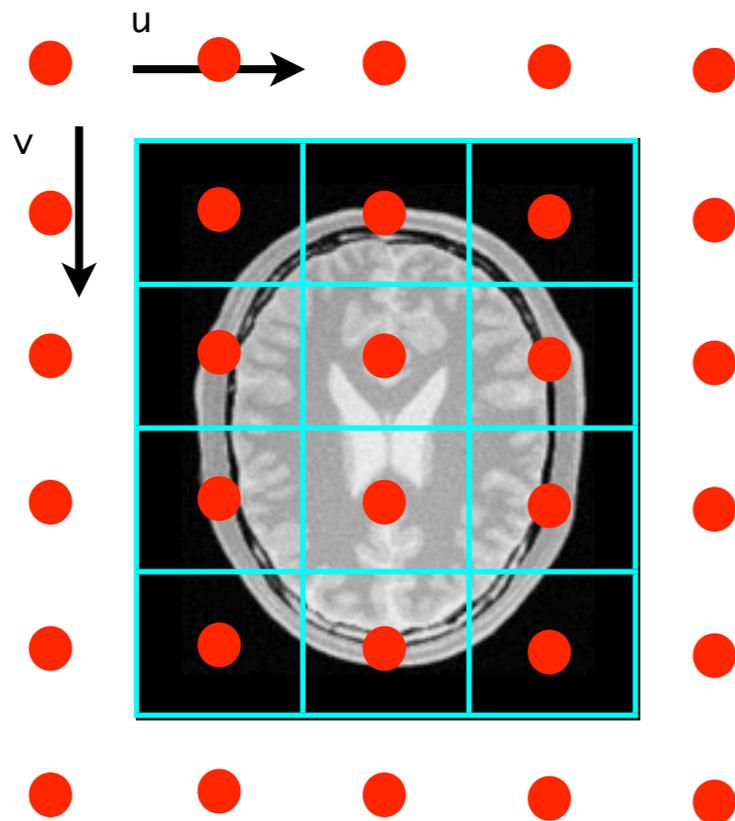


This is how the B-spline transform is currently evaluated via the transform point function:

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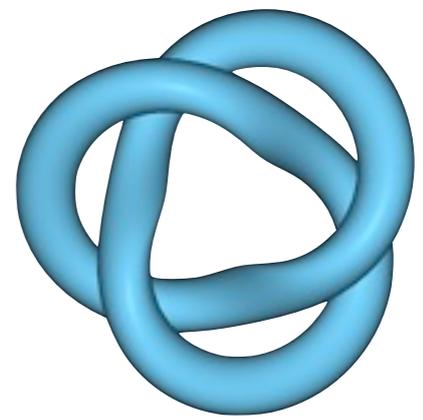
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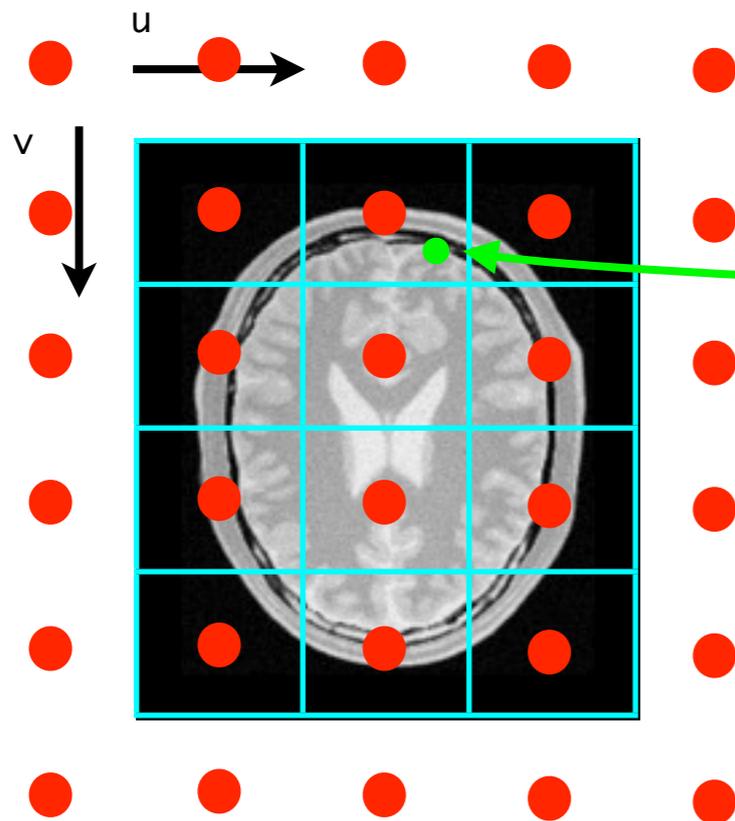
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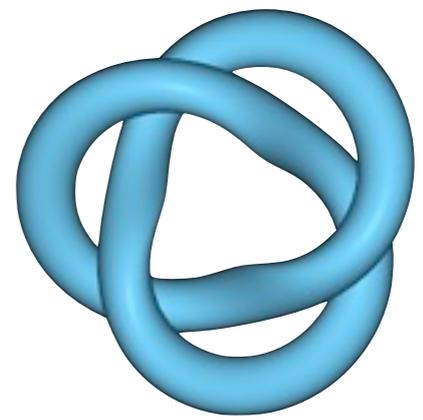
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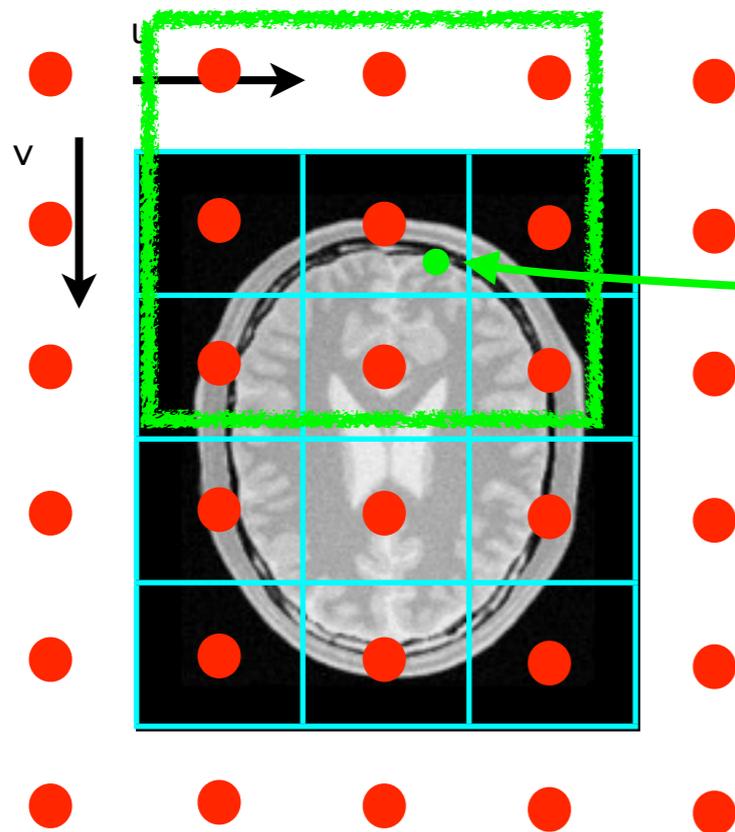
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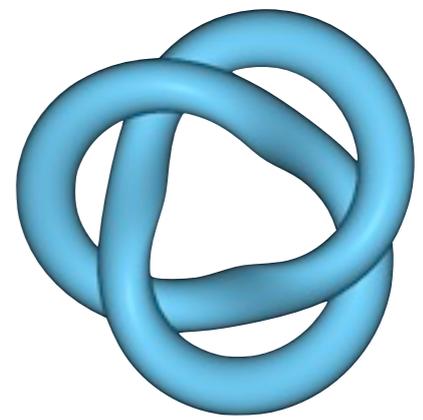


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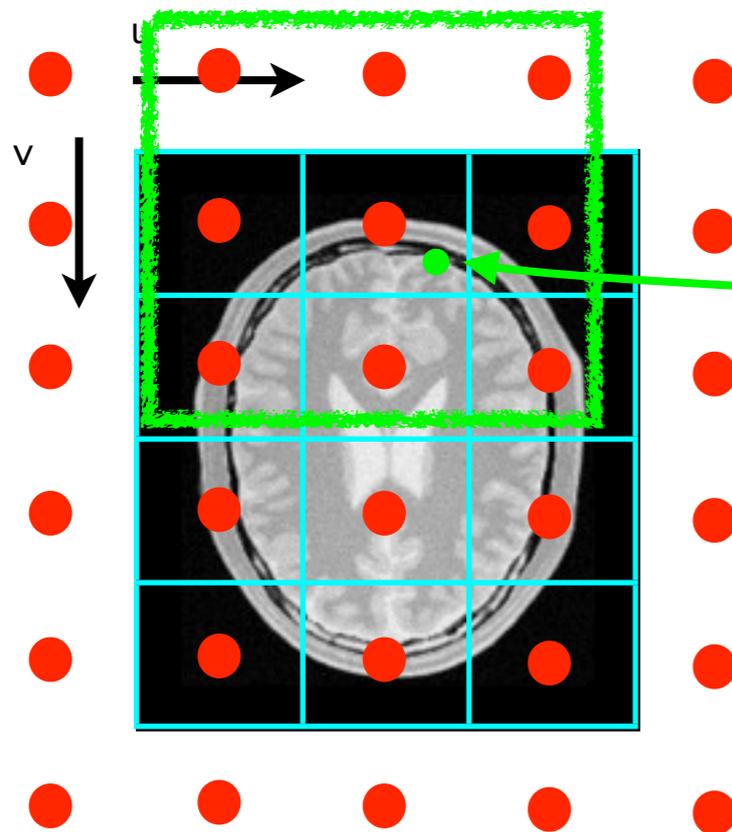
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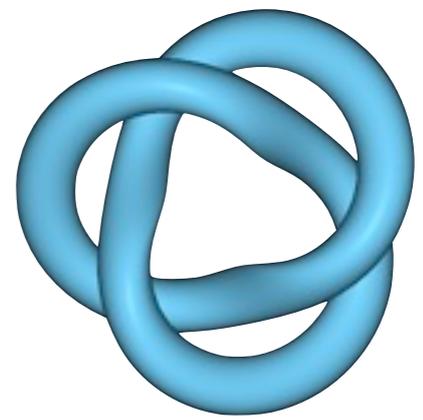


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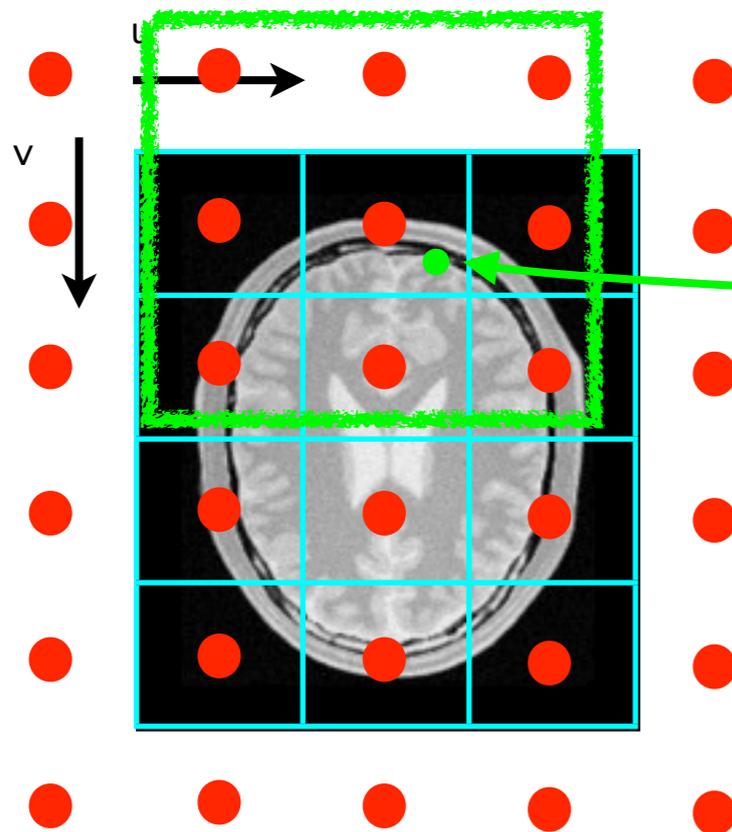
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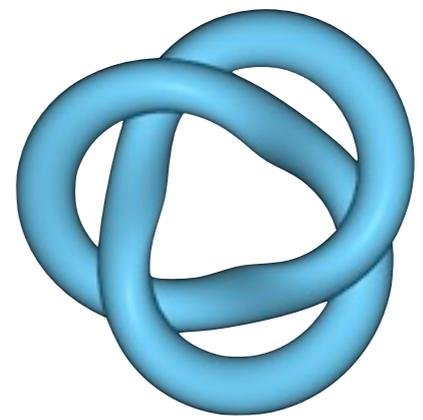
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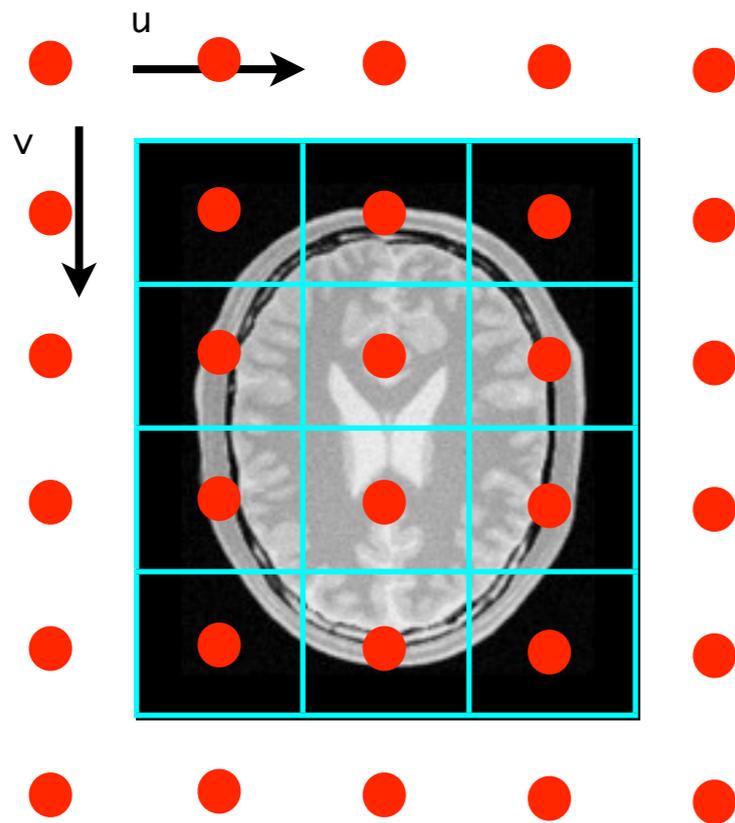
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Most commonly people use cubic B-splines in 3-D which means that for *each* input point, one has to calculate  $4 \times 4 \times 4 = 64$  B-spline weights! Storing the weights is currently used but this is a huge memory cost alternative.

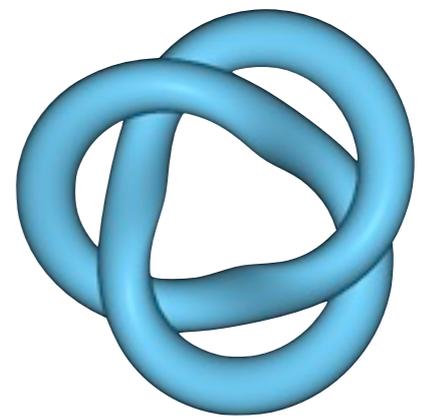
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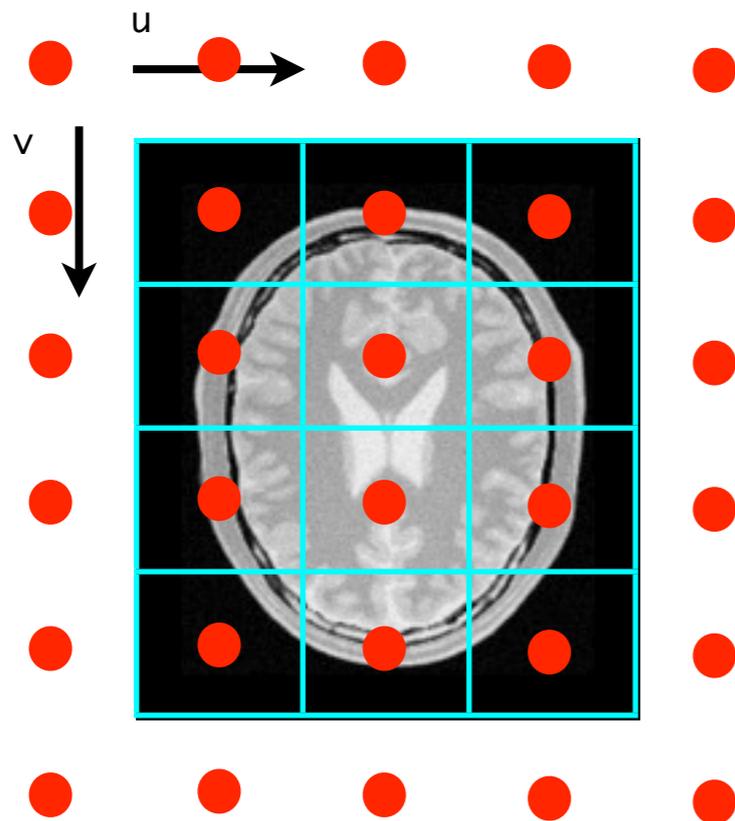
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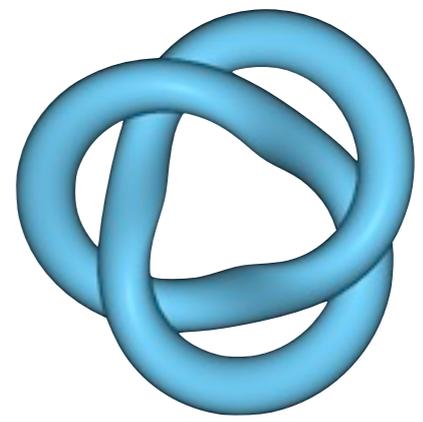


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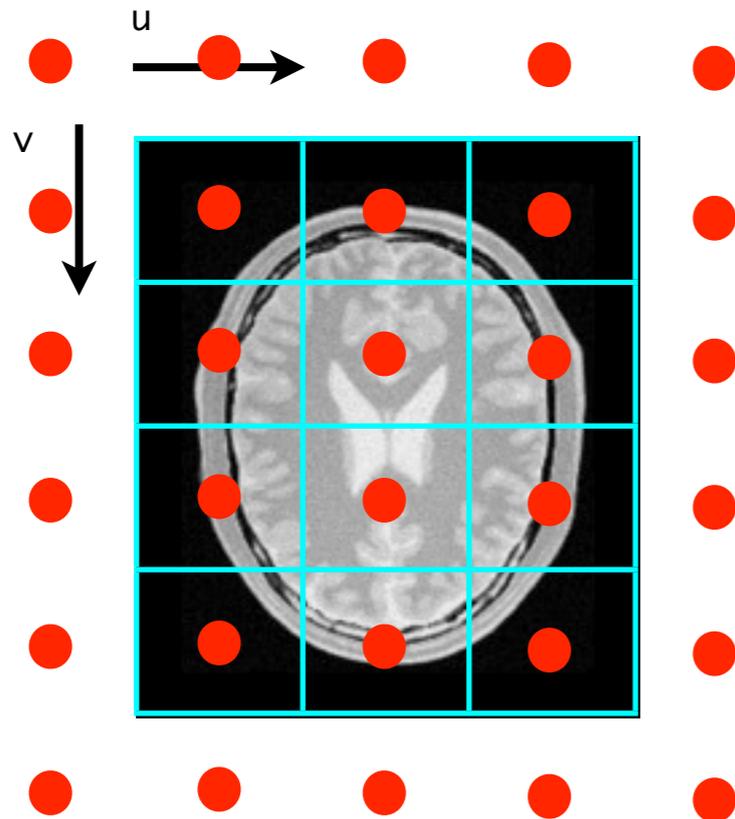


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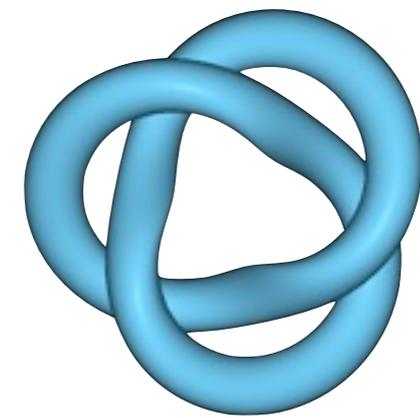
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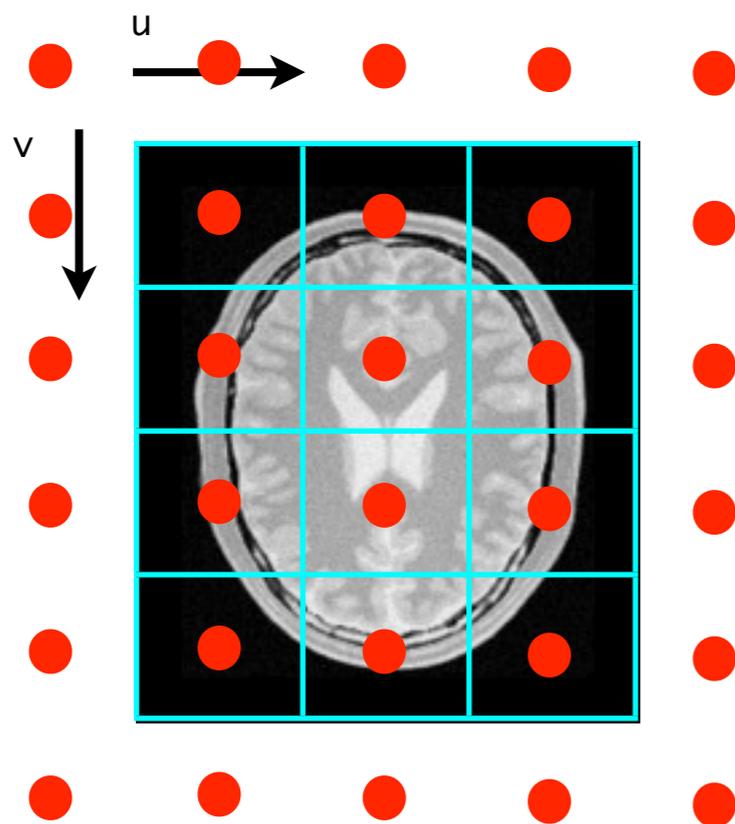
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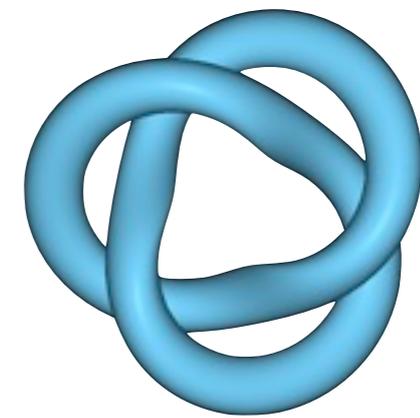


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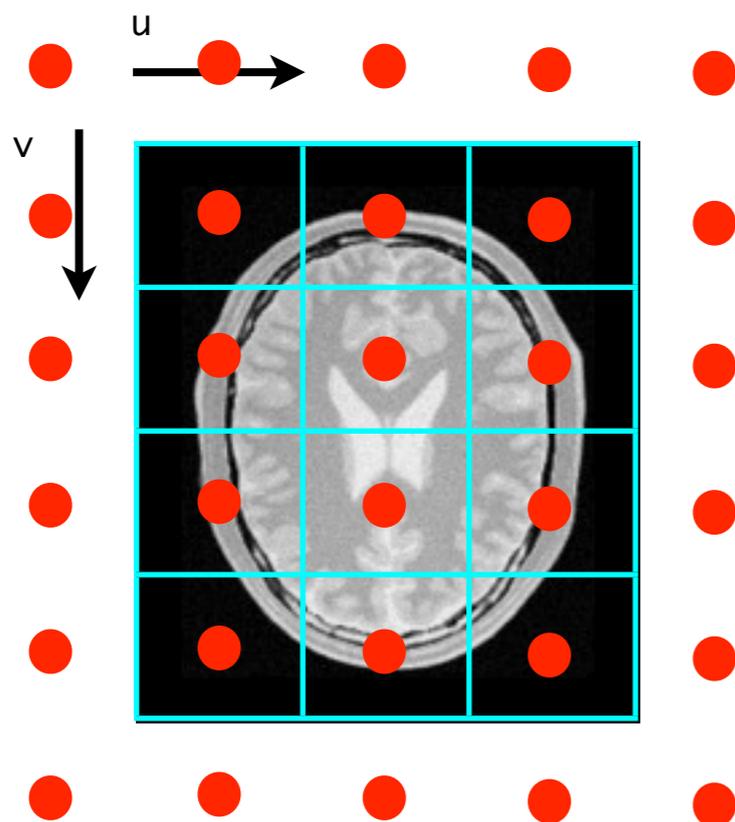
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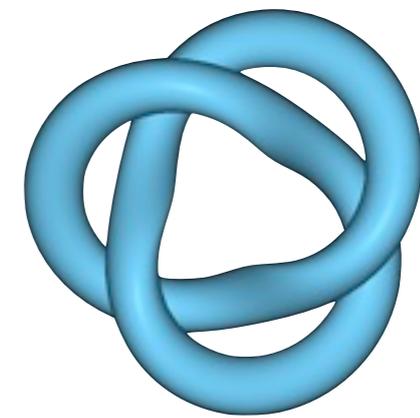


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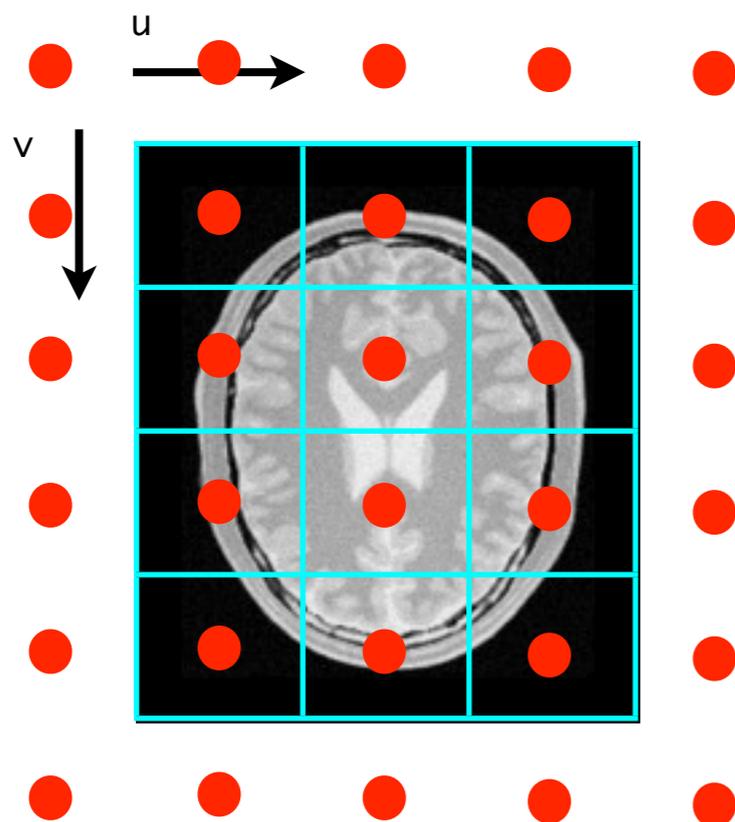
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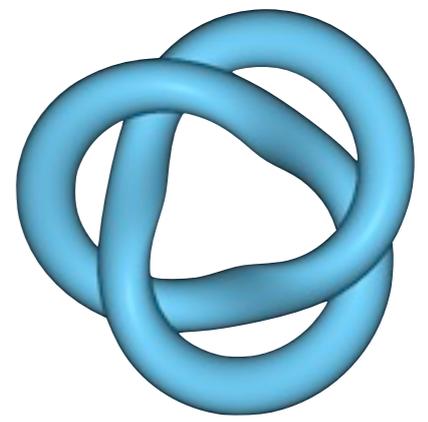
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- **Still need to work on DTI.** How much interest?

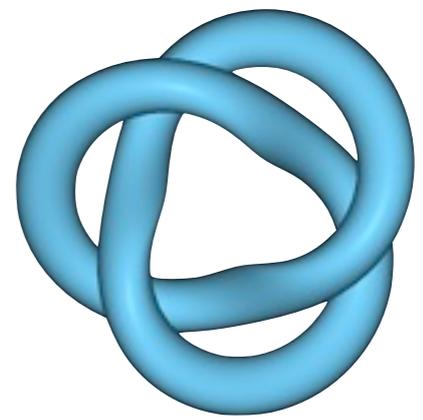
# CSV file reader/writer

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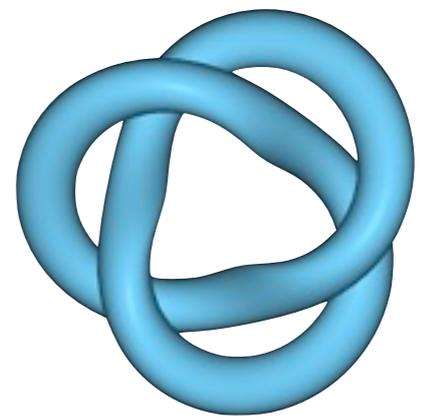
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A starter project for one of our developers, Shreyas.

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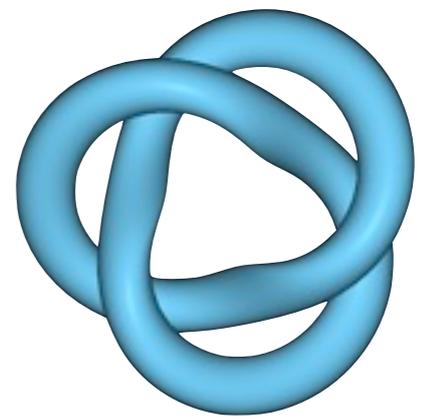


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Is currently in Gerrit.

# Pipeline: 4D Processing + SCCA

