

$$\phi_t = \nabla \cdot (D \nabla \phi)$$

$$\nabla \phi = \begin{bmatrix} \frac{\partial \phi}{\partial x} \\ \frac{\partial \phi}{\partial y} \\ \frac{\partial \phi}{\partial z} \end{bmatrix}$$

$$D = \begin{bmatrix} D_{11} & D_{21} & D_{31} \\ D_{12} & D_{22} & D_{32} \\ D_{13} & D_{23} & D_{33} \end{bmatrix}$$

$$D \nabla \phi = \begin{bmatrix} D_{11} \frac{\partial \phi}{\partial x} + D_{21} \frac{\partial \phi}{\partial y} + D_{31} \frac{\partial \phi}{\partial z} \\ D_{12} \frac{\partial \phi}{\partial x} + D_{22} \frac{\partial \phi}{\partial y} + D_{32} \frac{\partial \phi}{\partial z} \\ D_{13} \frac{\partial \phi}{\partial x} + D_{23} \frac{\partial \phi}{\partial y} + D_{33} \frac{\partial \phi}{\partial z} \end{bmatrix}$$

$$\nabla = \begin{bmatrix} \frac{\partial \phi}{\partial x} \\ \frac{\partial \phi}{\partial y} \\ \frac{\partial \phi}{\partial z} \end{bmatrix}$$

$$\cdot D \nabla \phi = \frac{\partial}{\partial x} \left[D_{11} \frac{\partial \phi}{\partial x} + D_{21} \frac{\partial \phi}{\partial y} + D_{31} \frac{\partial \phi}{\partial z} \right]$$

$$+ \frac{\partial}{\partial y} \left[D_{12} \frac{\partial \phi}{\partial x} + D_{22} \frac{\partial \phi}{\partial y} + D_{32} \frac{\partial \phi}{\partial z} \right]$$

$$+ \frac{\partial}{\partial z} \left[D_{13} \frac{\partial \phi}{\partial x} + D_{23} \frac{\partial \phi}{\partial y} + D_{33} \frac{\partial \phi}{\partial z} \right]$$